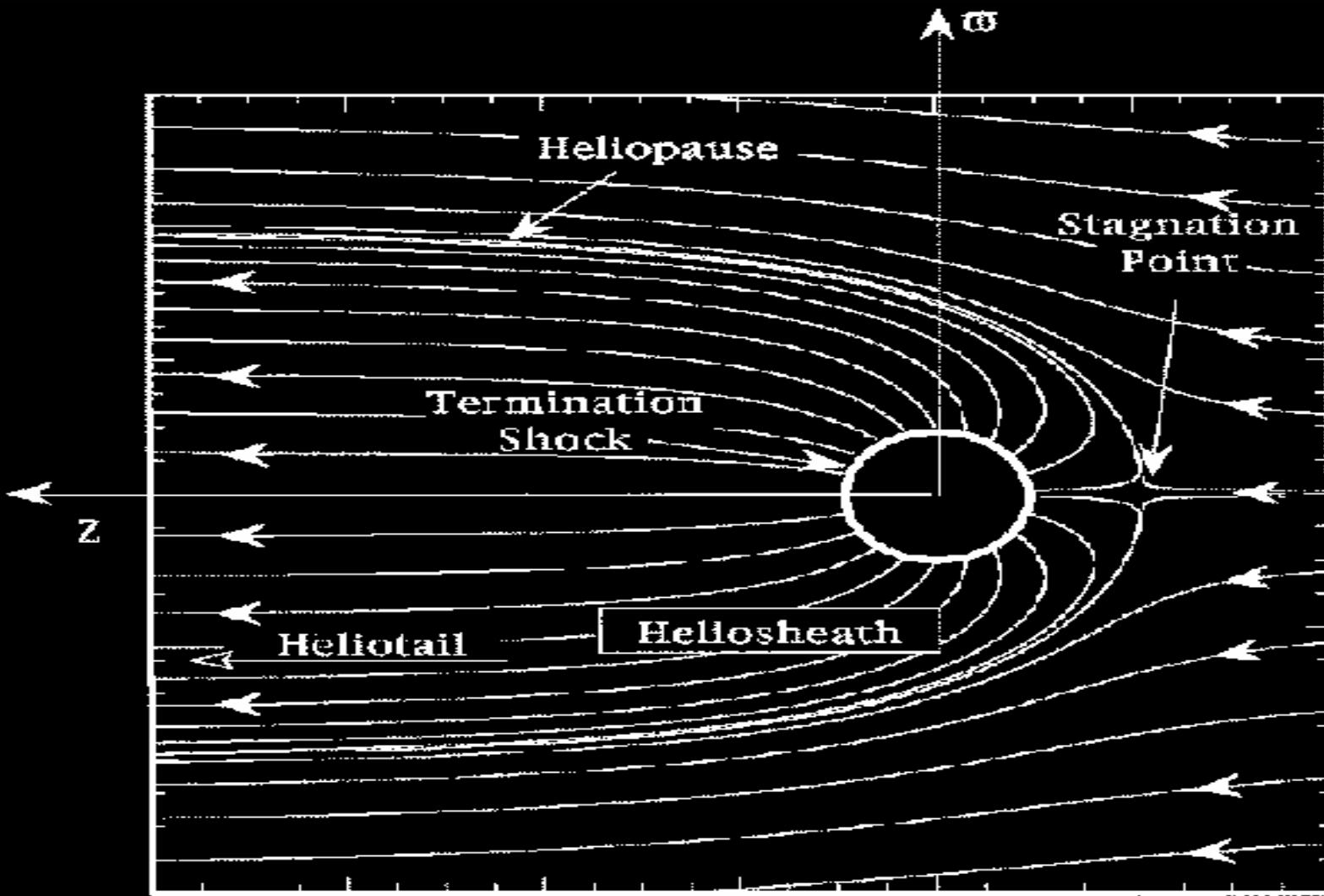


The **heliosphere** is a huge region in the Galaxy produced by the interaction of the solar wind with the interstellar medium, low density hydrogen and helium gas that permeates the local interstellar medium.



# *The heliosphere*

X. Moussas

University of Athens, Faculty of Physics, Laboratory of Astrophysics, Athens, Greece  
xmoussas @ phys.uoa.gr

The heliosphere is a huge region in the Galaxy dominated by the solar wind, rarefied plasma that is continuously emitted by the Sun and expands till its pressure is balanced by the pressure of the interstellar medium that surrounds all stars.

The heliosphere changes continuously from the variations of velocity, density, magnetic field and structure of the solar wind.

The heliosphere is the large scale environment of humans, and as such it greatly affects our lives on Earth (even more in space), mainly through the modulation of cosmic rays.

A brief presentation of the heliosphere is given, fast and slow streams in the heliosphere are described, the heliospheric current sheet, the termination shock, the heliosheath and the heliopause are presented and

its influence to the galactic cosmic rays and energetic particles.

A quick reference is also given concerning education and research on the heliosphere and more generally Space Physics in Greece.

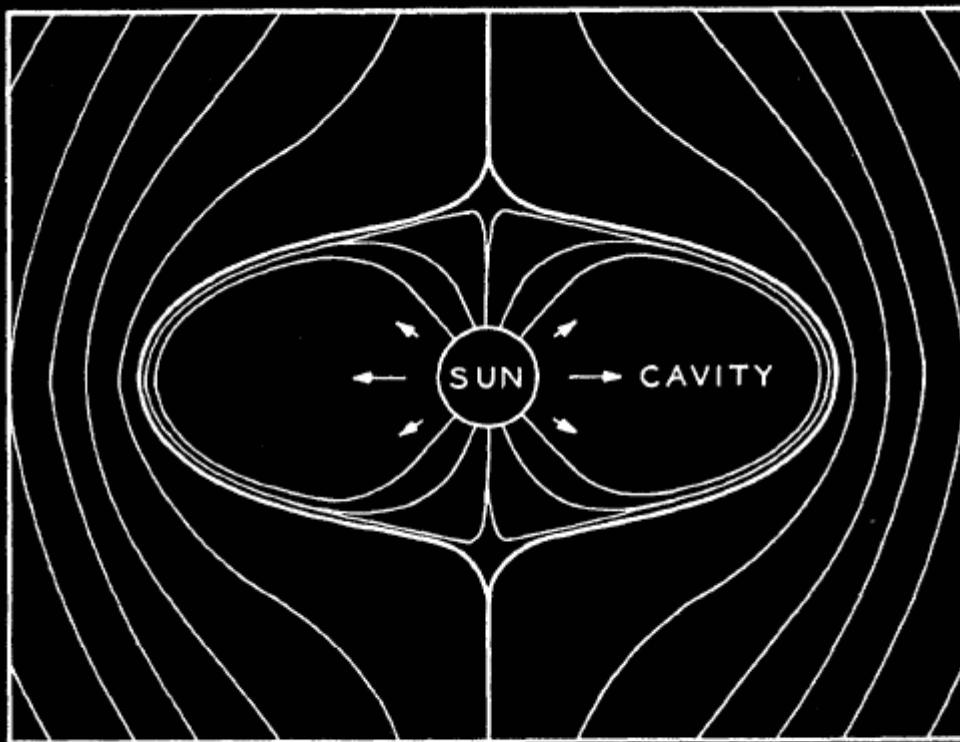
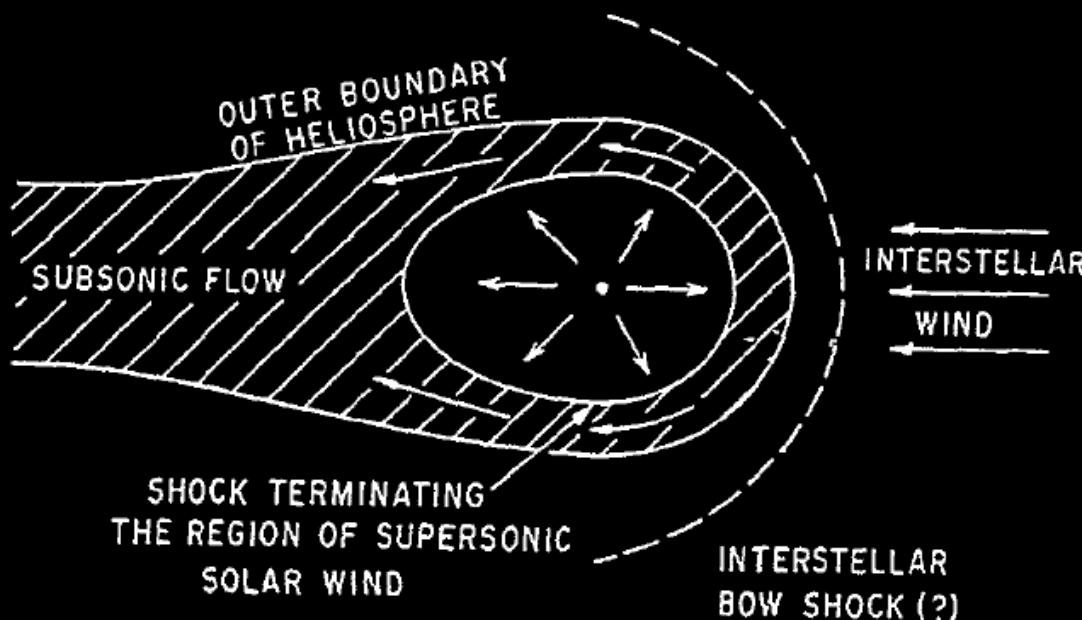


FIG. 1. A possible disposition of a solar magnetic field inside the cavity in the galactic field. The arrows represent the solar corpuscular radiation.

The first suggestions concerning the existence and nature of the heliosphere were made in 1955 by Leverett Davis in connection with the origin and propagation of cosmic rays

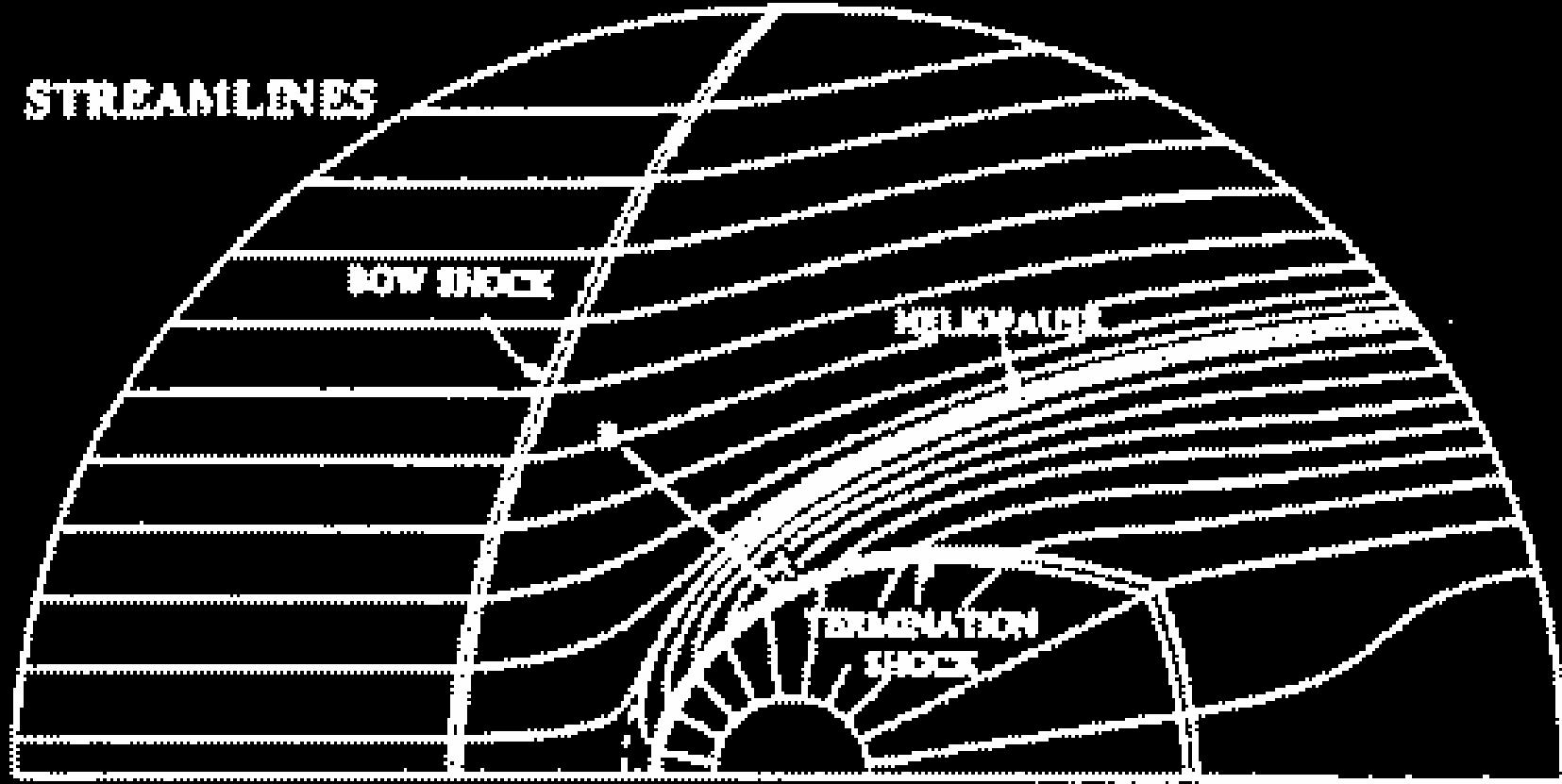


Outer boundary of heliosphere = "heliopause"  
Region of subsonic flow = "heliosheath"

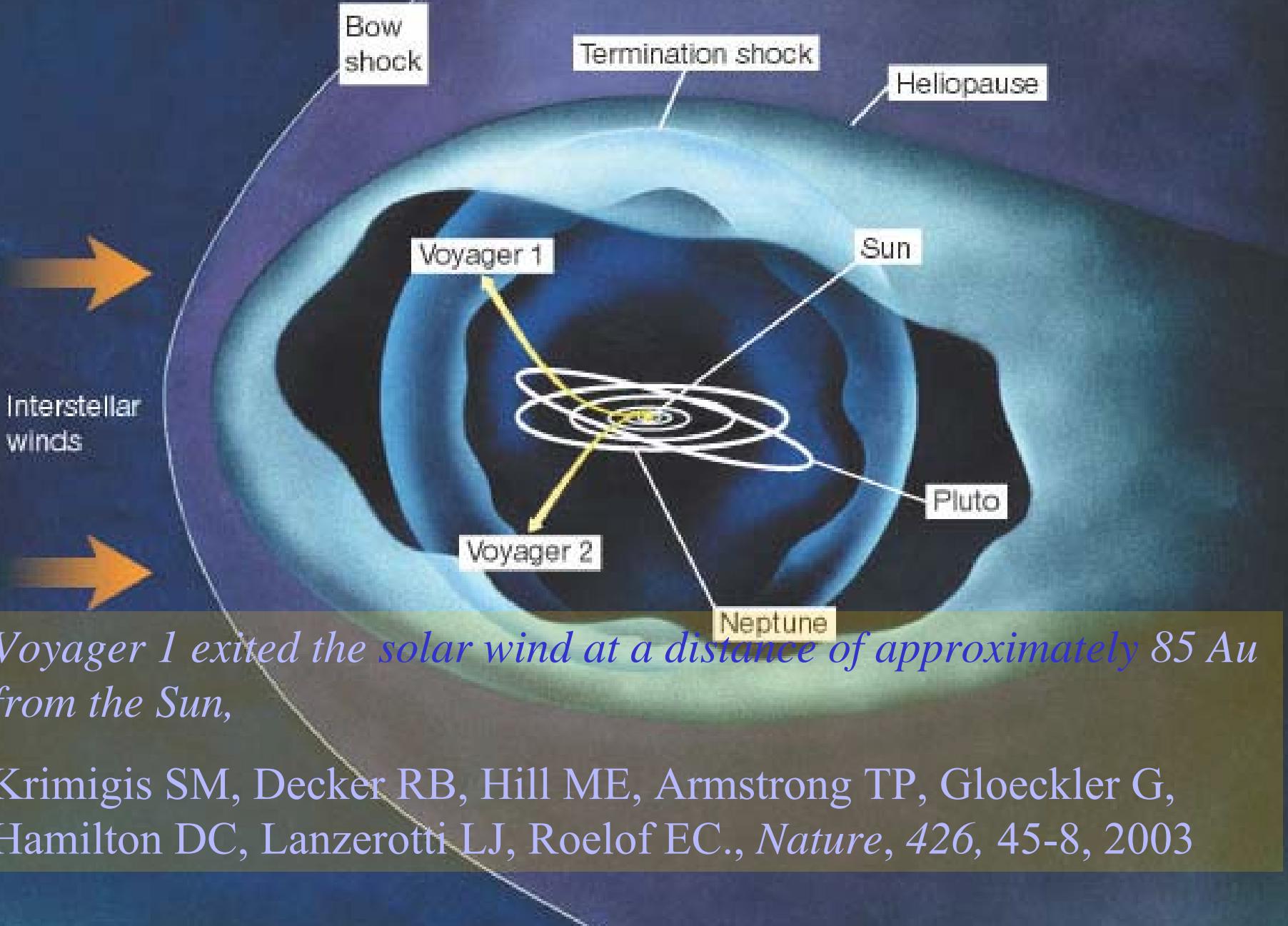
*Figure 1.* The configuration of the heliosphere shown schematically.

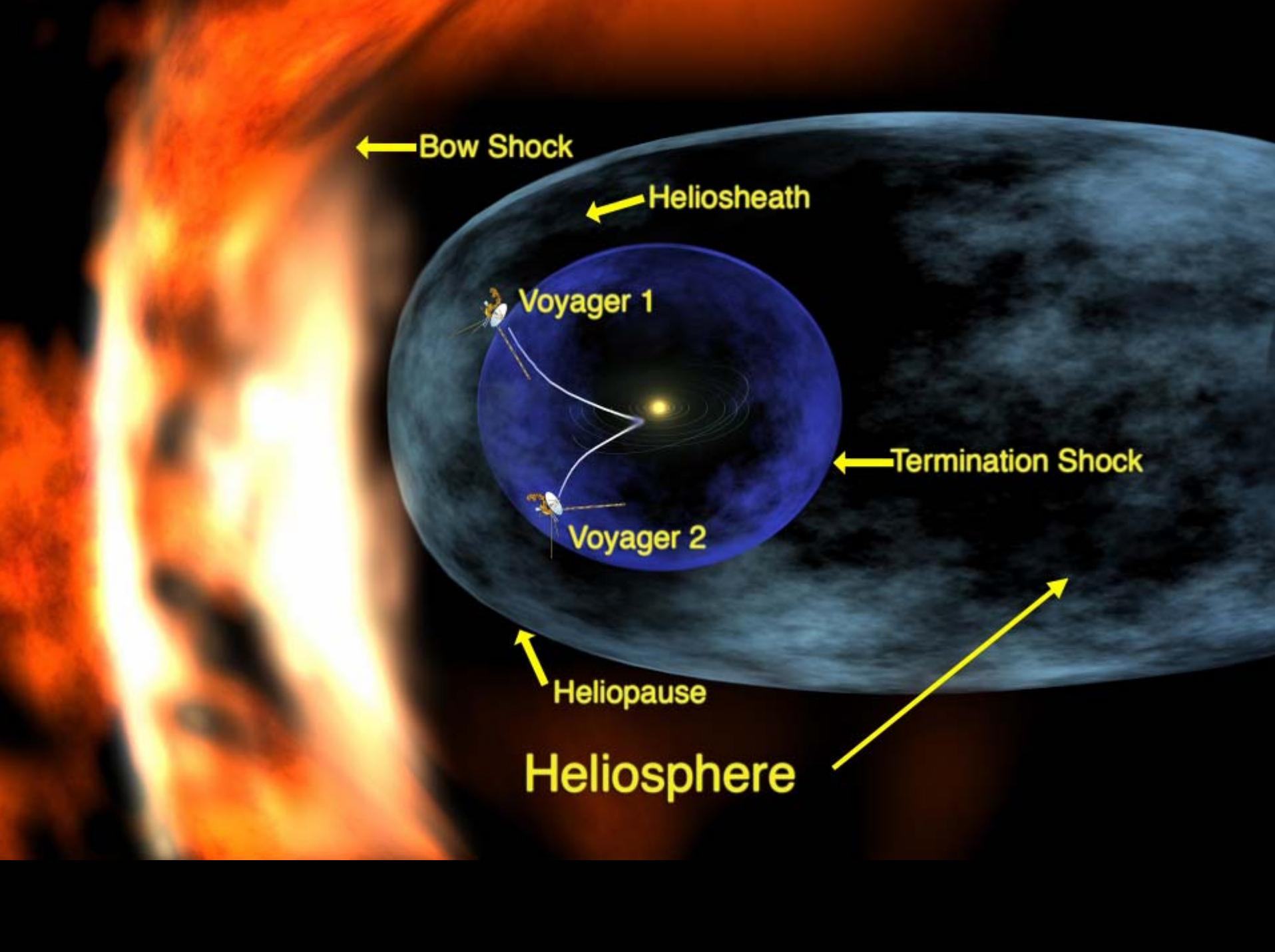
Axford, W. I., The interaction of the solar wind with the interstellar medium, *Solar Wind*, NASA SP-308 (C. P. Sonett, P. J. Coleman, Jr., and J. M. Wilcox, eds.), pp 609-657, NASA, Washington D.C., 1972.

and Axford, *Space Science Reviews* 78: 9-14, 1996.

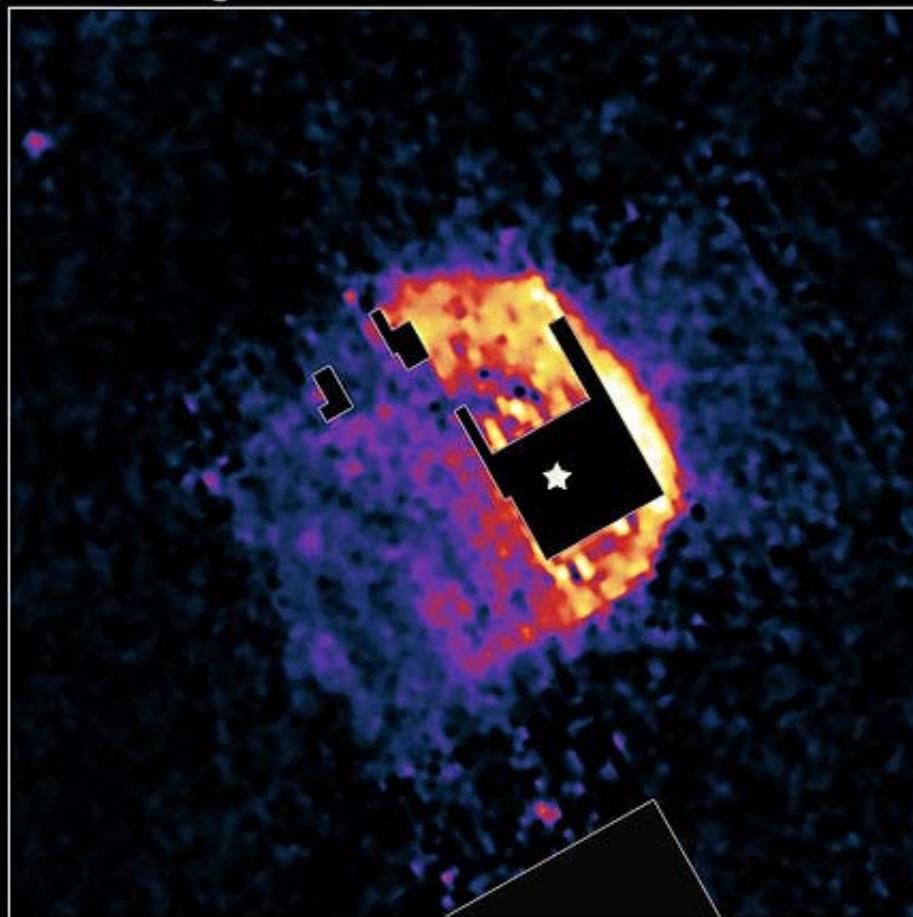


**Heliosphere  
Bow Shock  
Heliopause  
Termination Shock**





Infrared Image



Artist's Concept



NASA/JPL-Caltech / T. Pyle (SSC)

## "Bow Shock" Around Star R Hydri

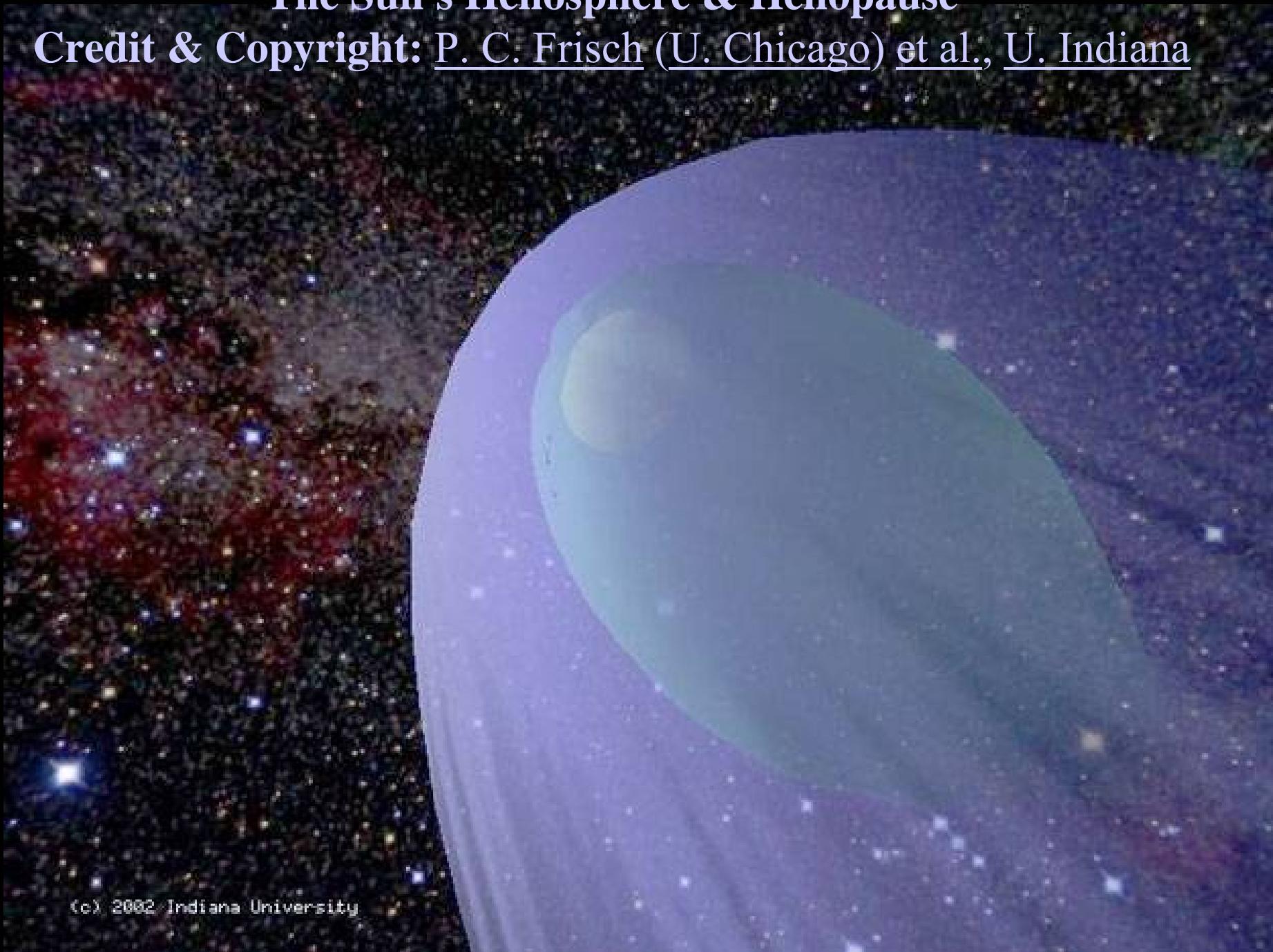
NASA / JPL-Caltech / T. Ueta (University of Denver)

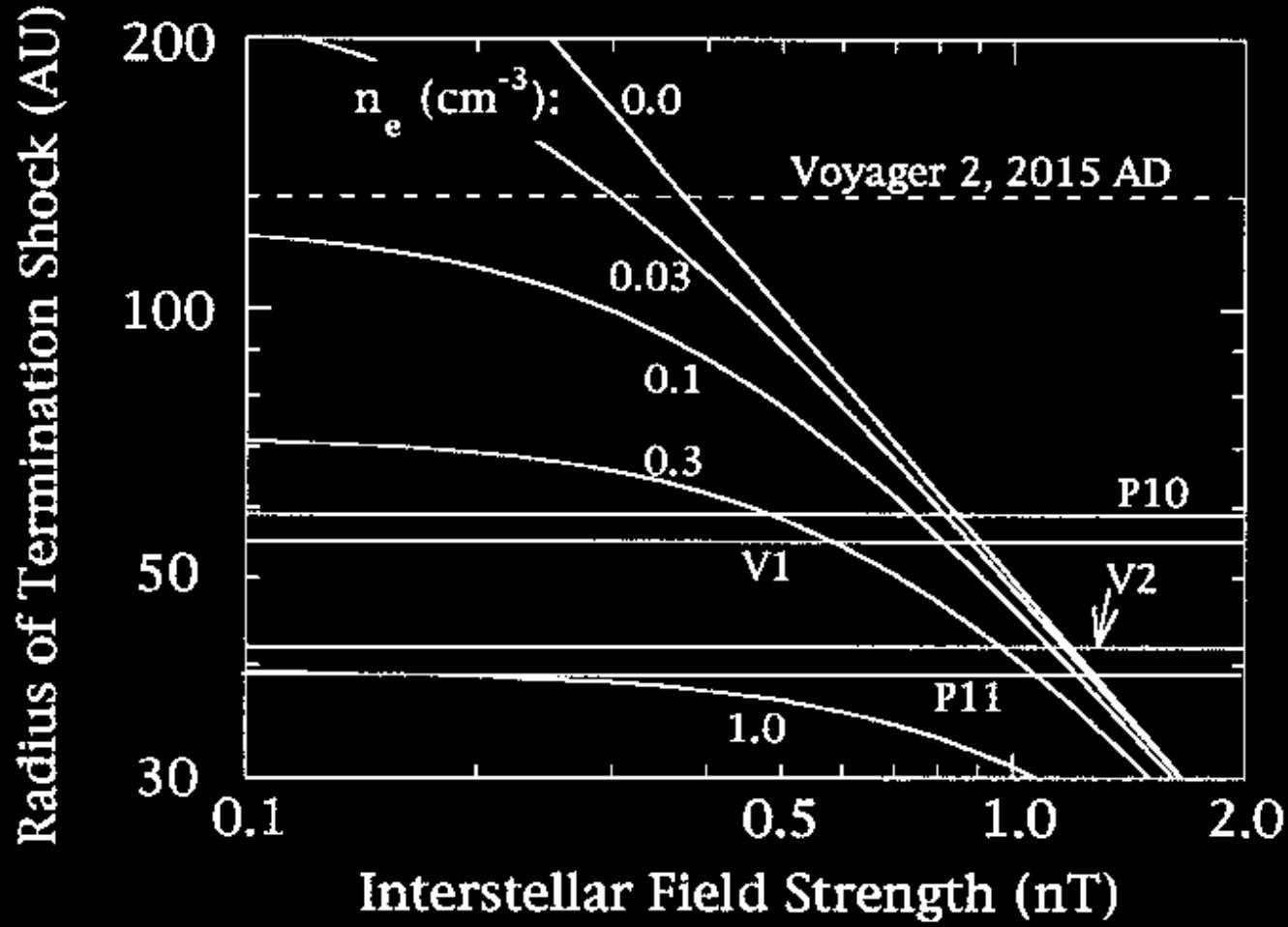
Spitzer Space Telescope • MIPS

sig06-029

# The Sun's Heliosphere & Heliopause

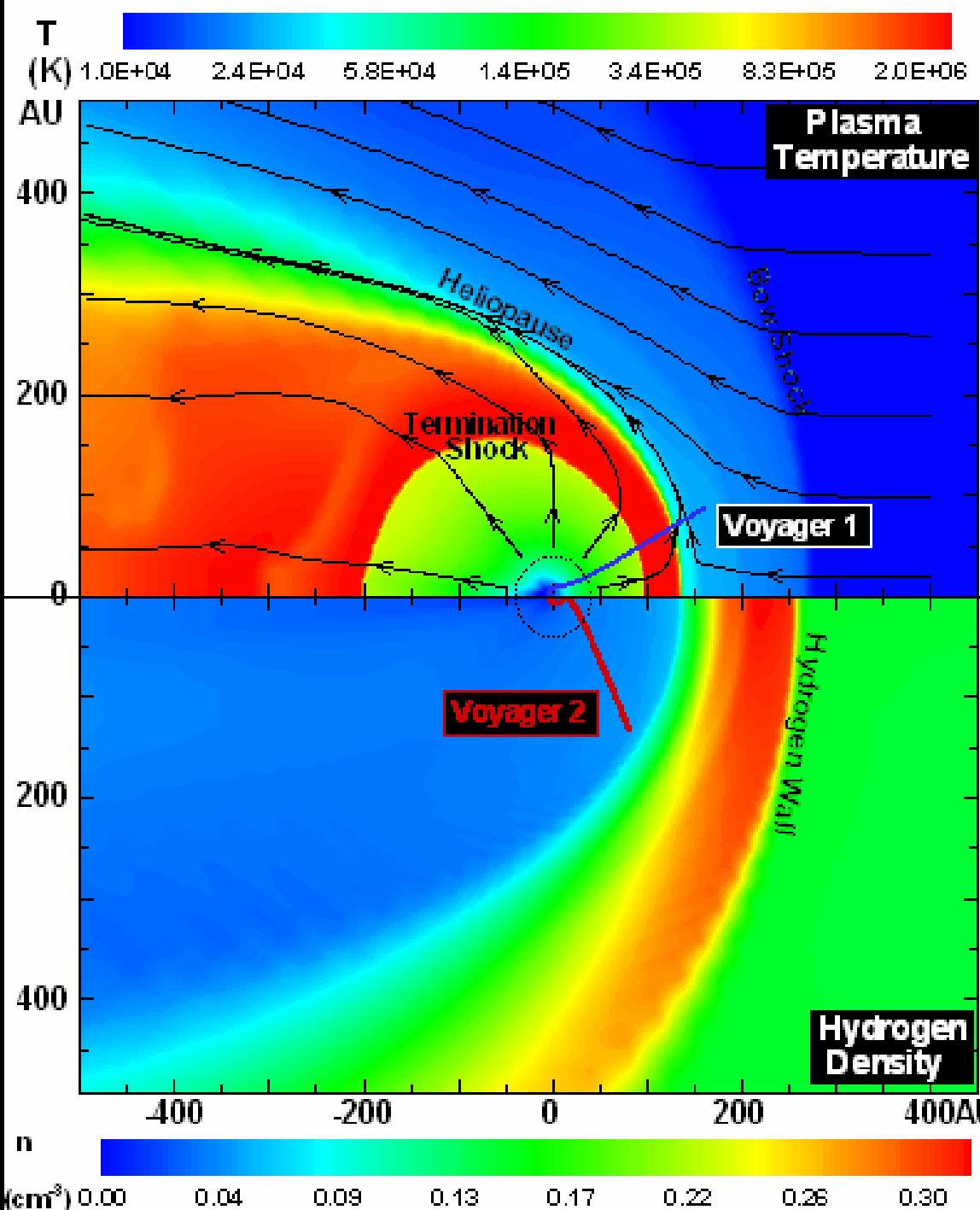
Credit & Copyright: P. C. Frisch (U. Chicago) et al., U. Indiana

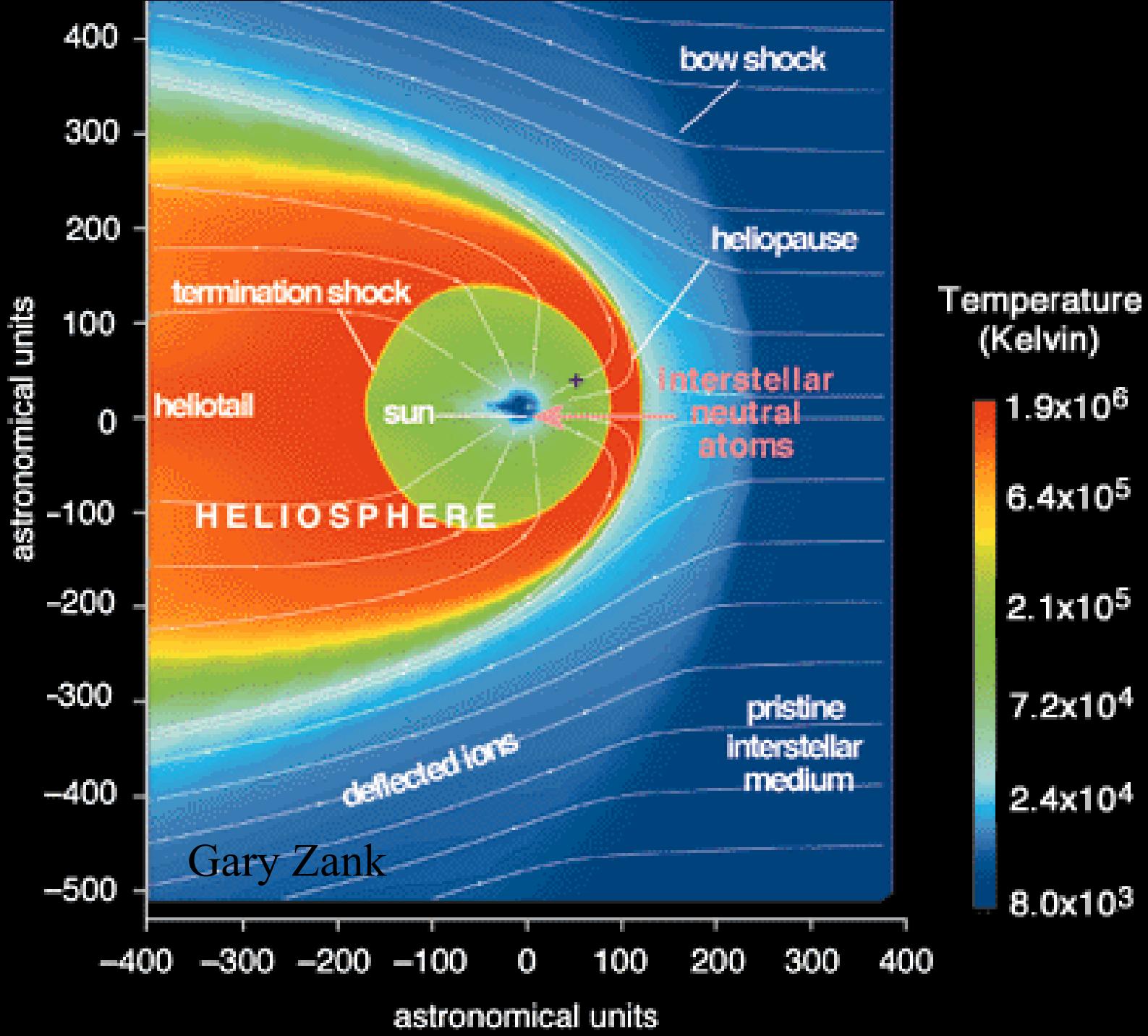


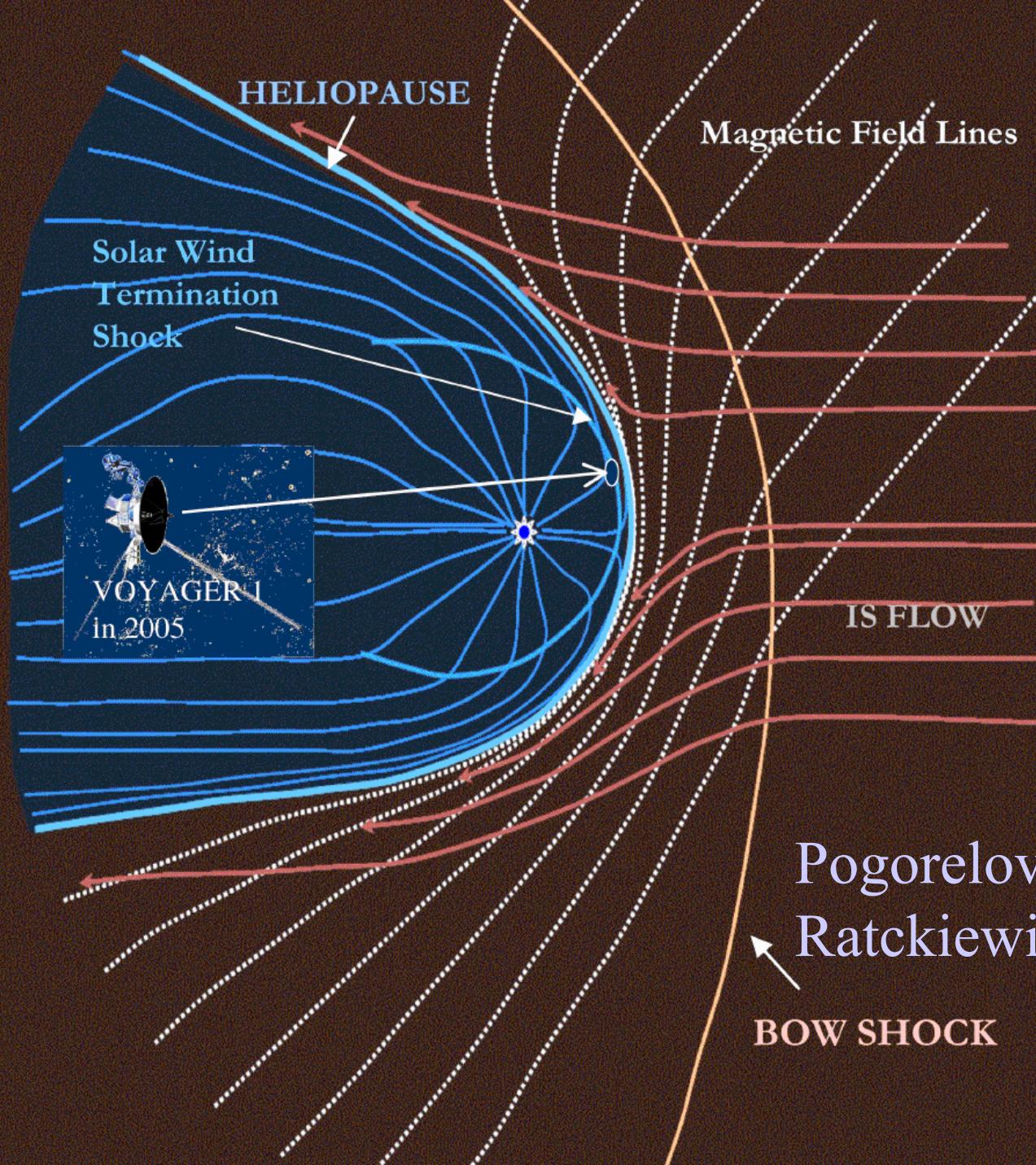


Possible extend, radius of Termination Shock  
based on the LISM magnetic field and desnity

# Hans-Reinhard Müller

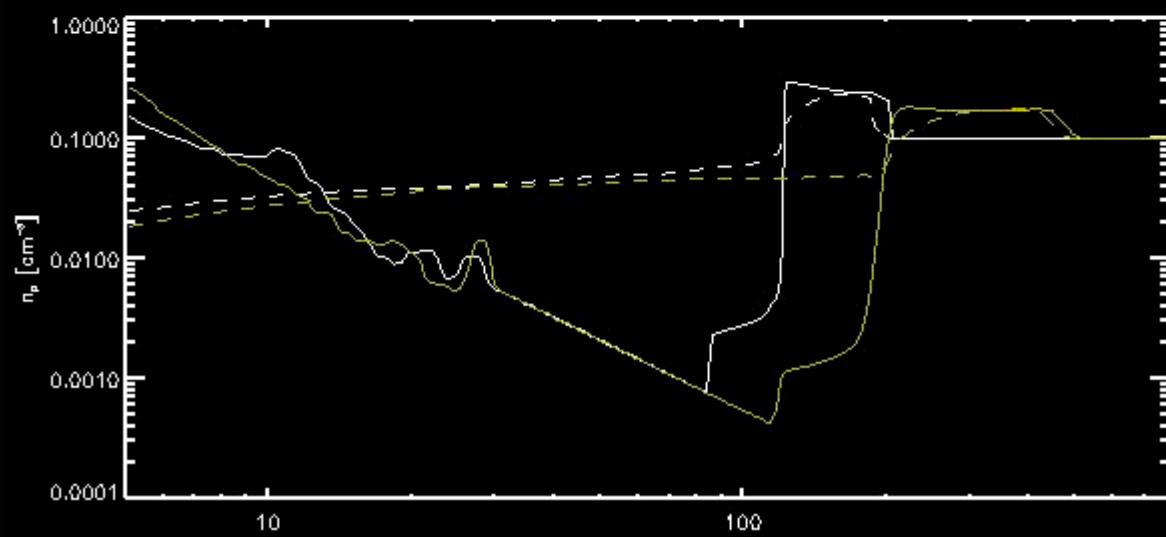
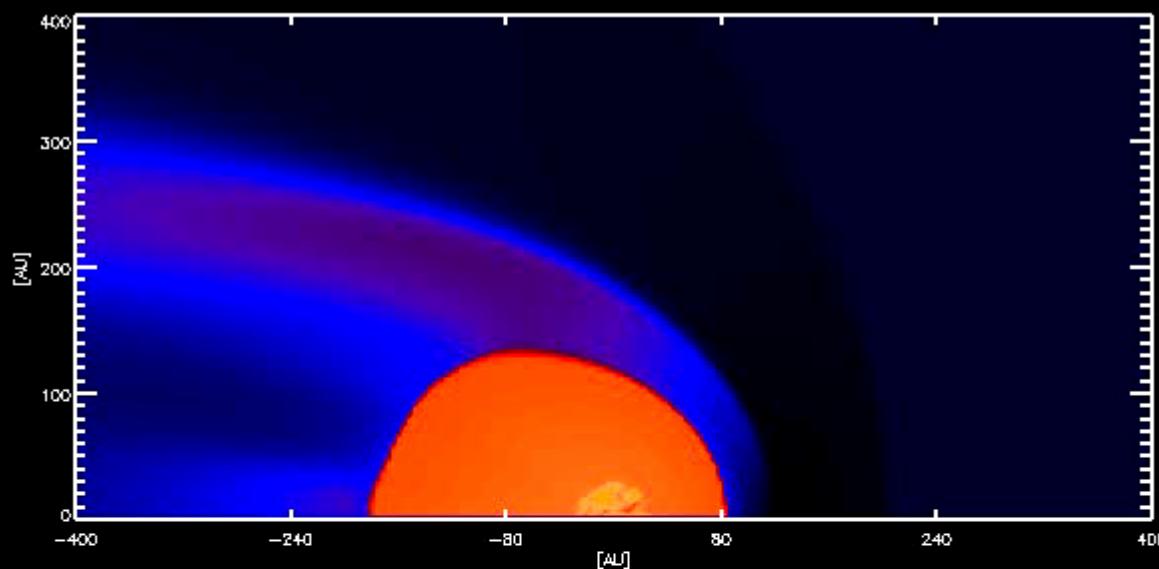


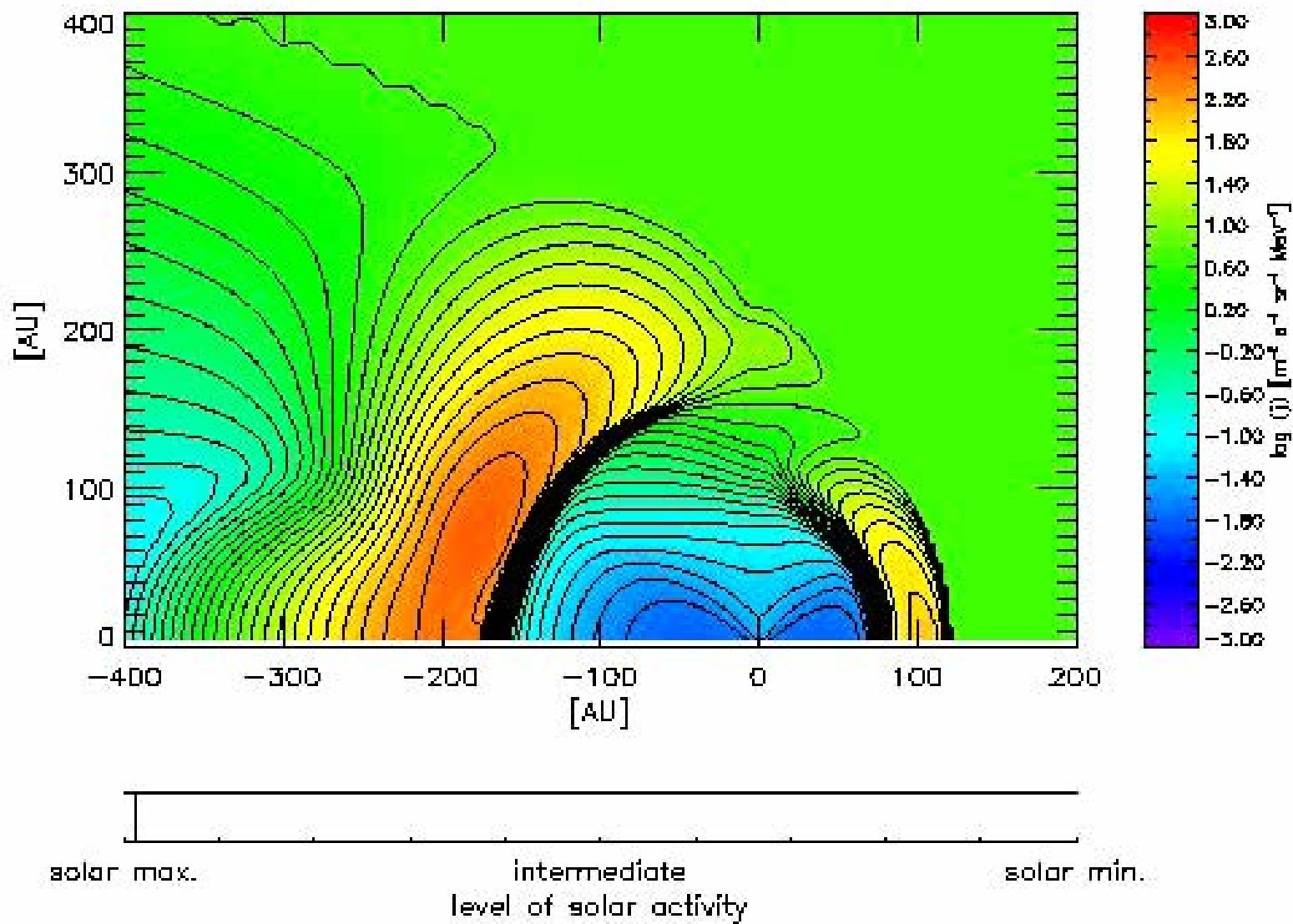




Pogorelov and Zank (2004),  
Ratckiewicz et al (2002)

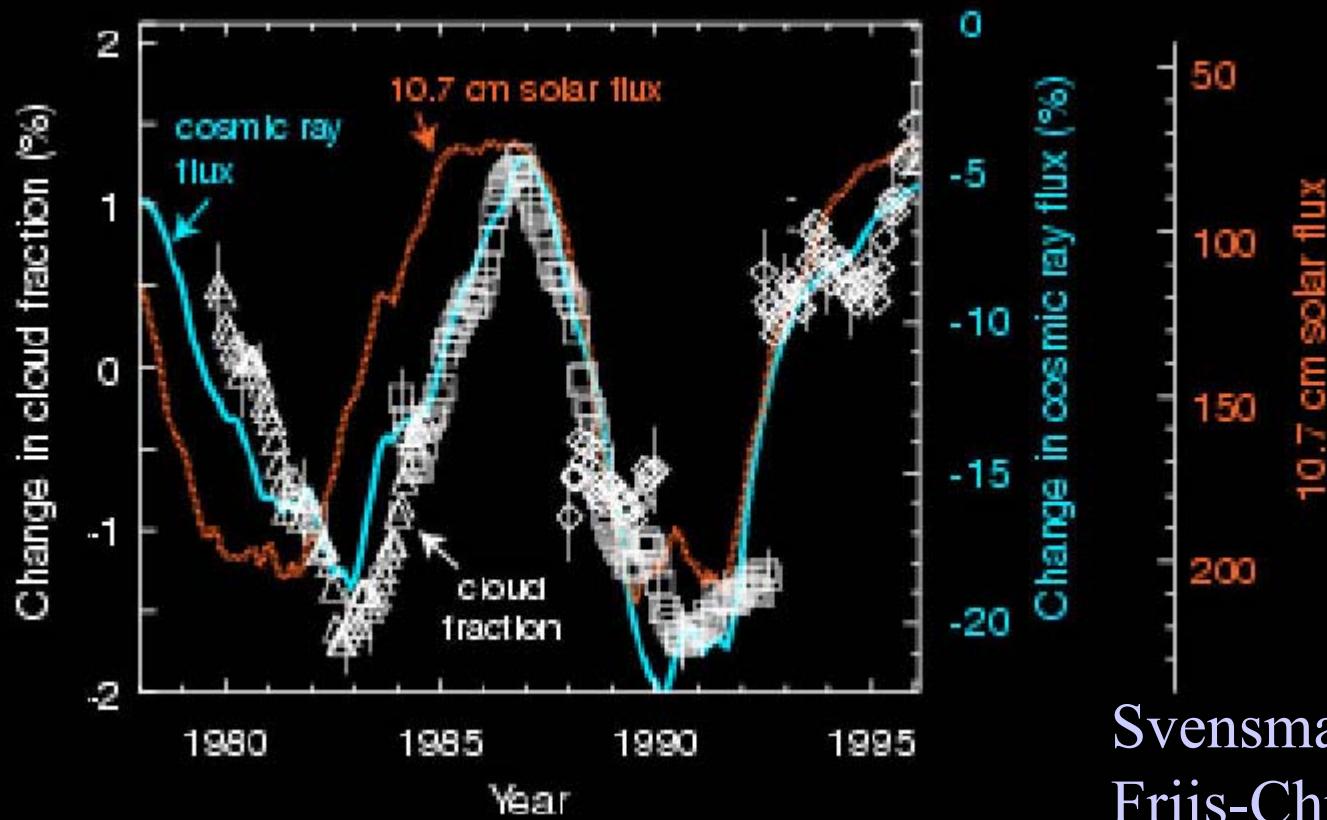
BOW SHOCK





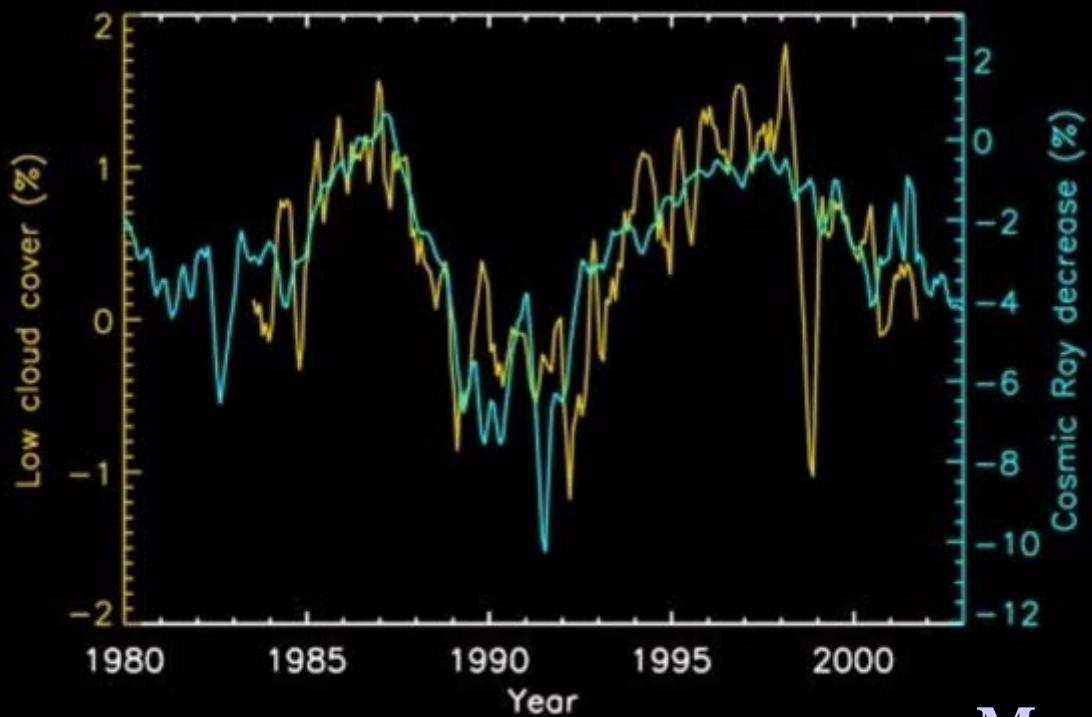


solar activity changes the heliosphere,  
the heliosphere modulates cosmic rays  
cosmic rays "seed" clouds and affect rainfall ?



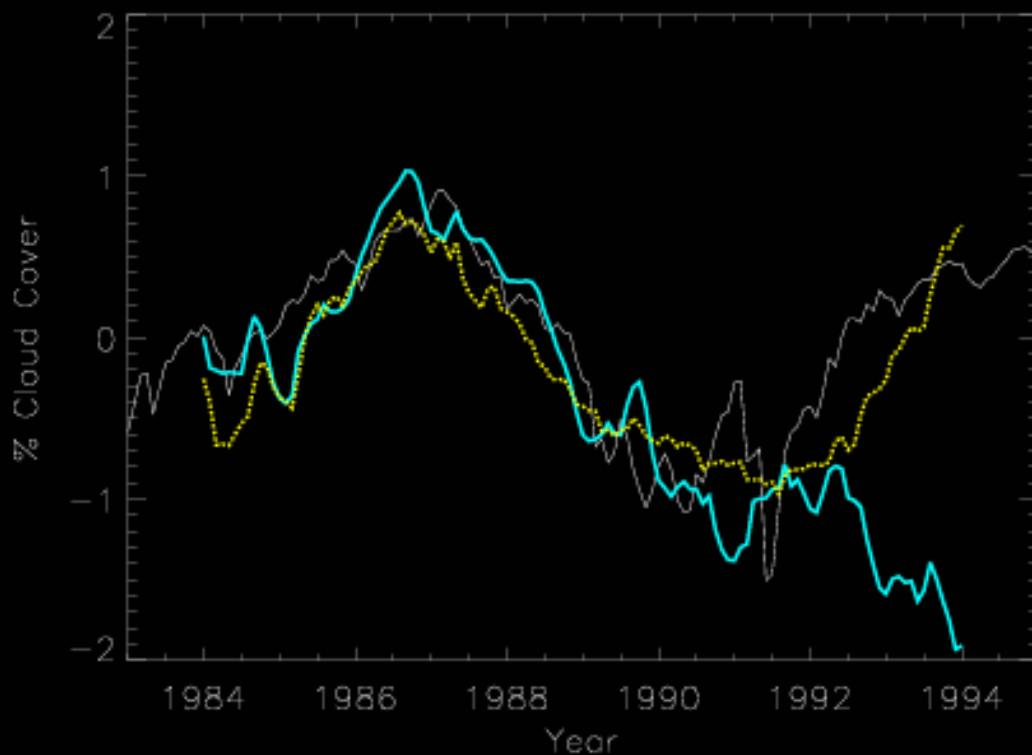
Svensmark and  
Friis-Christensen, 1997.

solar activity changes the heliosphere,  
the heliosphere modulates cosmic rays  
cosmic rays "seed" clouds and affect rainfall ?

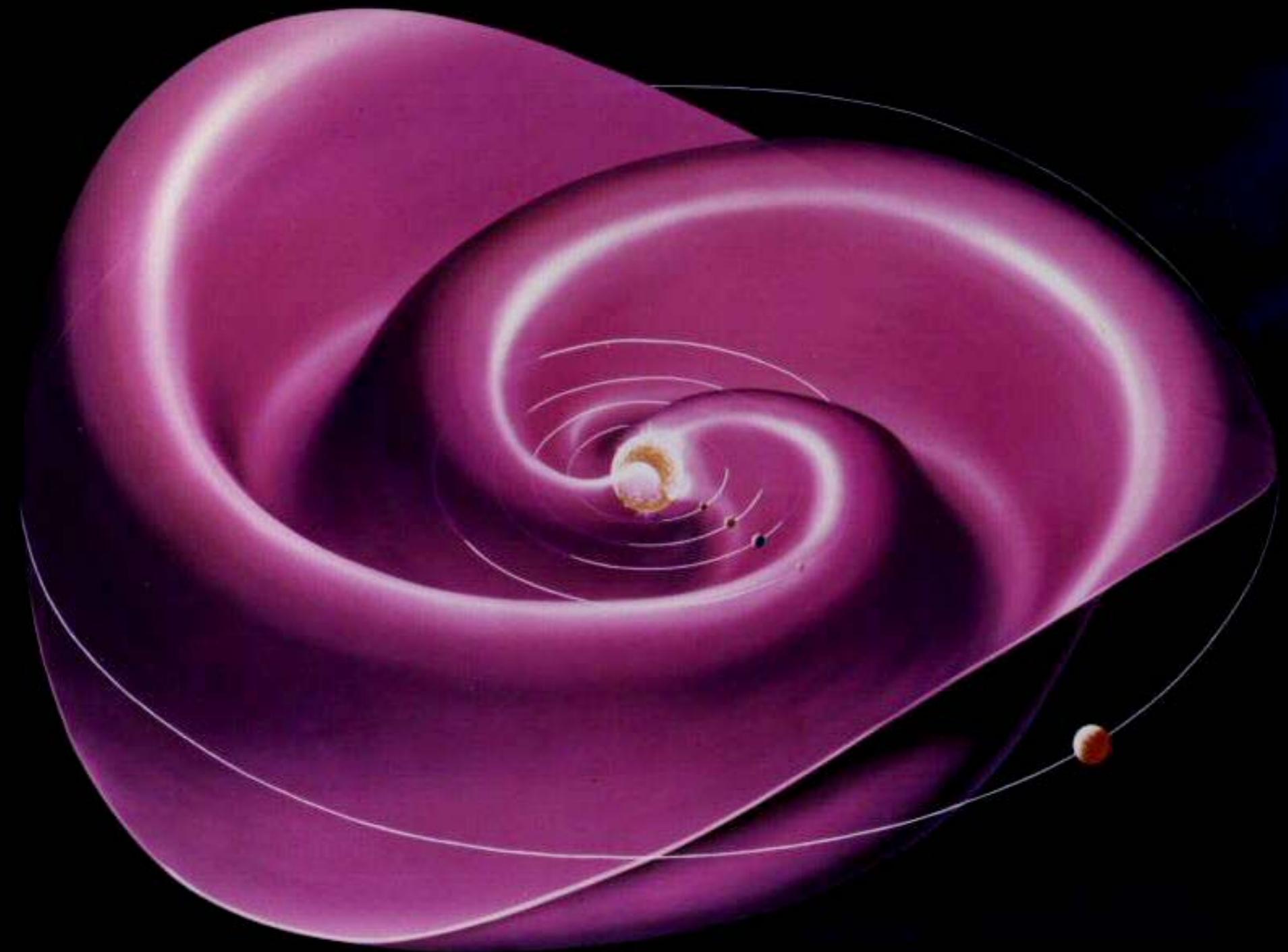


Marsh & Svensmark, 2000

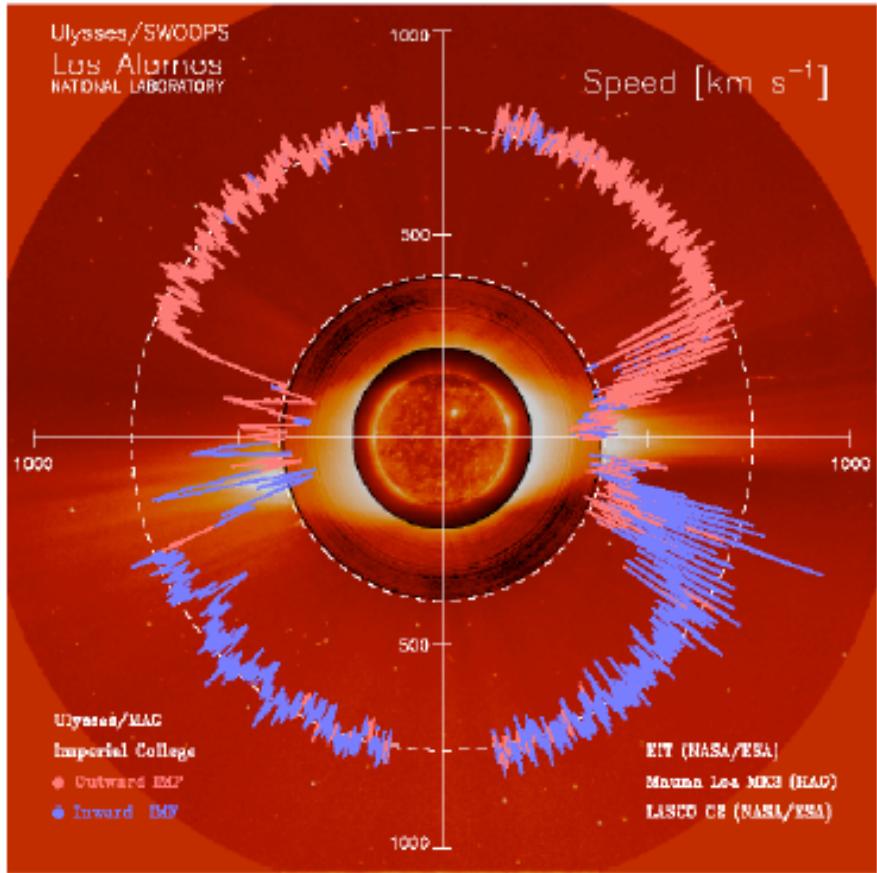
solar activity changes the heliosphere,  
the heliosphere modulates cosmic rays  
cosmic rays "seed" clouds and affect rainfall ?



**E. Palle Bago and C. J. Butler**  
*The influence of cosmic rays on  
terrestrial clouds and global  
warming*  
Astronomy & Geophysics, August  
2000, 41, 18-22.



## Orbit 1



## Orbit 2

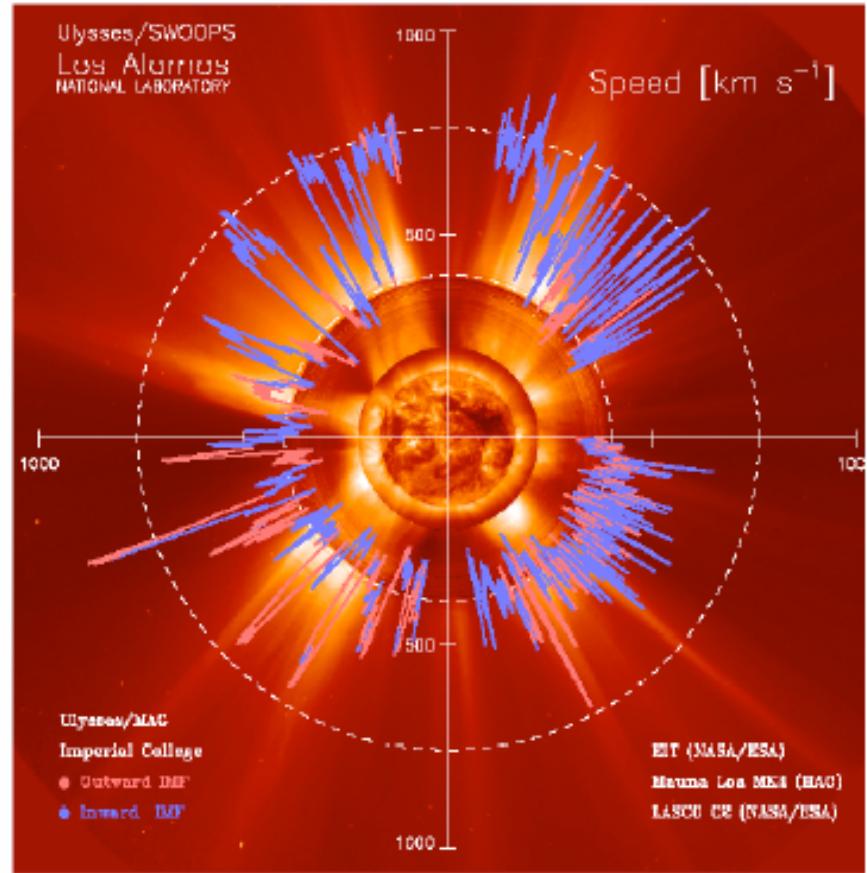
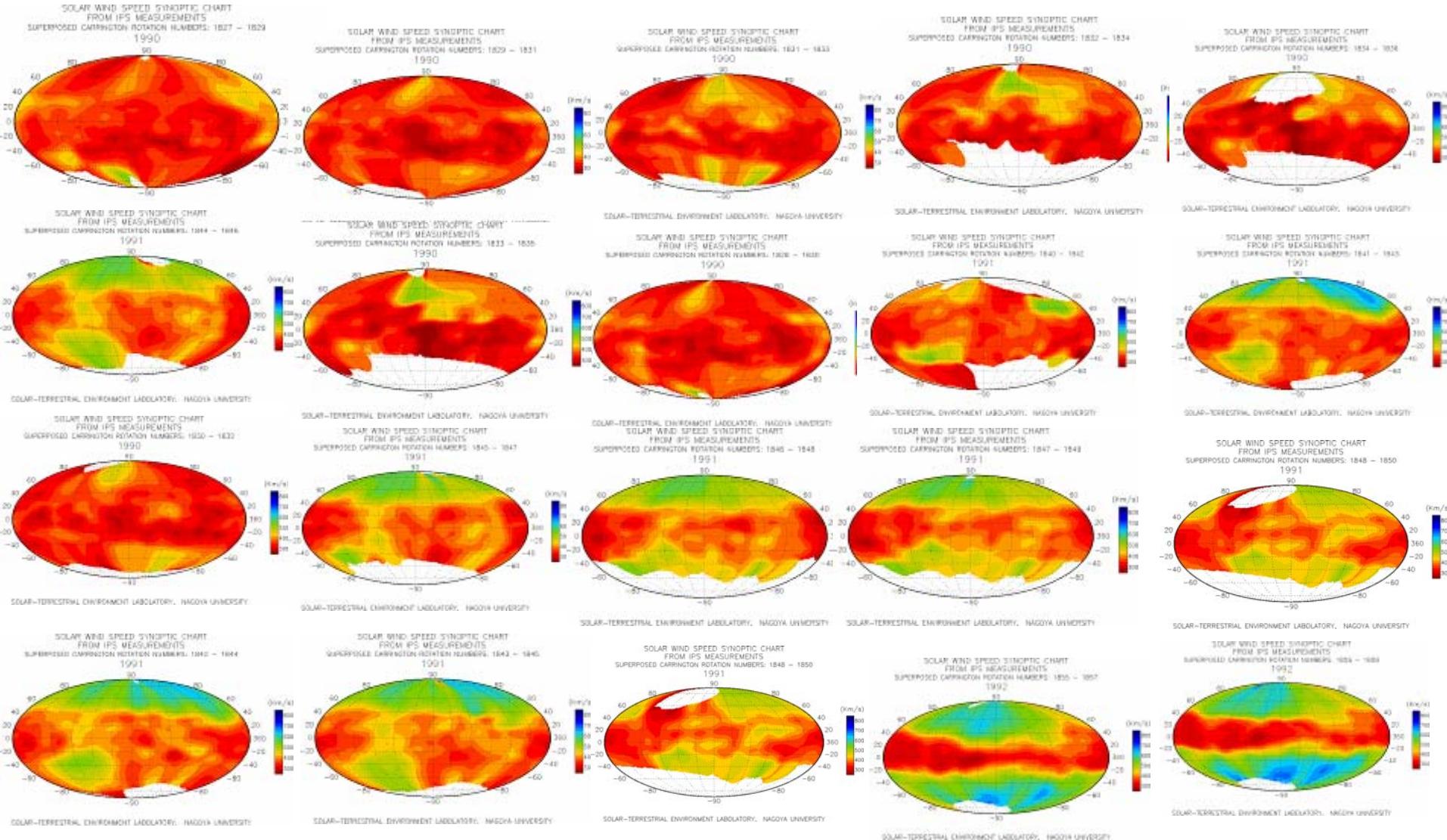
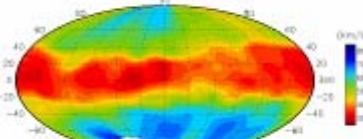


Figure 1.3. Dial plots of solar wind speed with co-temporal coronal images two years prior to solar minimum (Orbit 1) and at solar maximum (Orbit 2). Time runs clockwise from 3 o'clock, along with heliographic latitude. The solar wind speed scales are 500 km/s (1000 km/s) on the inner (outer) dashed circle. The 6.2 year orbits start in 1992 and 1998. The gaps at the north and south poles reflect the maximum Ulysses latitude of  $80.2^\circ$ . The final U-II data point is from December 2002.

# Solar wind velocity in 3D for several Carrington rotations near solar maximum (1990)

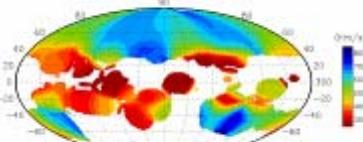


SOLAR WIND SPEED SYNTHETIC CHART  
FROM IPS MEASUREMENTS  
SUPERPOSED CARRINGTON ROTATION NUMBERS: 1857 - 1858  
1992



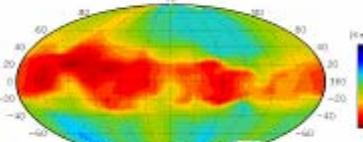
SOLAR-TERRESTRIAL ENVIRONMENT LABORATORY, NAGOYA UNIVERSITY

SOLAR WIND SPEED SYNTHETIC CHART  
FROM IPS MEASUREMENTS  
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1993



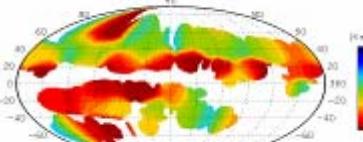
SOLAR-TERRESTRIAL ENVIRONMENT LABORATORY, NAGOYA UNIVERSITY

SOLAR WIND SPEED SYNTHETIC CHART  
FROM IPS MEASUREMENTS  
SUPERPOSED CARRINGTON ROTATION NUMBERS: 1870 - 1872  
1993



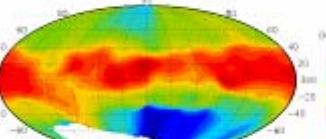
SOLAR-TERRESTRIAL ENVIRONMENT LABORATORY, NAGOYA UNIVERSITY

SOLAR WIND SPEED SYNTHETIC CHART  
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1994



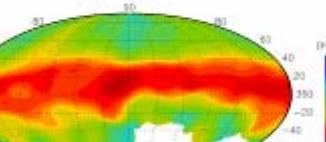
SOLAR-TERRESTRIAL ENVIRONMENT LABORATORY, NAGOYA UNIVERSITY

SOLAR WIND SPEED SYNTHETIC CHART  
FROM IPS MEASUREMENTS  
SUPERPOSED CARRINGTON ROTATION NUMBERS: 1858 - 1860  
1992

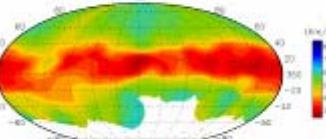


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SOLAR WIND SPEED SYNTHETIC CHART  
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1992

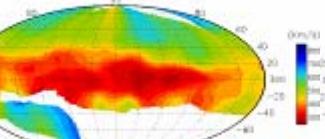


SOLAR WIND SPEED SYNTHETIC CHART  
FROM IPS MEASUREMENTS  
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1992



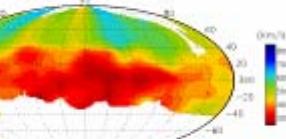
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SOLAR WIND SPEED SYNTHETIC CHART  
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1993



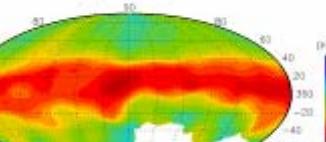
SOLAR-TERRESTRIAL ENVIRONMENT LABORATORY, NAGOYA UNIVERSITY

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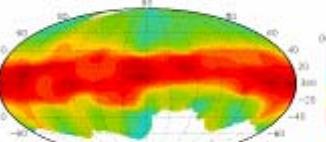


SOLAR-TERRESTRIAL ENVIRONMENT LABORATORY, NAGOYA UNIVERSITY

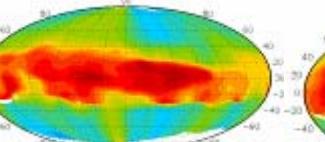
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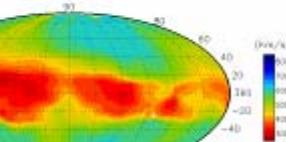
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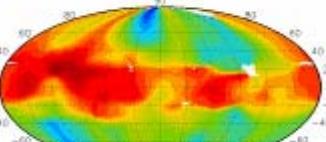
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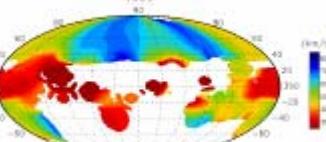
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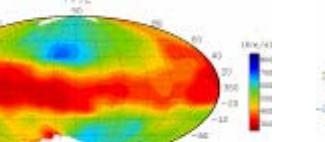
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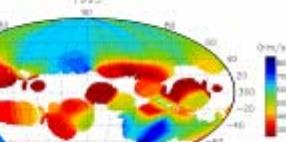
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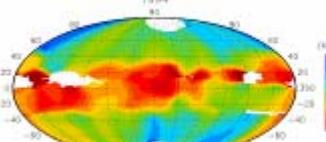
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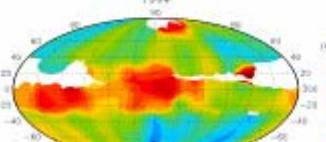
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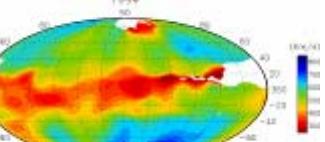
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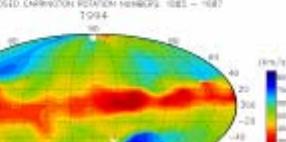
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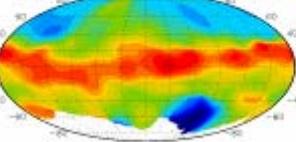
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SOLAR WIND SPEED SYNTHETIC CHART  
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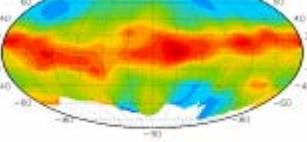


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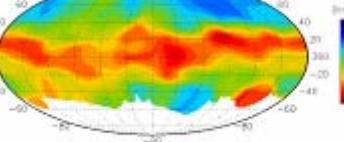
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SOLAR WIND SPEED SYNTHETIC CHART  
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1994



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SOLAR WIND SPEED SYNTHETIC CHART  
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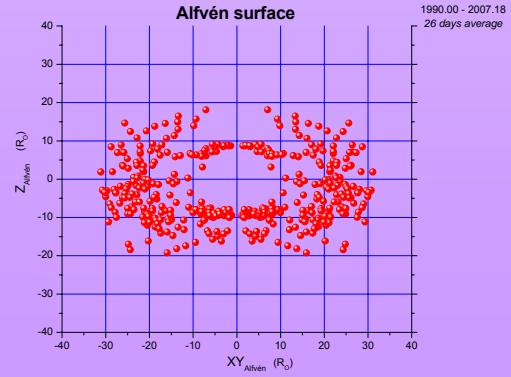
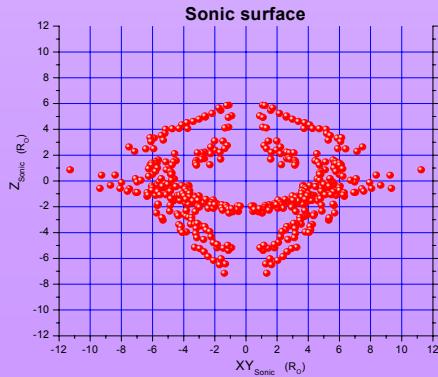


SOLAR-TERRESTRIAL ENVIRONMENT LABORATORY, NAGOYA UNIVERSITY

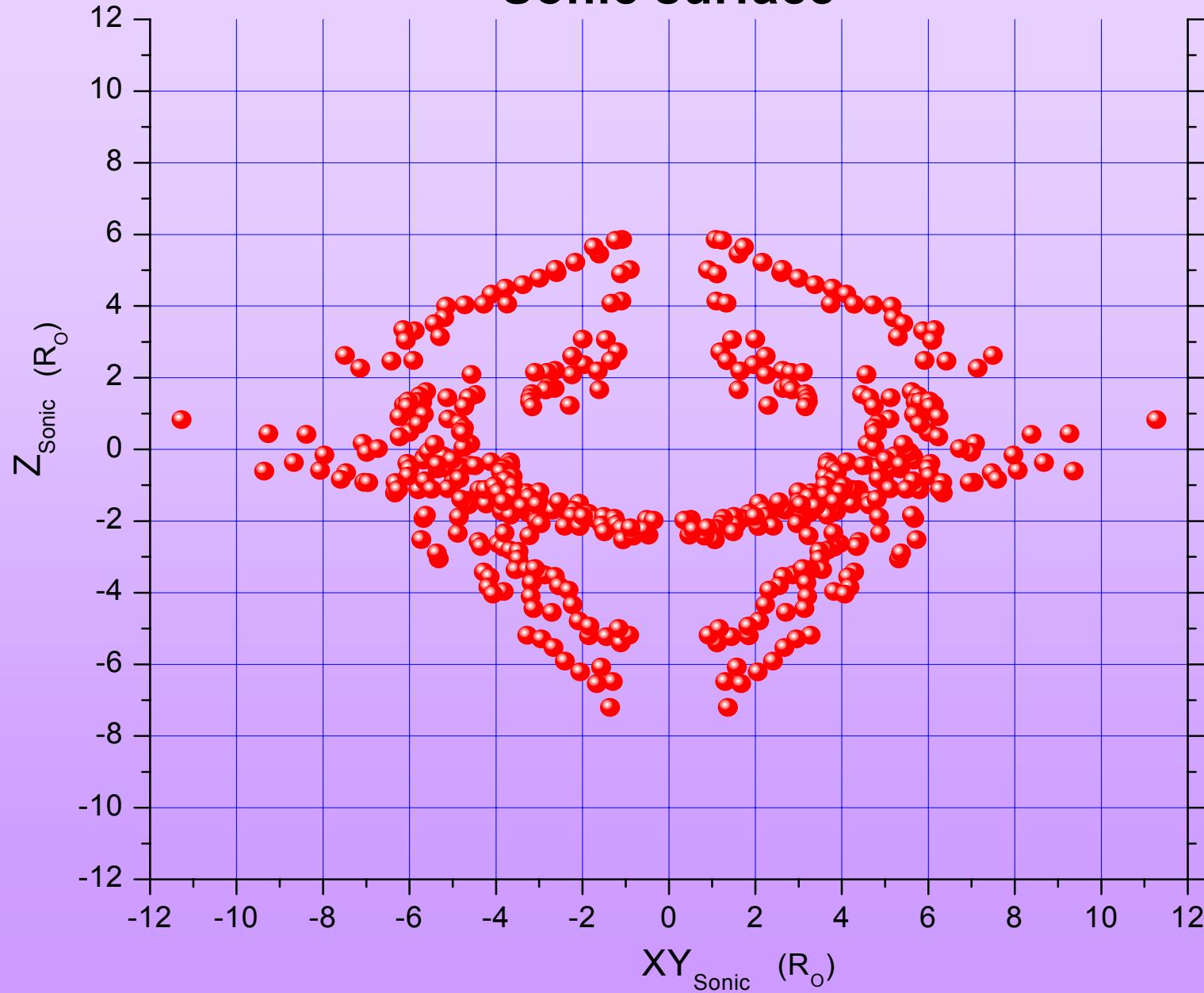
1994 near  
solar minimum

# Study of the solar Slow Sonic, Alfvén and Fast Magnetosonic transition surfaces, using data from Ulysses and spacecrafts at 1AU (OMNI)

Valadis Katsikas, George Exarhos

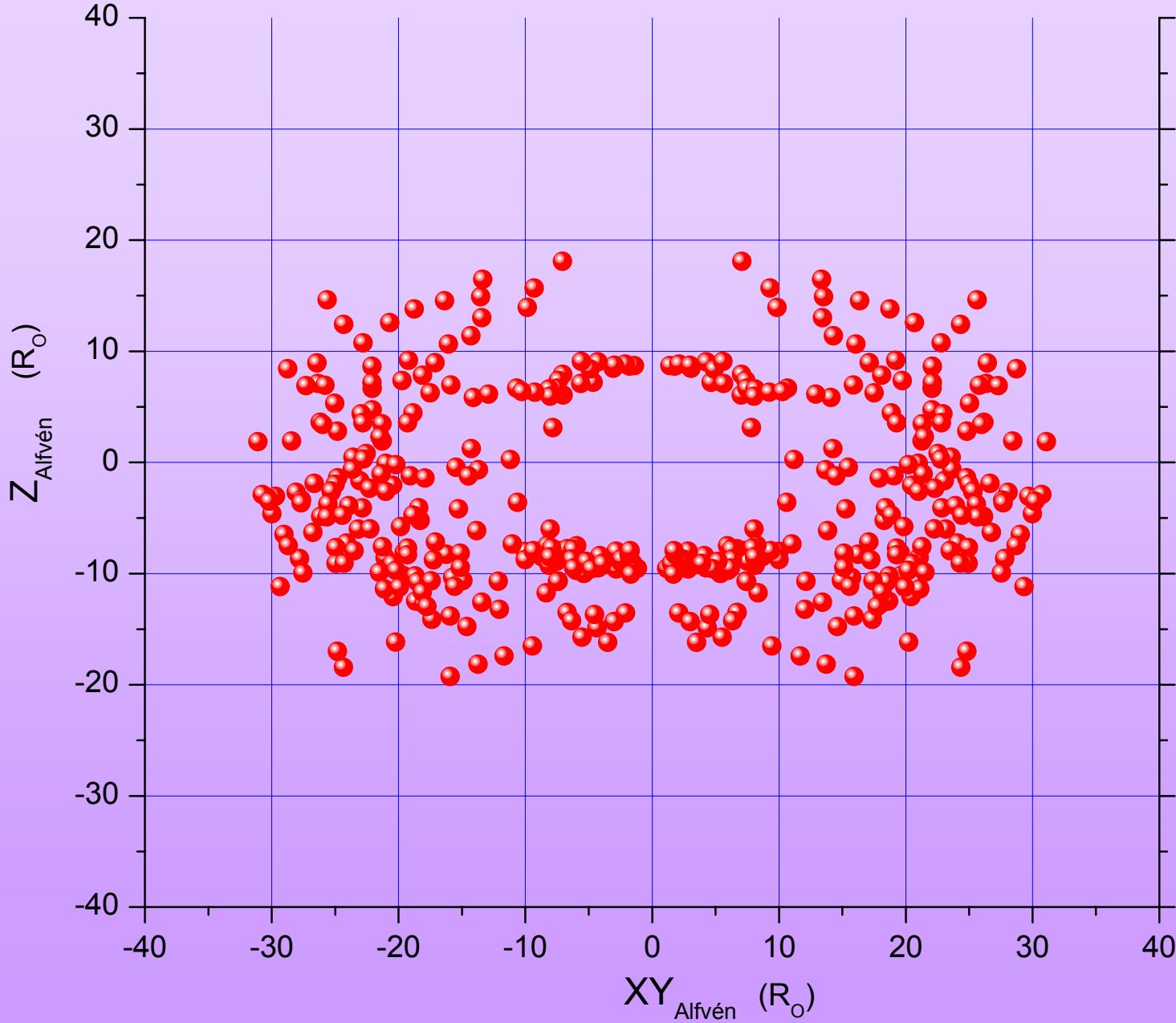


# Sonic surface

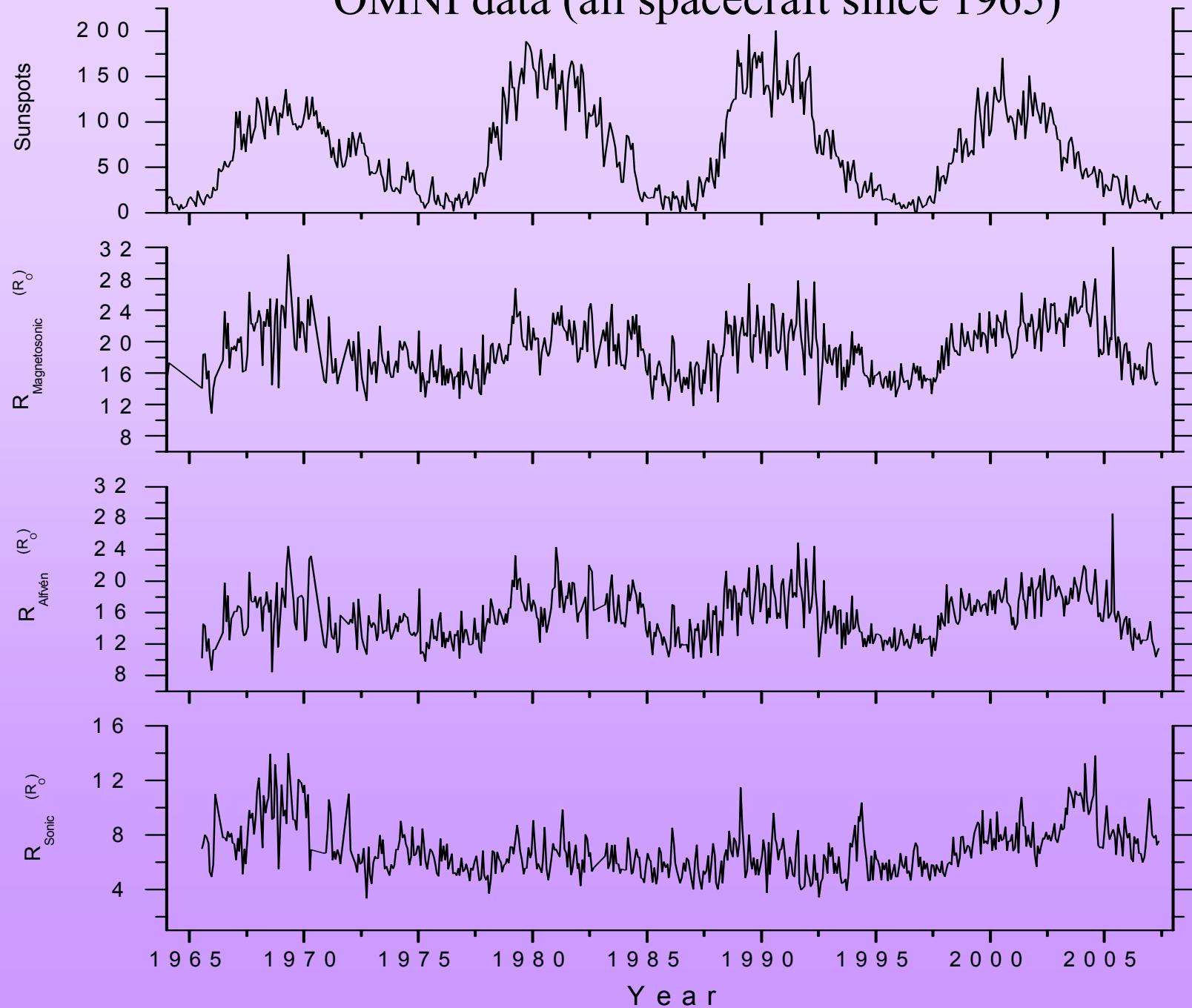


# Alfvén surface

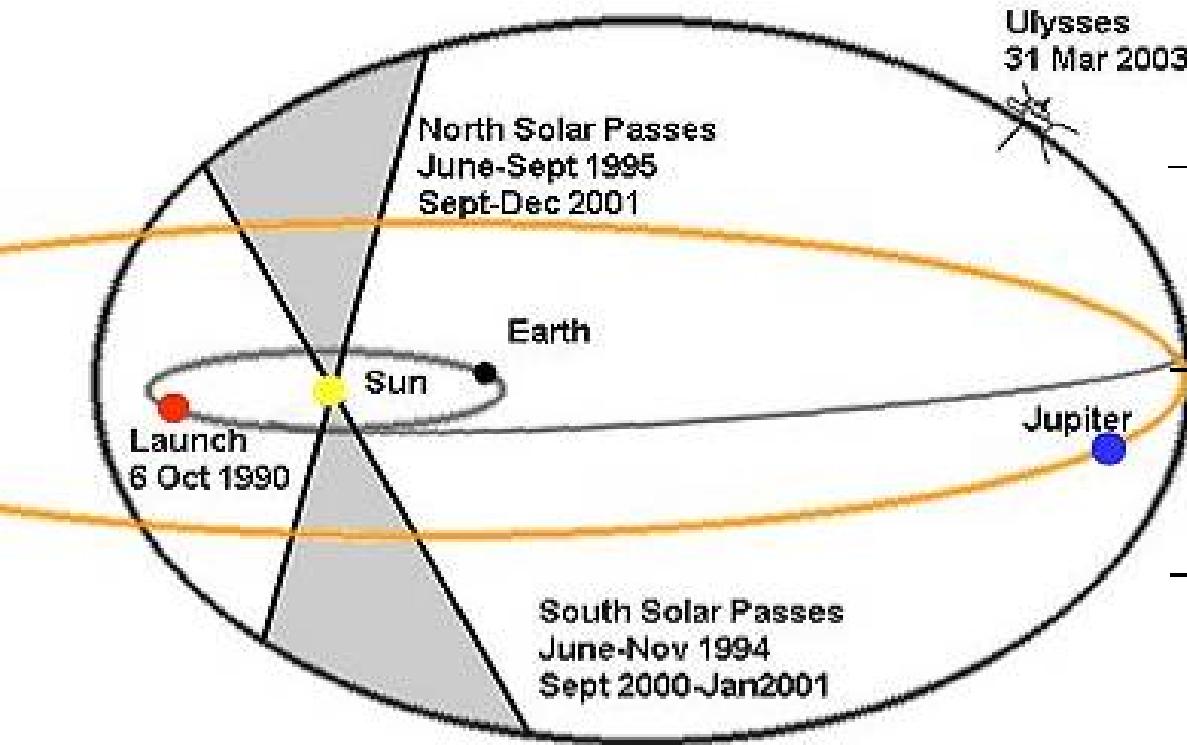
1990.00 - 2007.18  
26 days average



# OMNI data (all spacecraft since 1965)

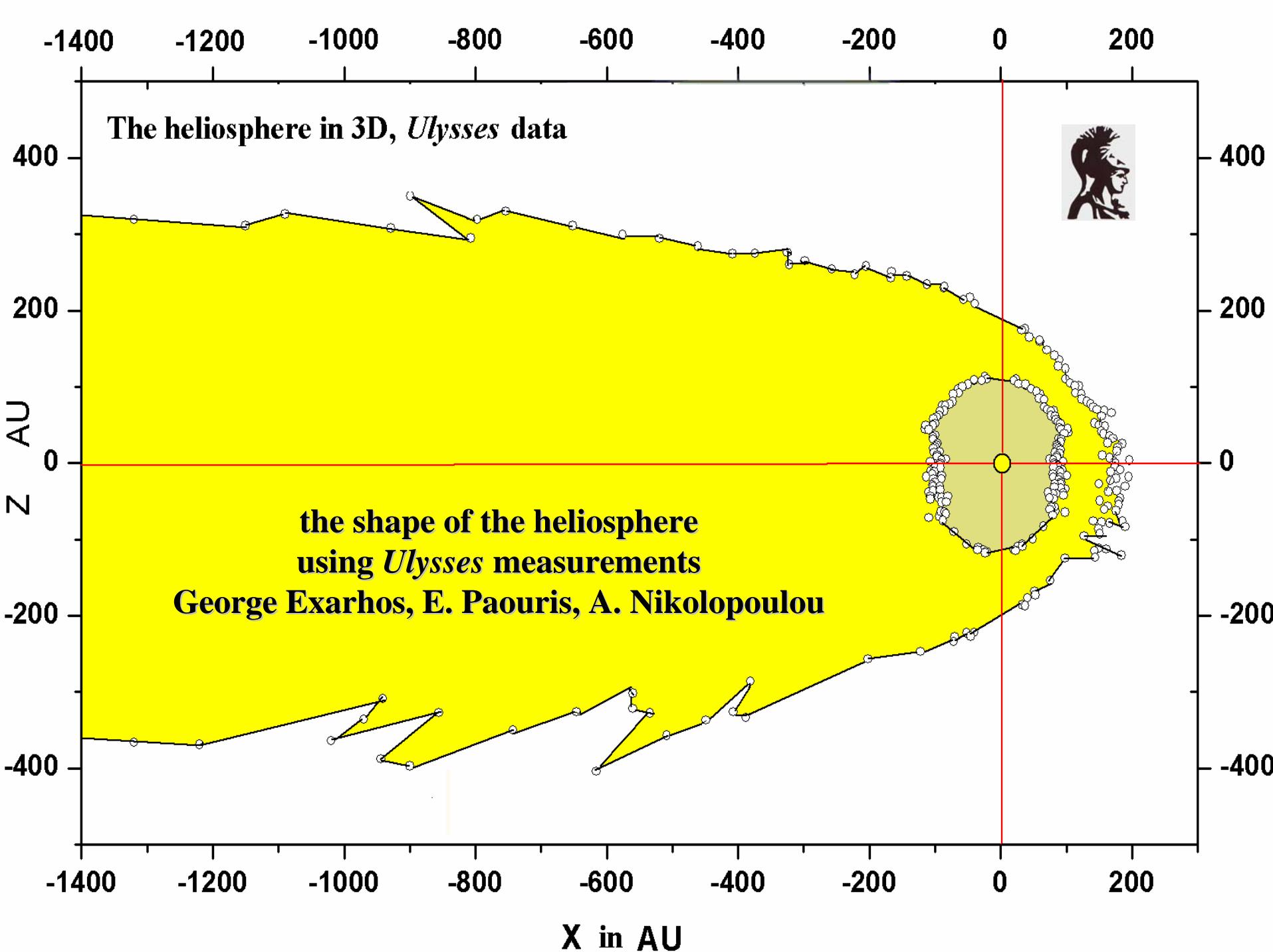


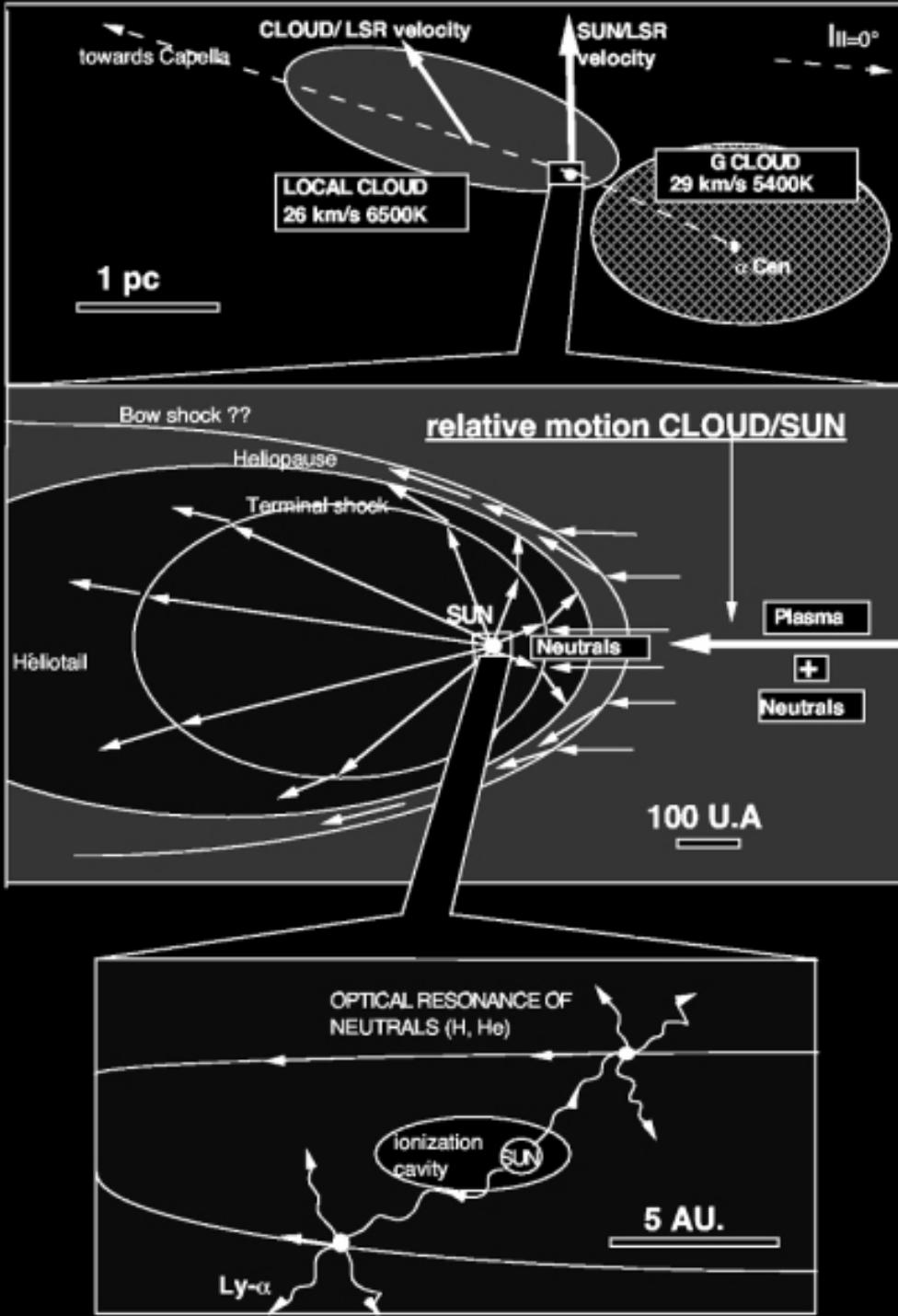
# Ulysses mission



## Orbit:

- It is the first time that a mission study the heliosphere in 3D observing the interplanetary medium off the ecliptic,**
- above the poles of the Sun.**





## Deflection of the Interstellar Medium

Lallemand, R., et al., Science, 307, 1449, 2005

Doppler shifts of the interstellar hydrogen resonance glow to show the direction of the neutral hydrogen flow as it enters the inner heliosphere.

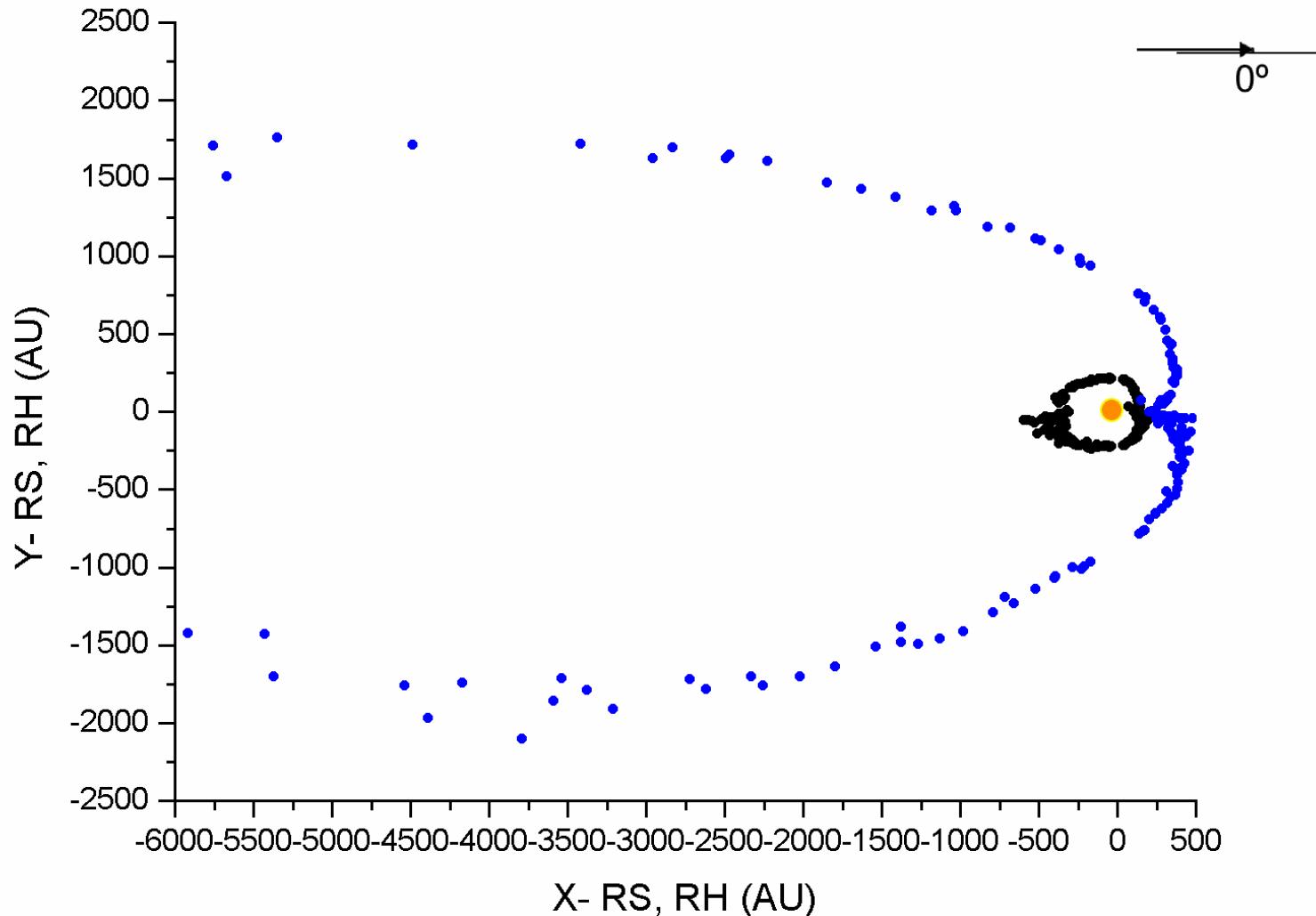
The neutral hydrogen flow is found to be deflected relative to the helium flow by 4 degrees. Due to the direction of the interstellar magnetic field. In this case, the helium flow vector and the hydrogen flow vector constrain the direction of the magnetic field and act as an interstellar magnetic compass.

# the shape of the heliosphere and the interstellar magnetic field orientation

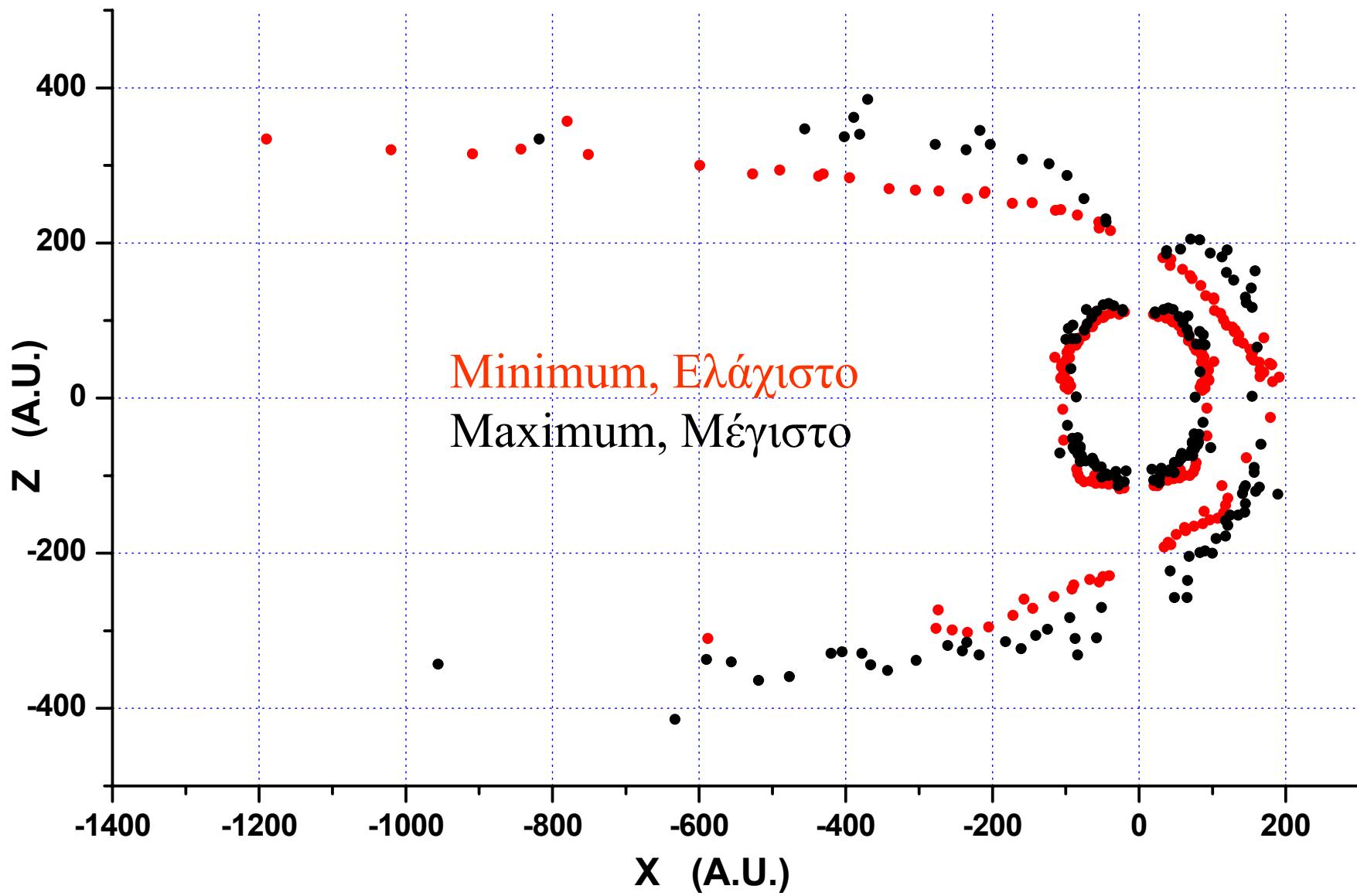
Angeliki Nikolopoulou, 2000



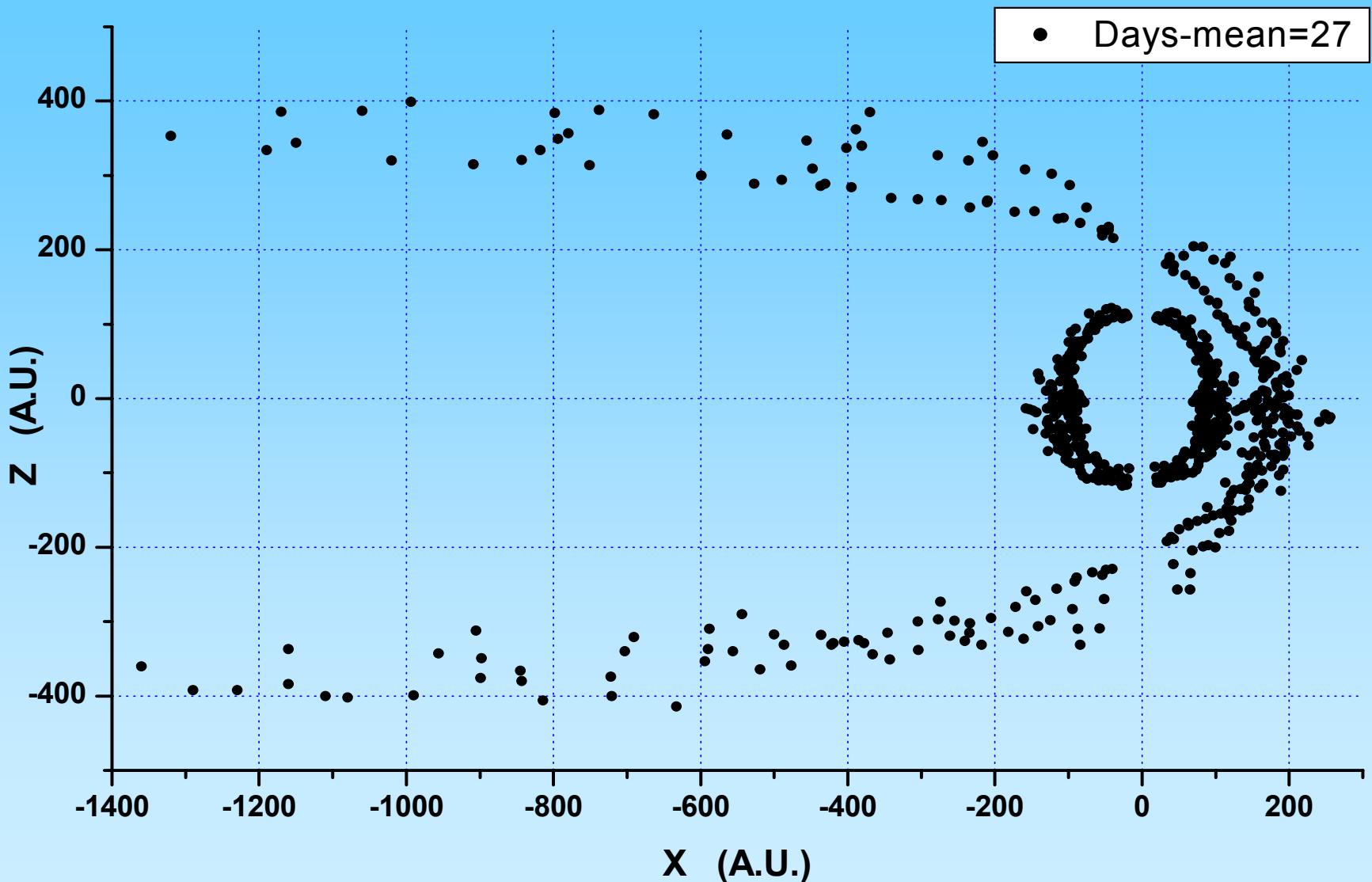
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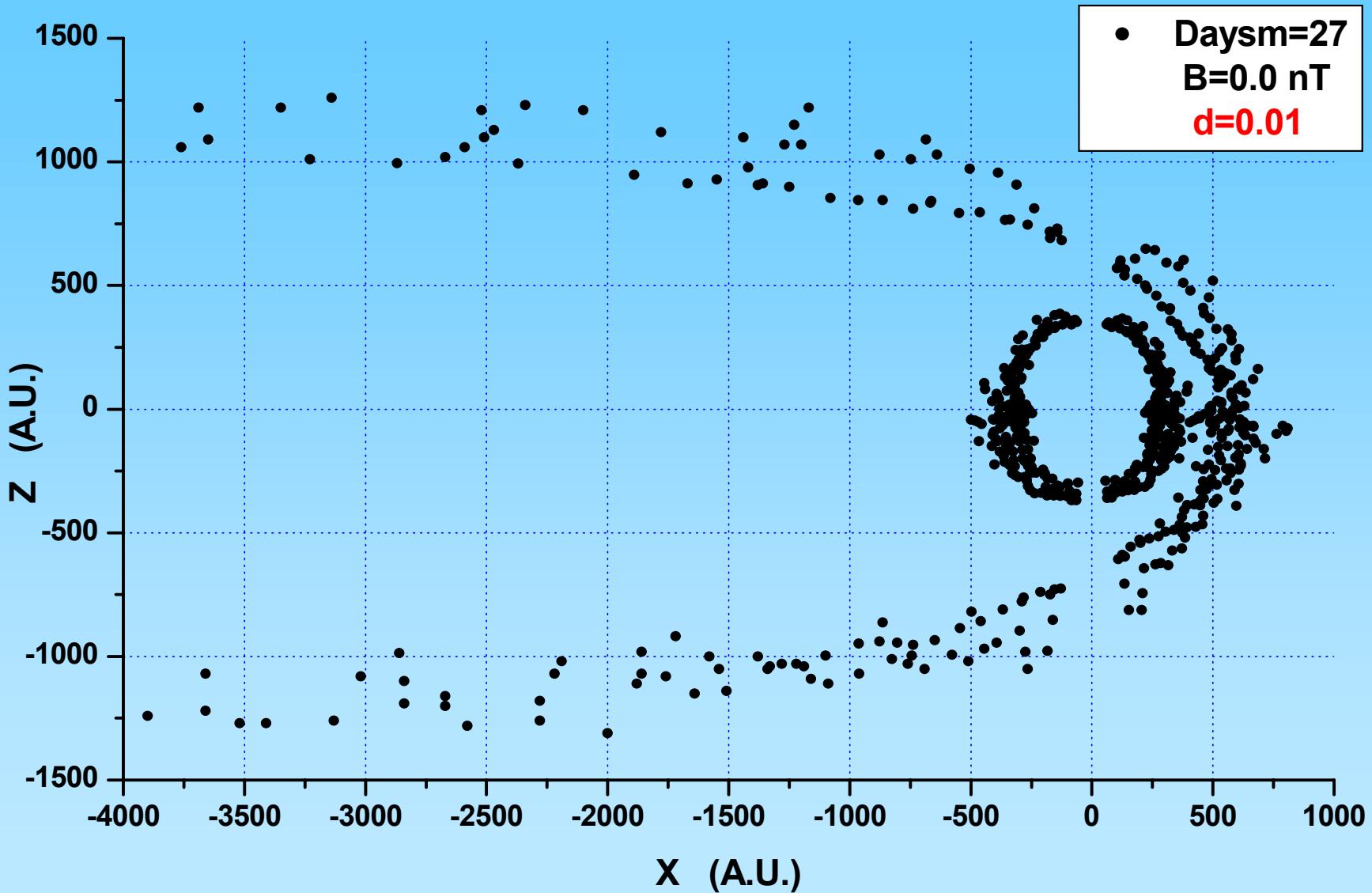


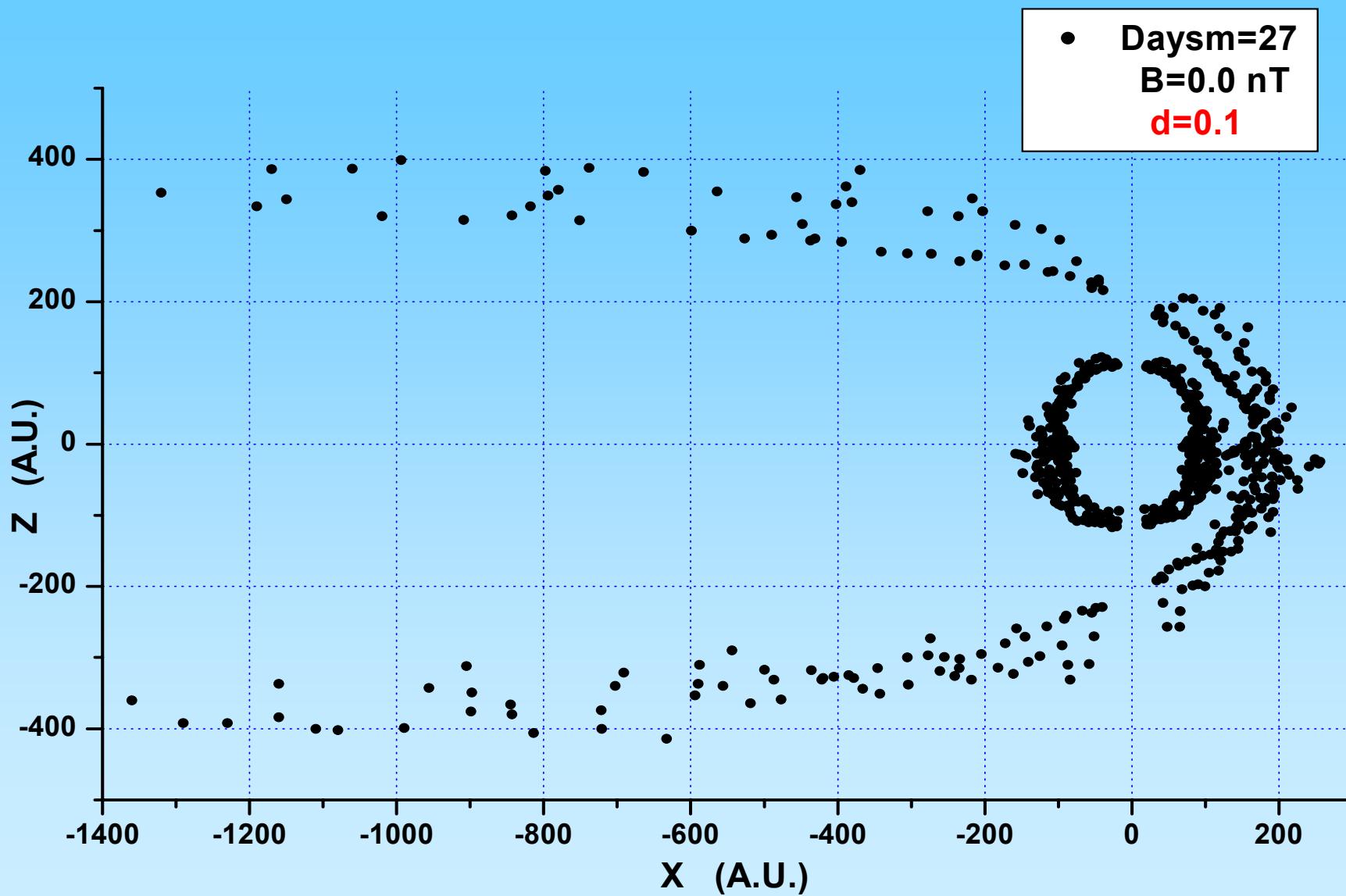
# the shape of the heliosphere using *Ulysses* measurements

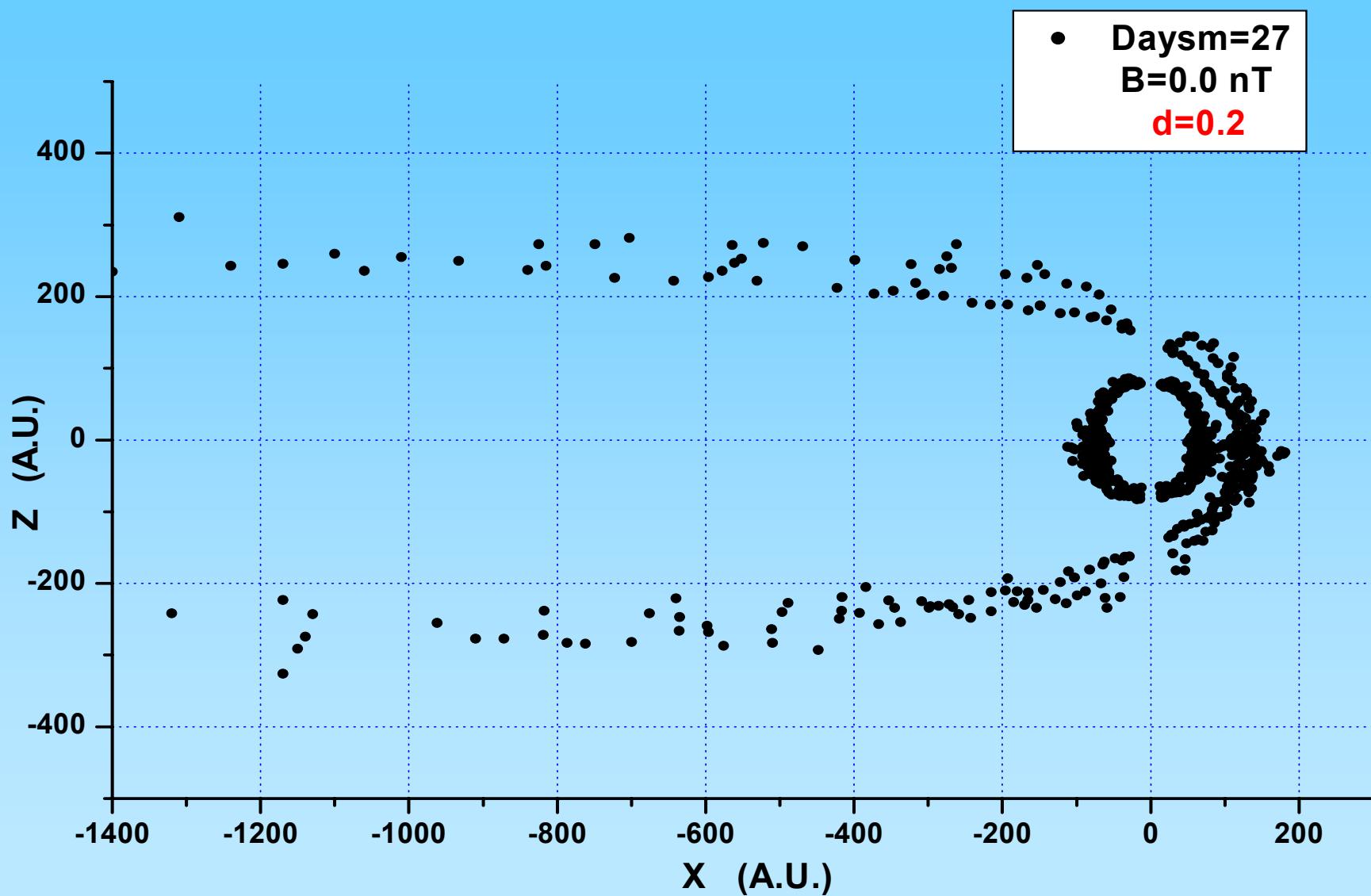


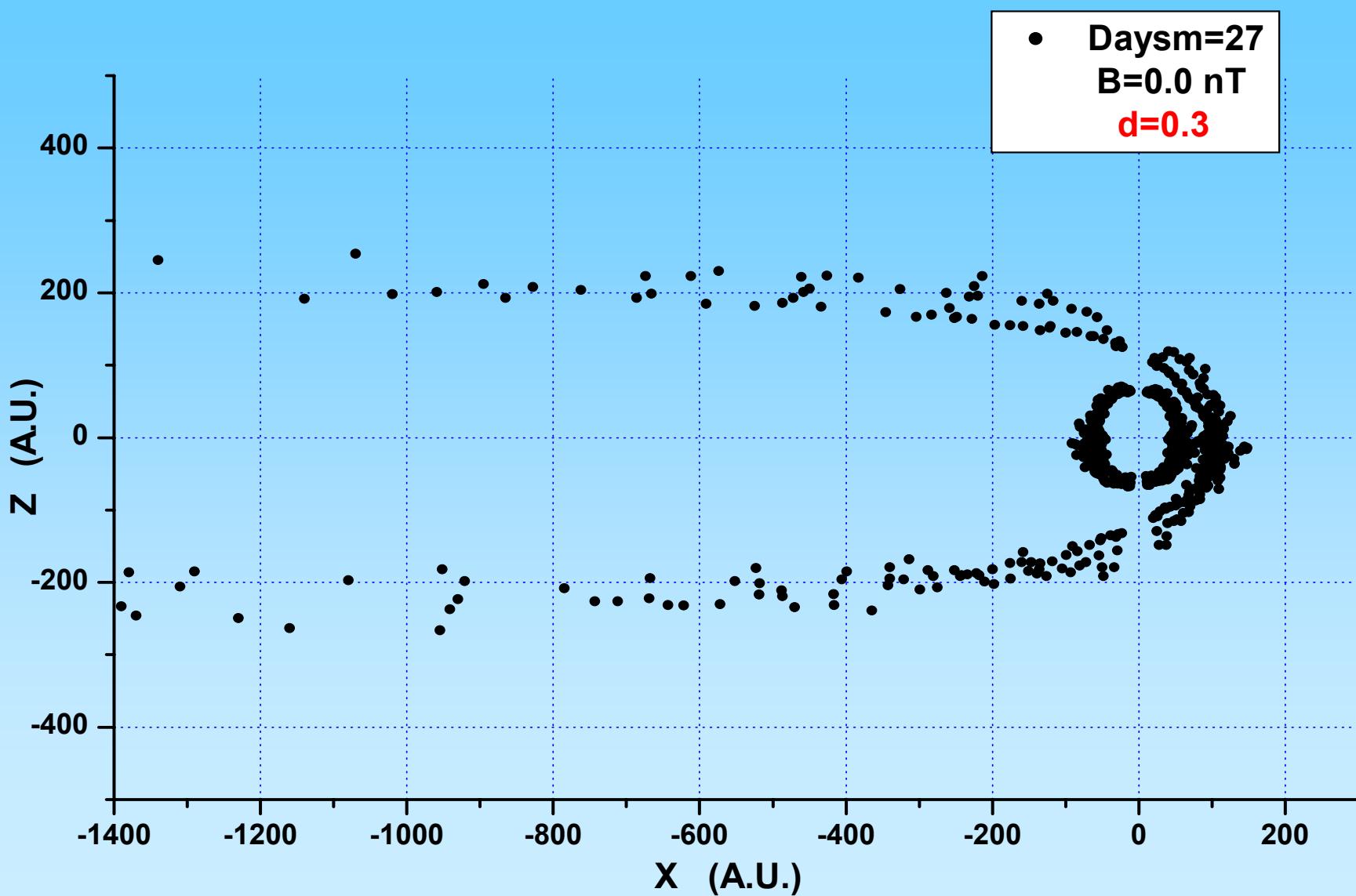
# the shape of the heliosphere using *Ulysses* measurements

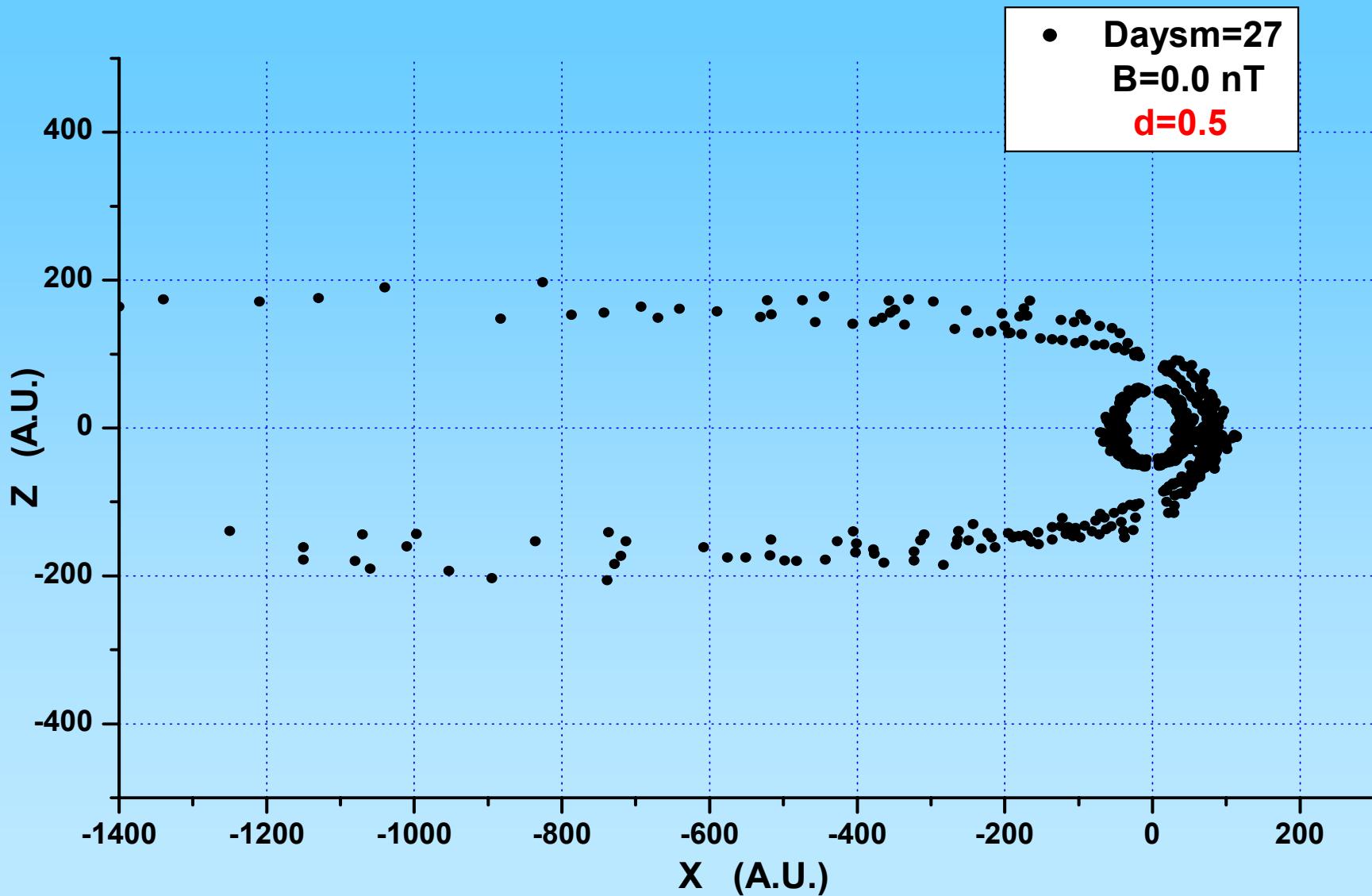






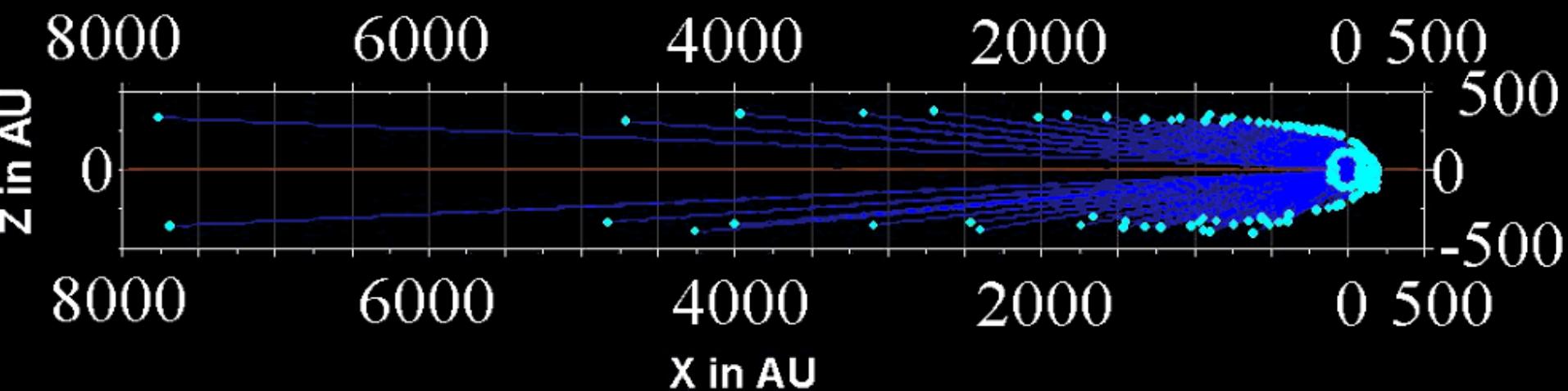


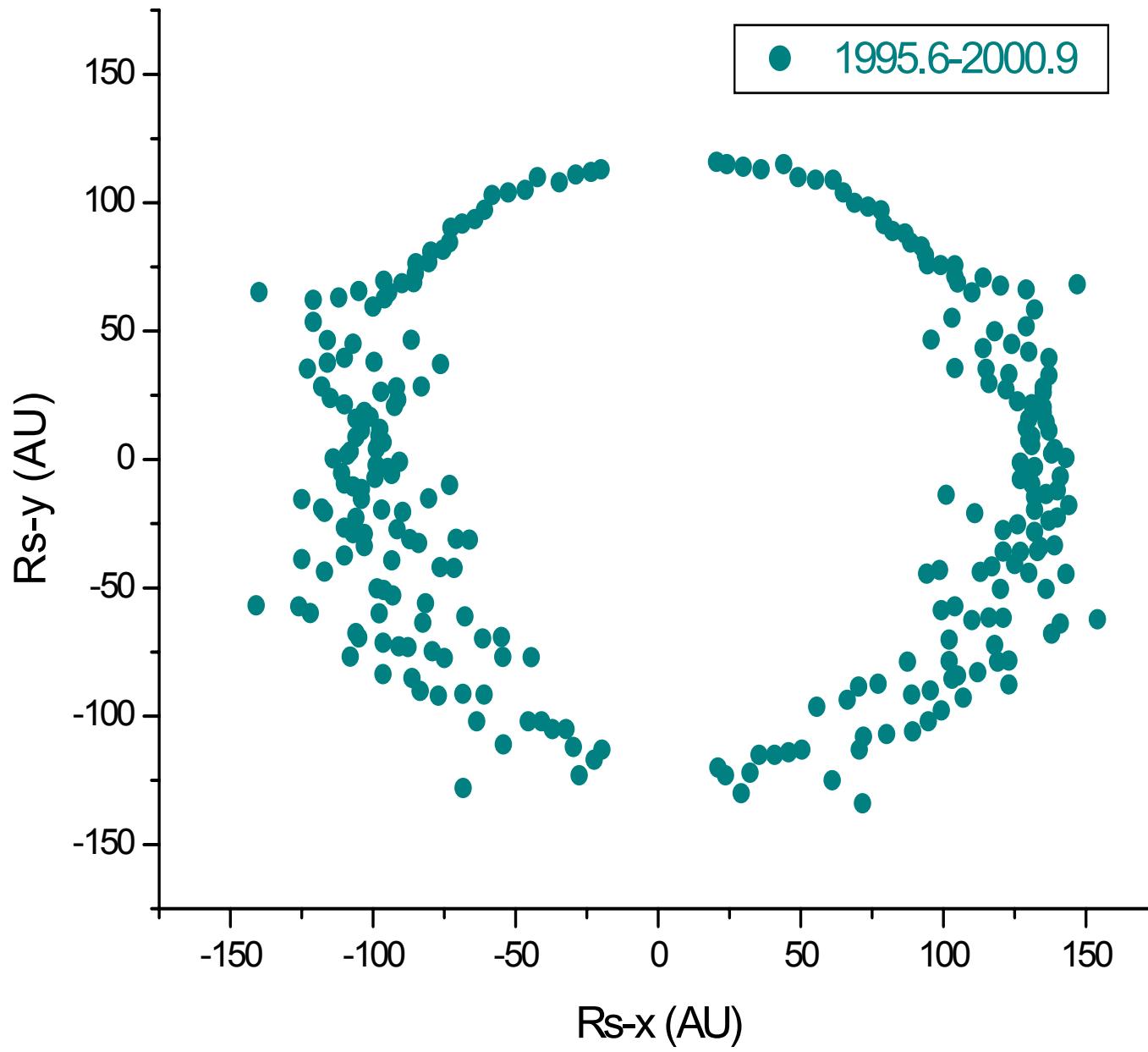


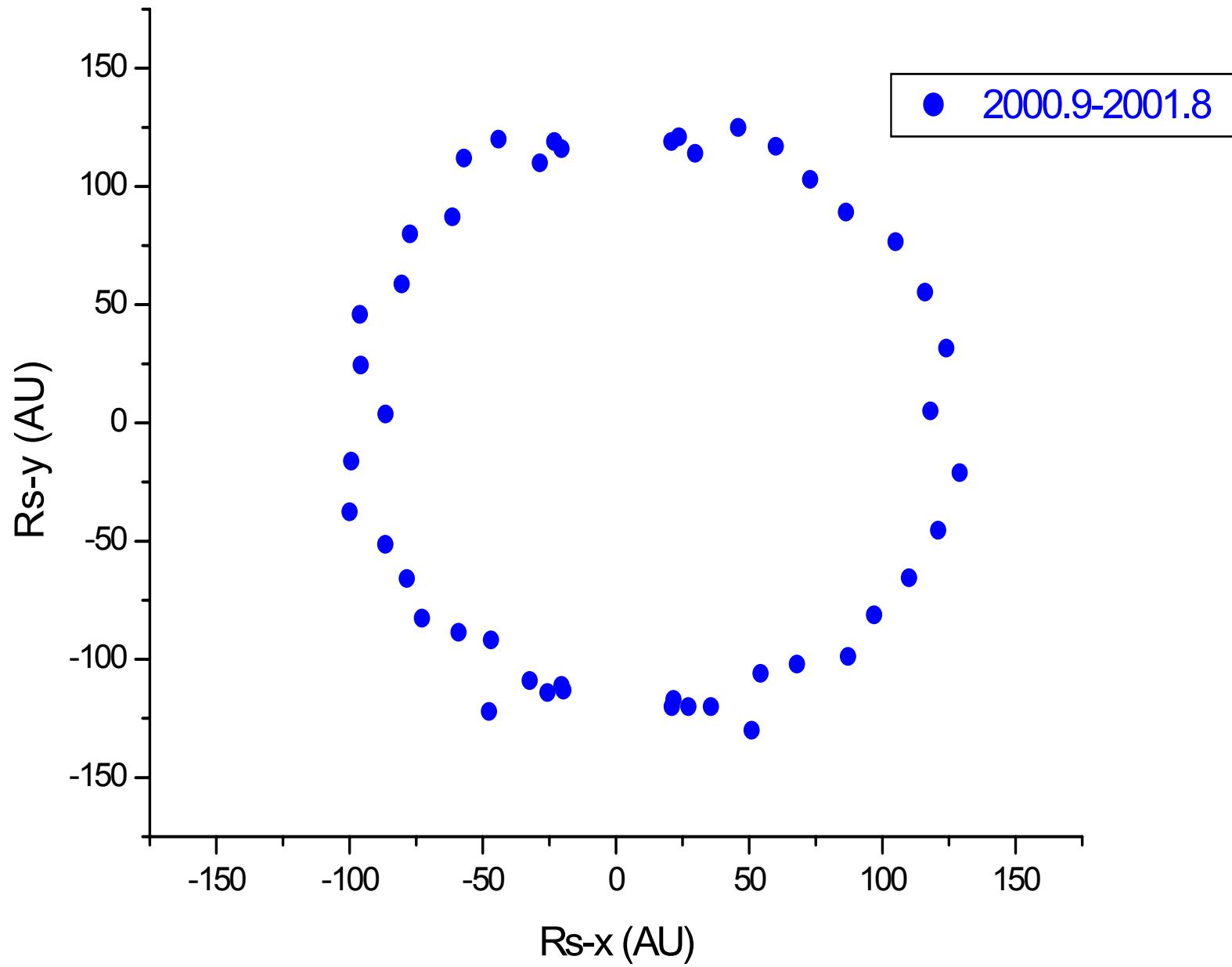


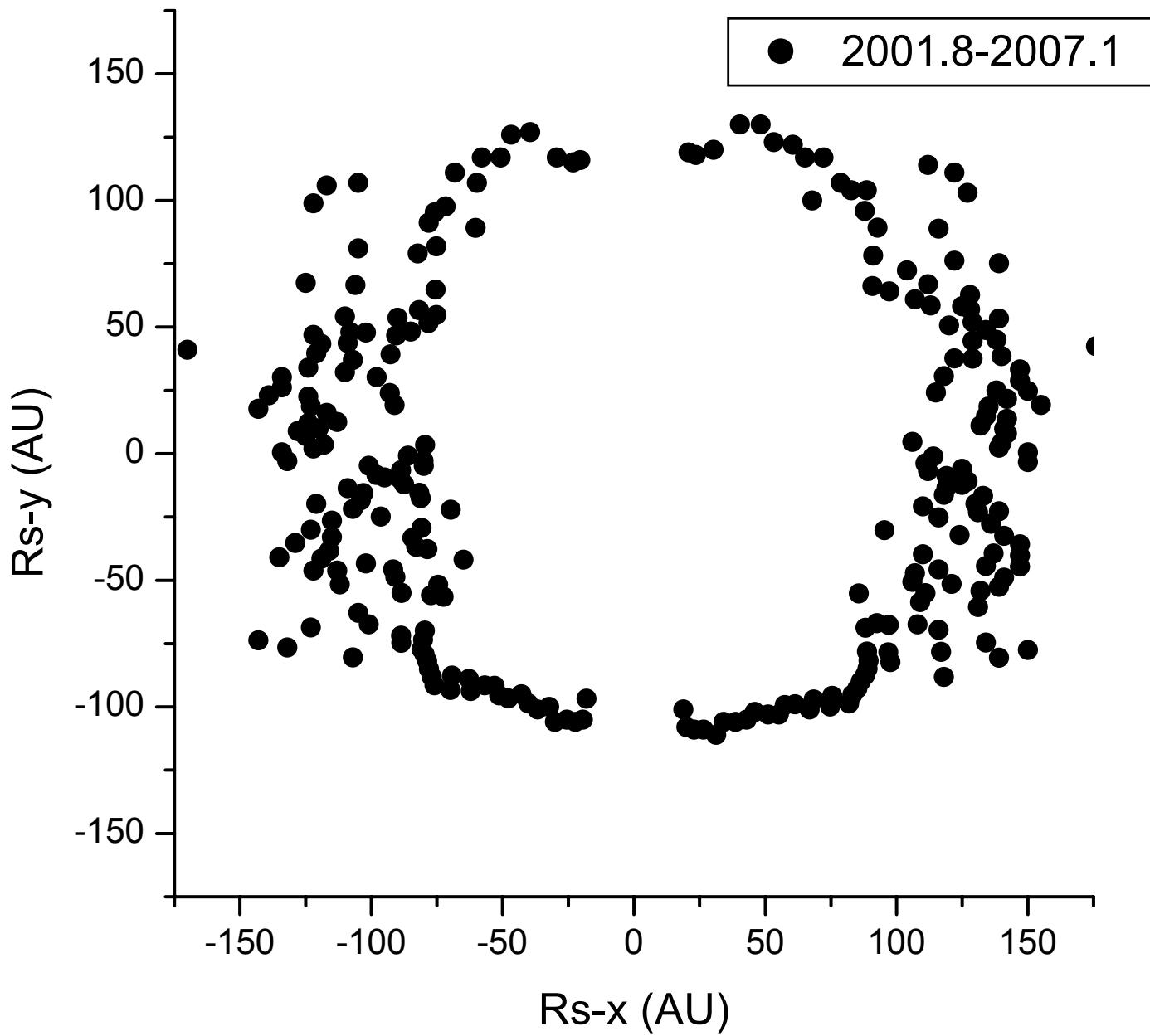


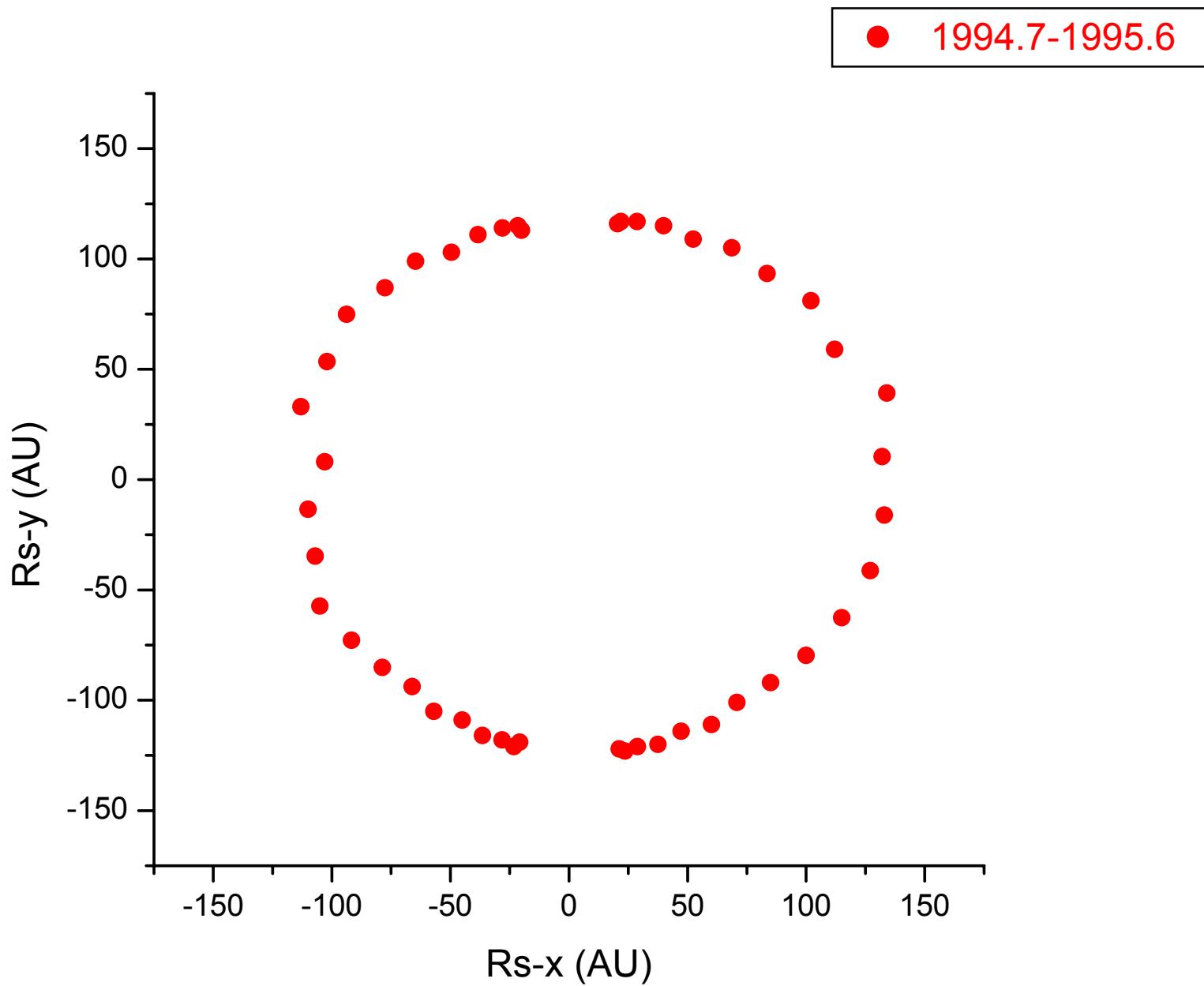
## heliosphere and heliopause *Ulysses* data

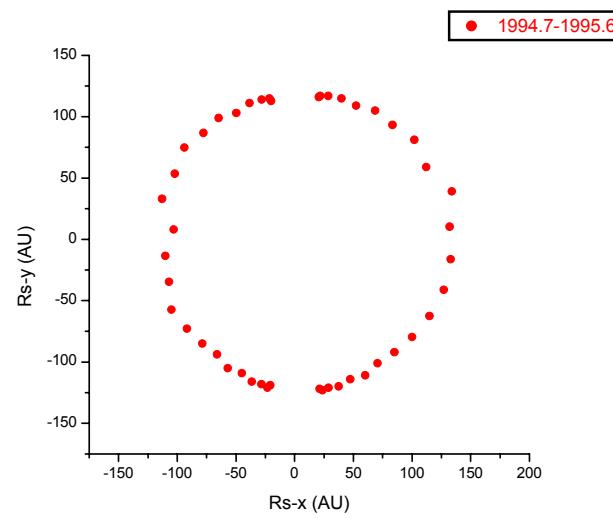
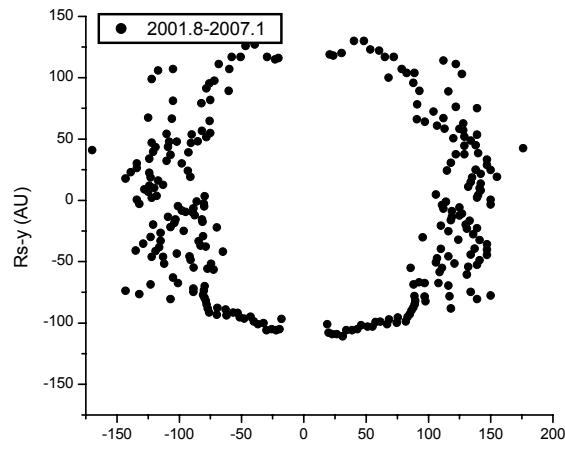
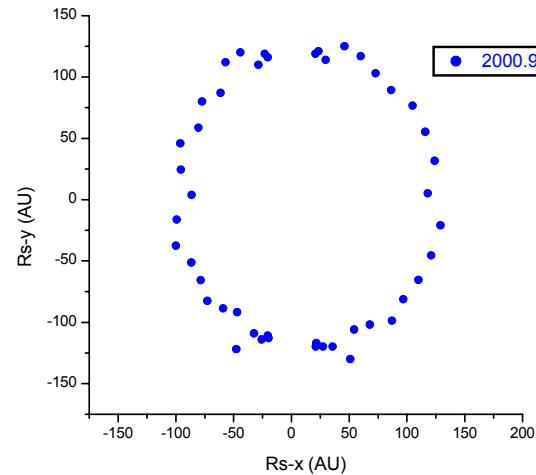
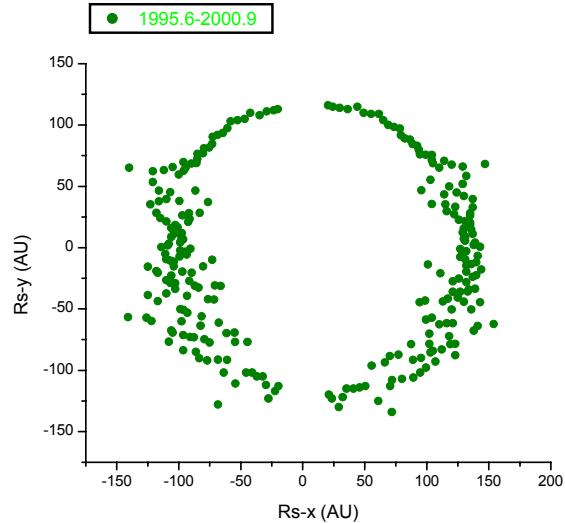










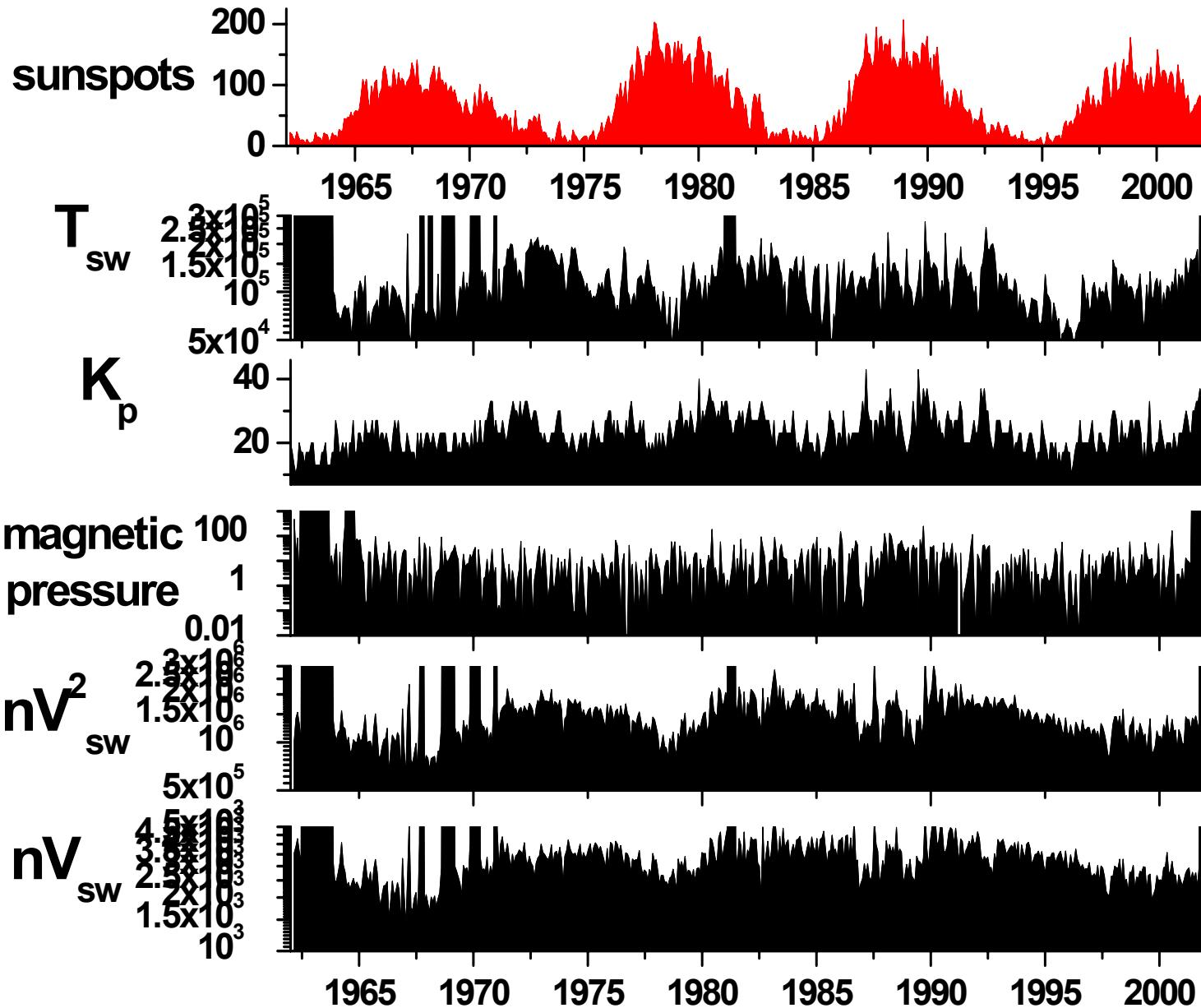


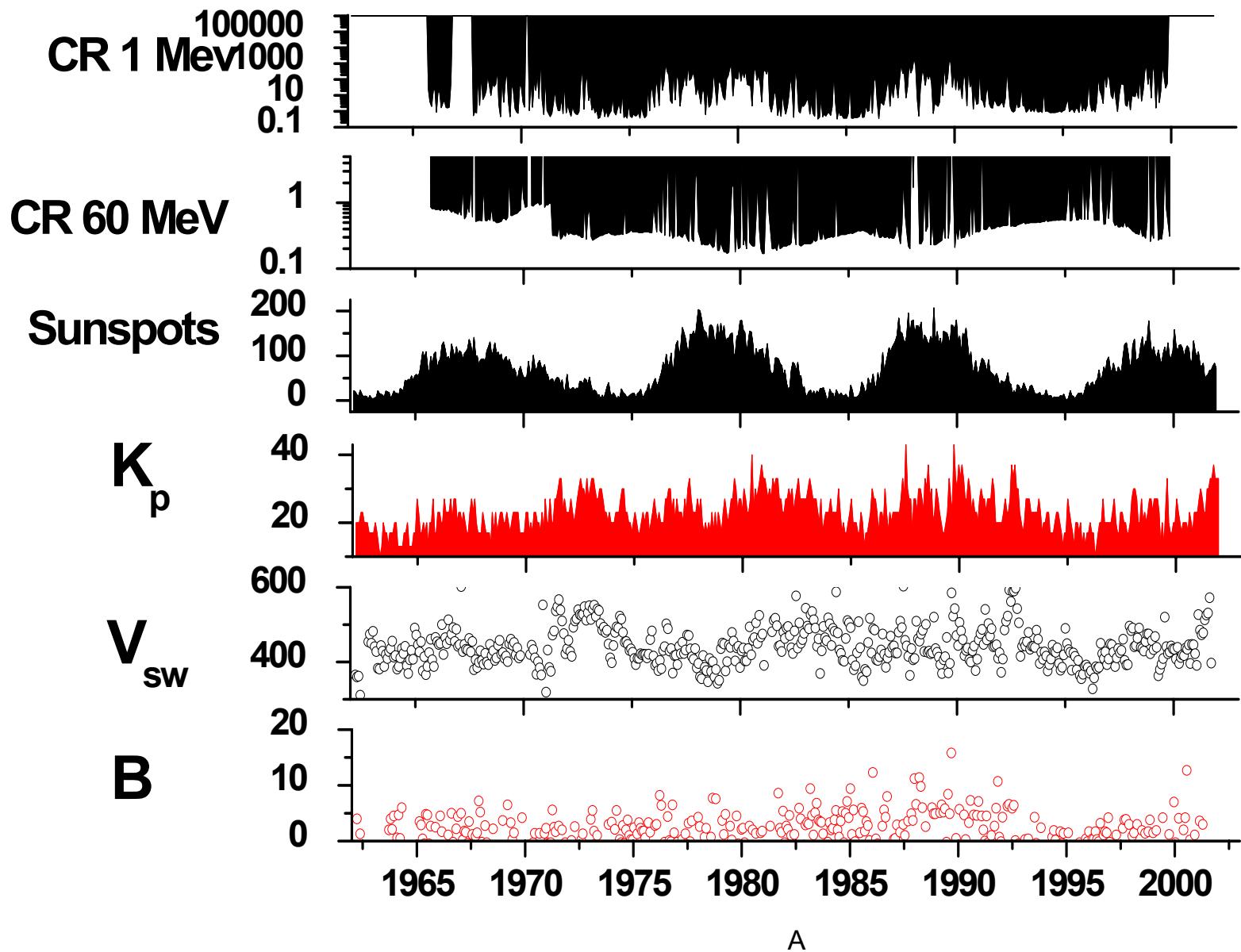
$$\rho_{\infty} = 0.07 \text{ cm}^{-3}$$

$$u_{\infty} = 25 \text{ km/s}$$

$$R_h - R_s = 37.6 \text{ AU}$$

13 days averages from Ulysses daily values



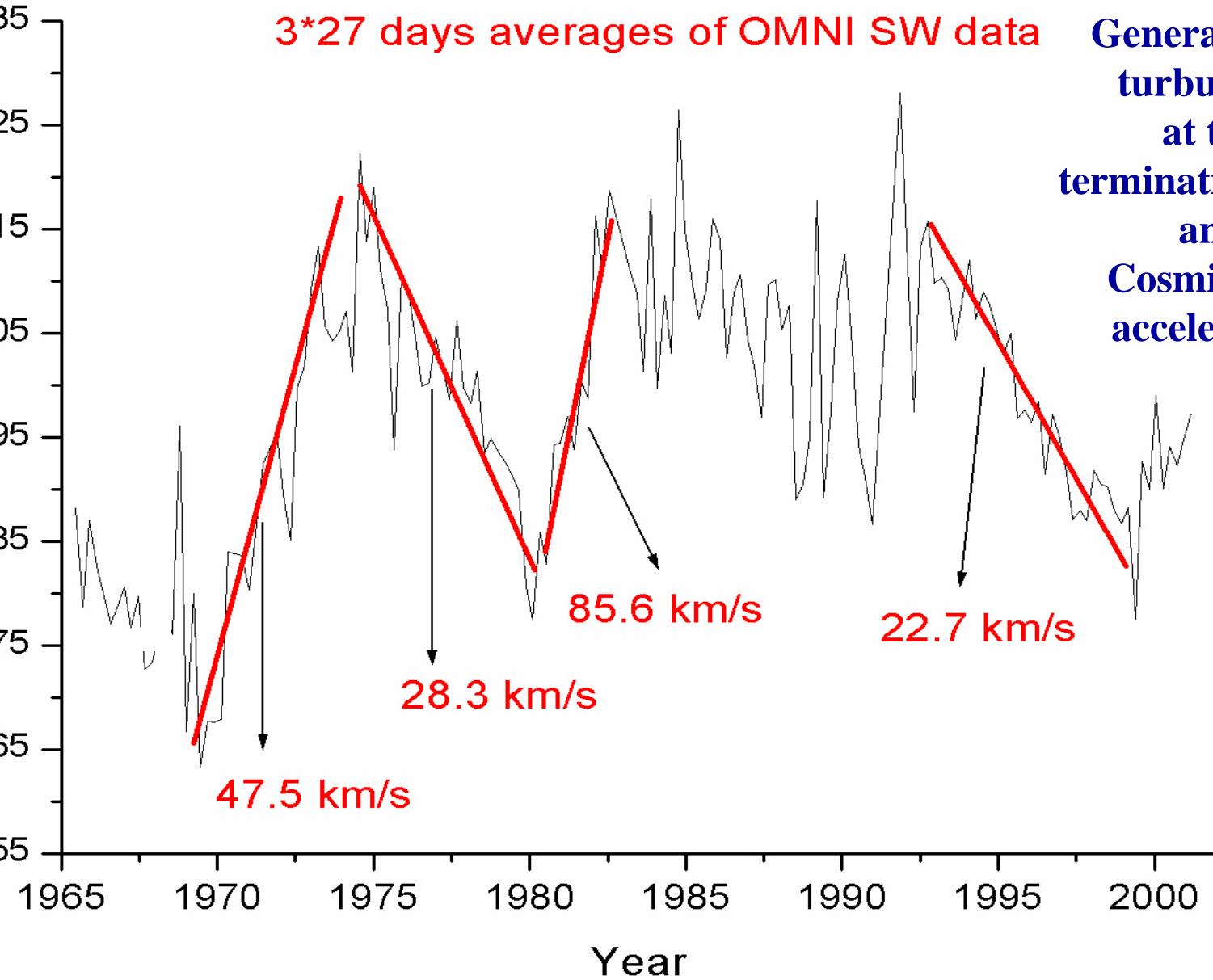




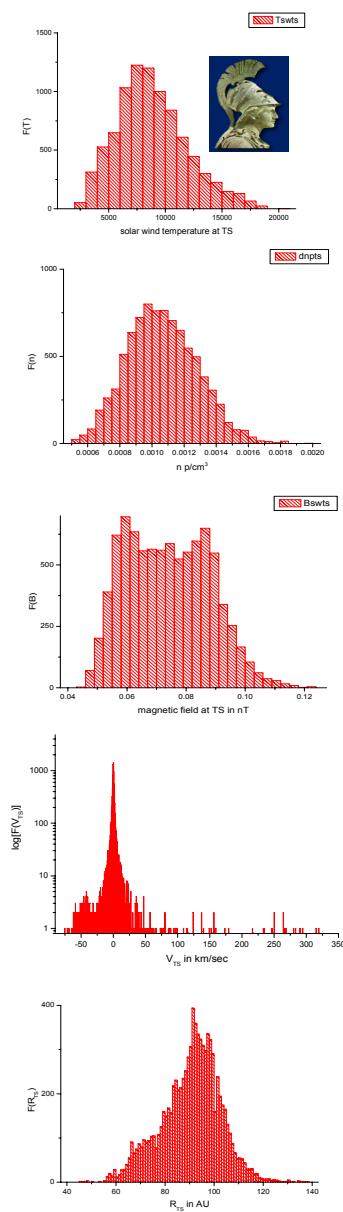
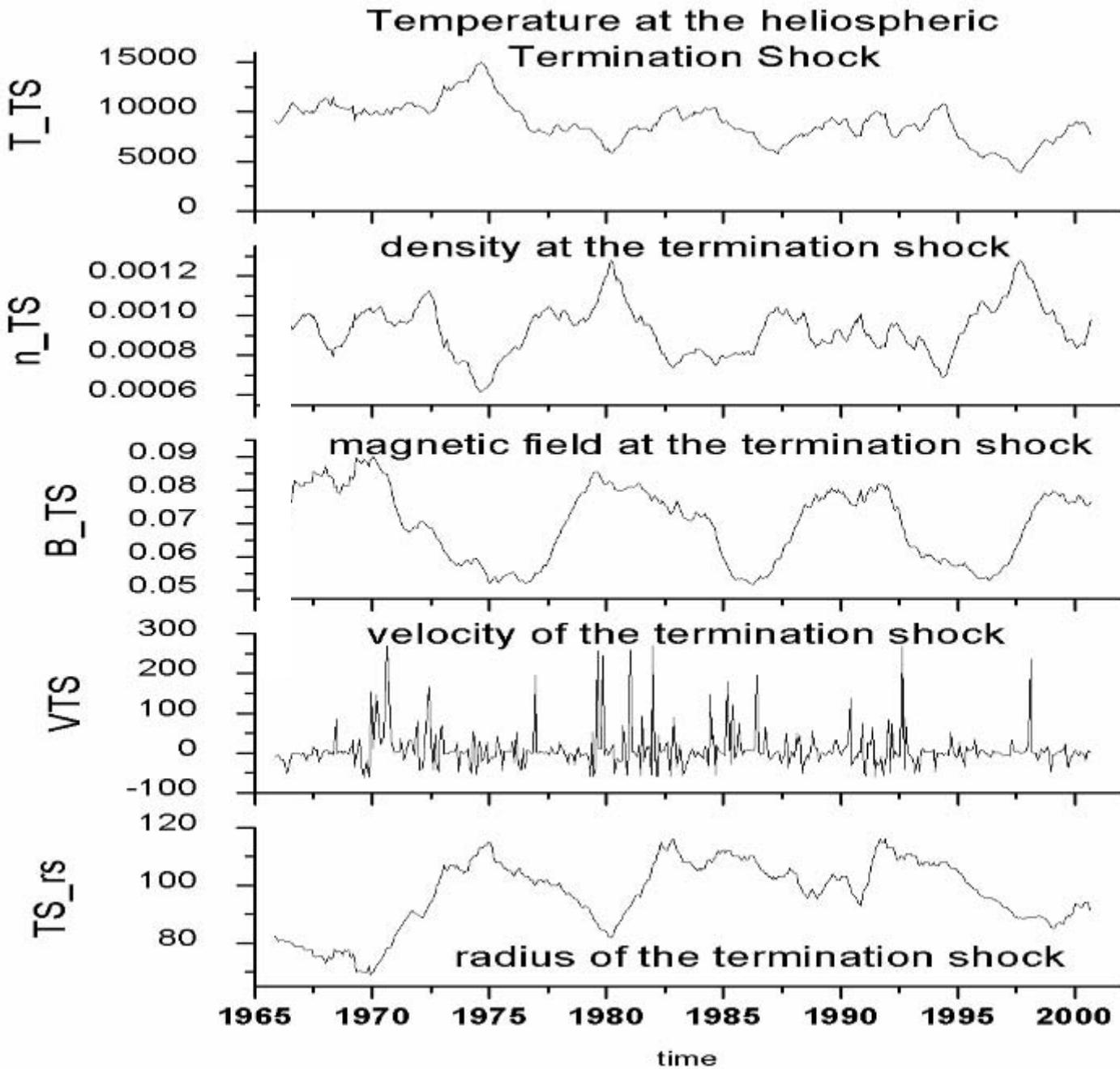
3\*27 days averages of OMNI SW data

Generation of  
turbulence  
at the  
termination shock  
and  
Cosmic Ray  
acceleration

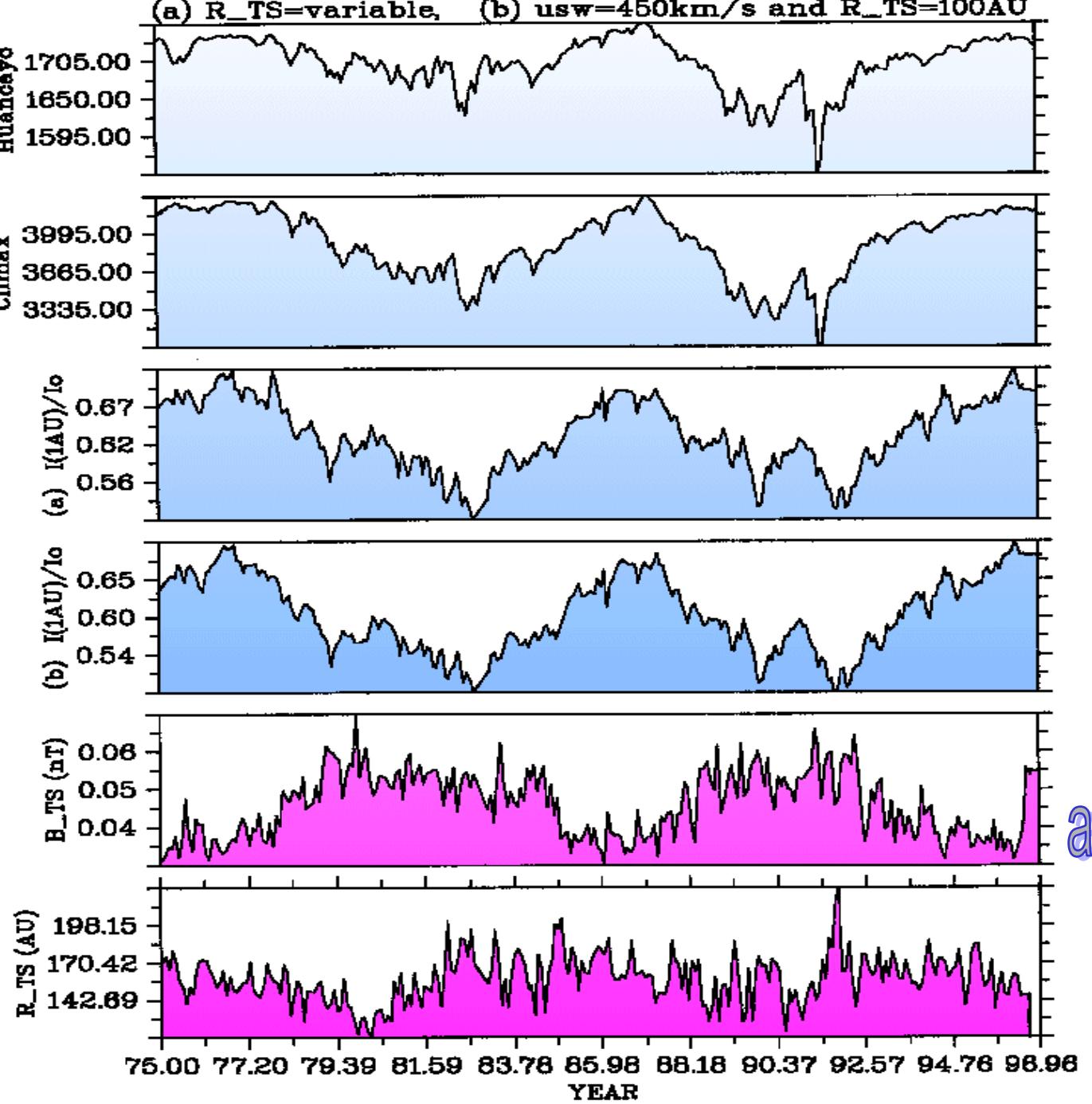
heliospheric termination shock in AU



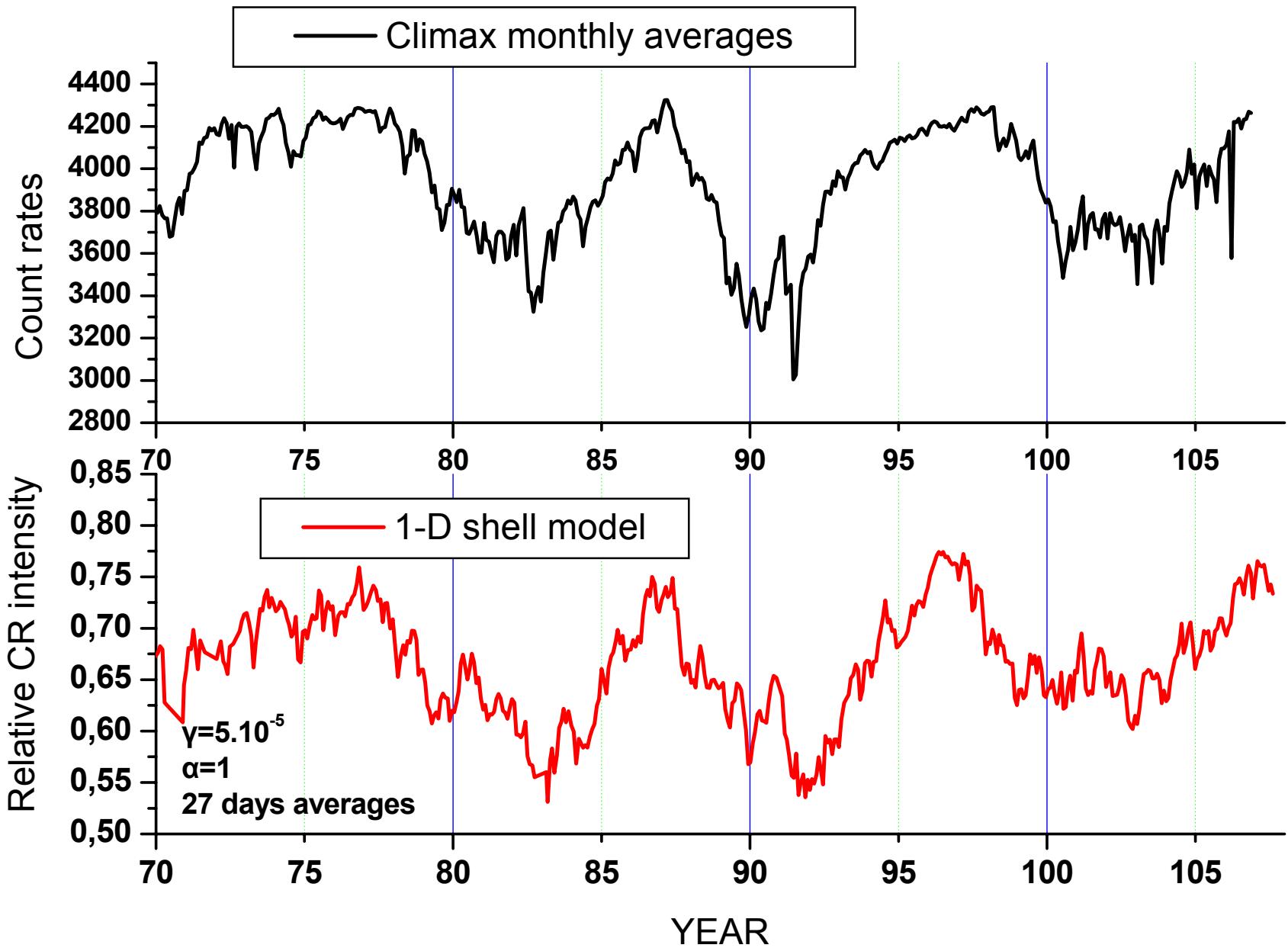
Time variations of the Heliosphere, estimations of the heliospheric termination velocity (OMNI data).



time variations of the Heliosphere: temperature, density, magnetic filed, velocity of the termination shock and radius (OMNI data)



neutron  
monitor  
data  
CR modulation  
model  
with variable  
IMF & heliosphere  
magnetic field  
at termination shock  
heliospheric  
radius



● 1ST SCAN -80 --> +80 DEG

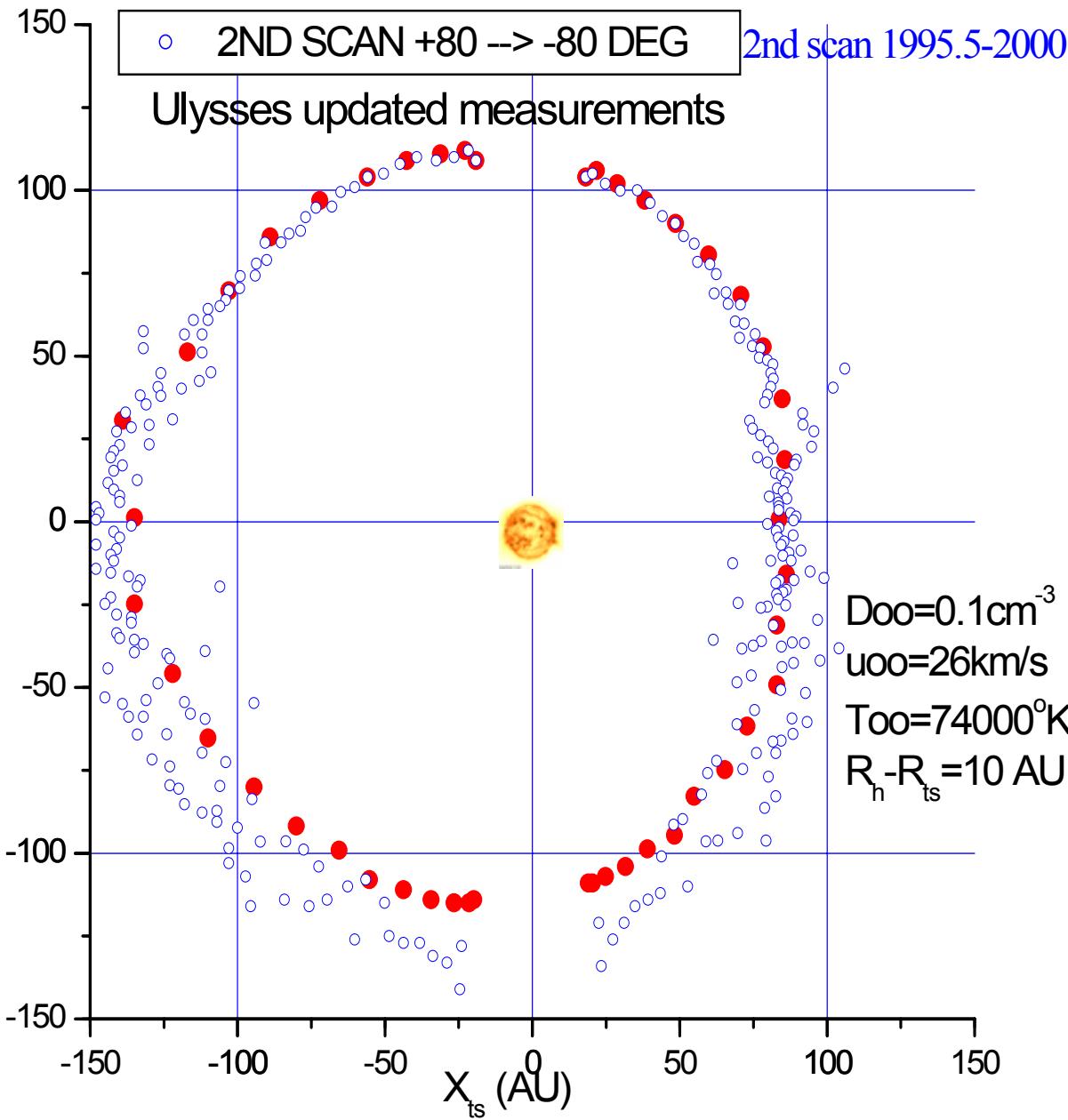
1st scan 1994.4-1995.5

○ 2ND SCAN +80 --> -80 DEG

2nd scan 1995.5-2000

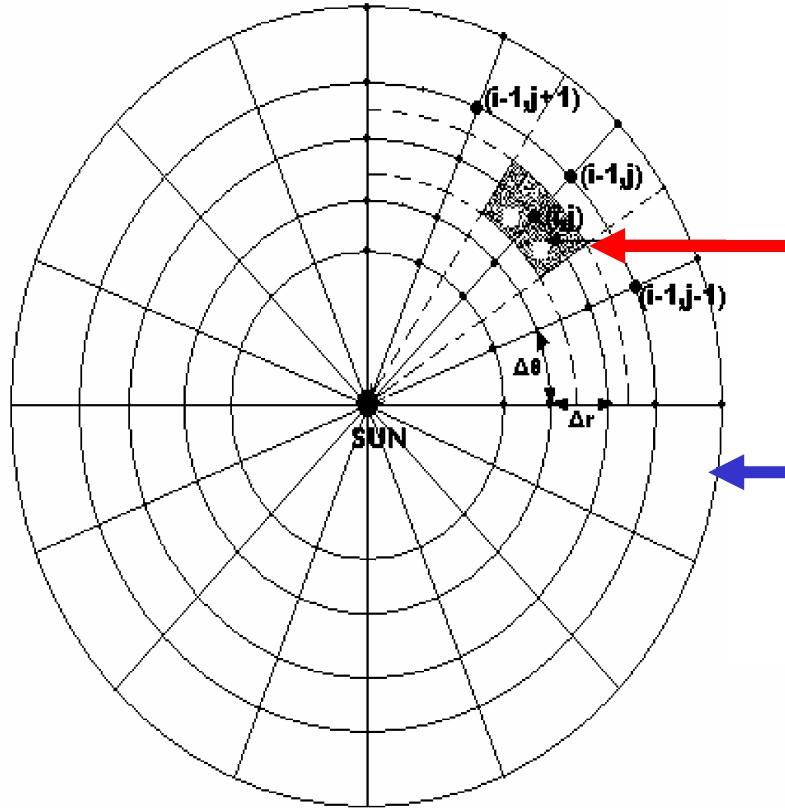
Ulysses updated measurements

$Y_{ts}$  (AU)



asymmetry  
North-South  
East-West

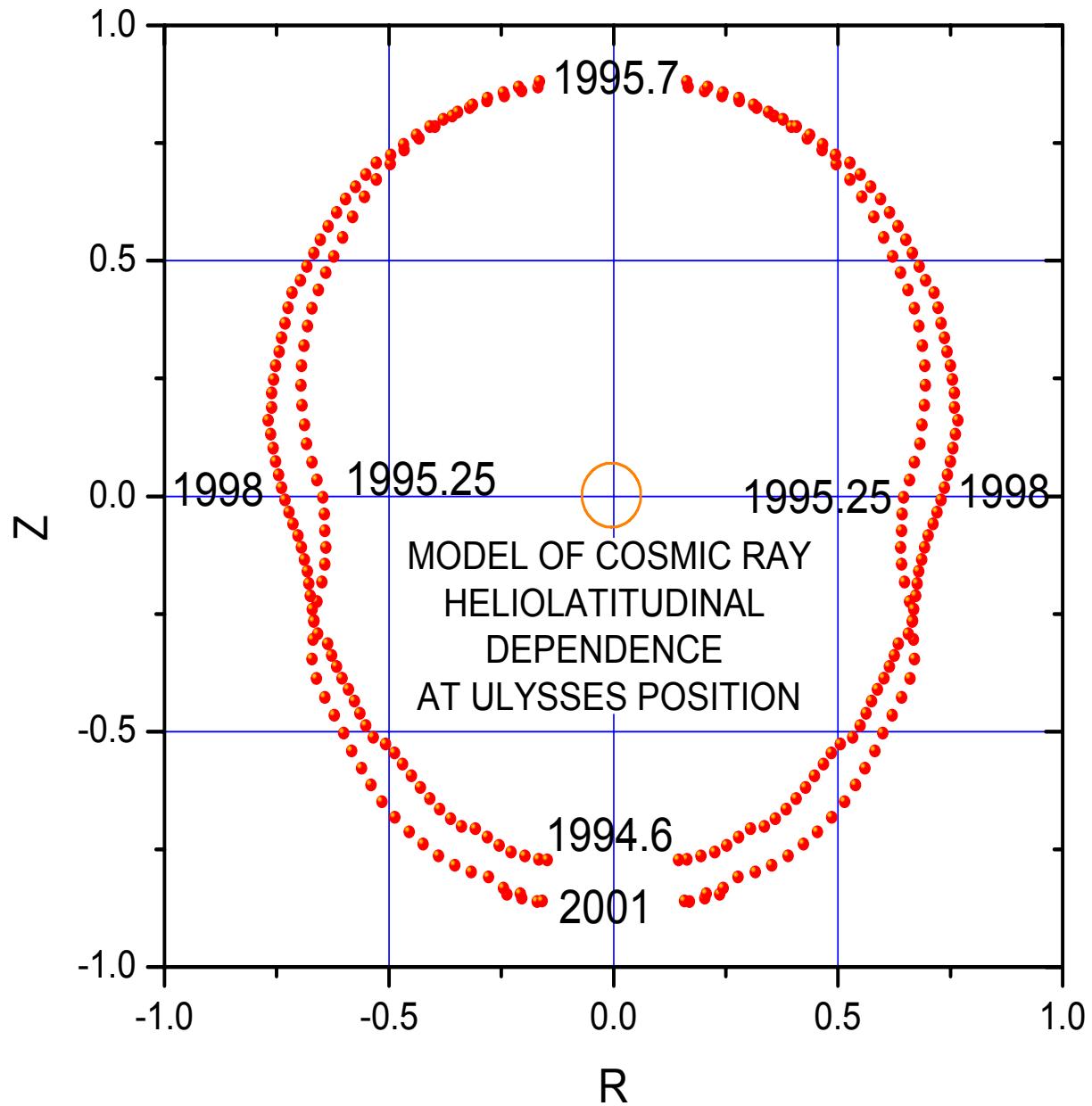
$D_{oo}=0.1\text{cm}^{-3}$   
 $u_{oo}=26\text{km/s}$   
 $T_{oo}=74000^\circ\text{K}$   
 $R_h-R_{ts}=10\text{ AU}$



Spherical  
magnetic  
sector

Heliospheric  
termination  
shock

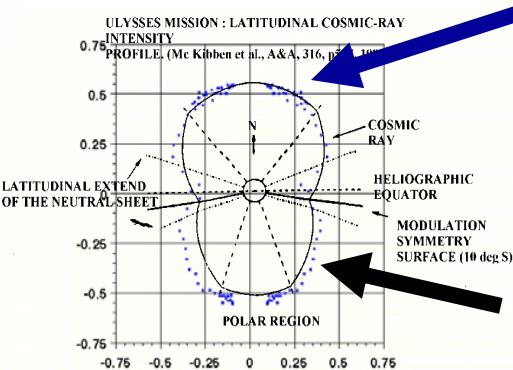
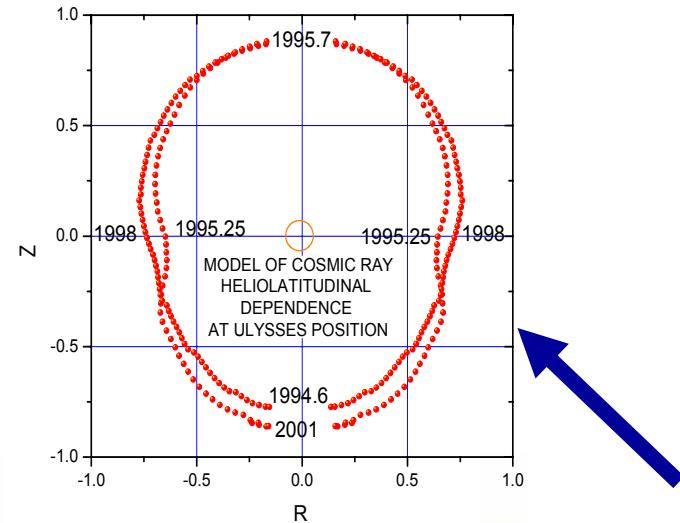
Magnetic heliosphere model (time variable)  
homocentric spherical shells with  
constant magnetic field measured by s/c



**Cosmic ray model: time and latitudinal dependence (polar diagram)**

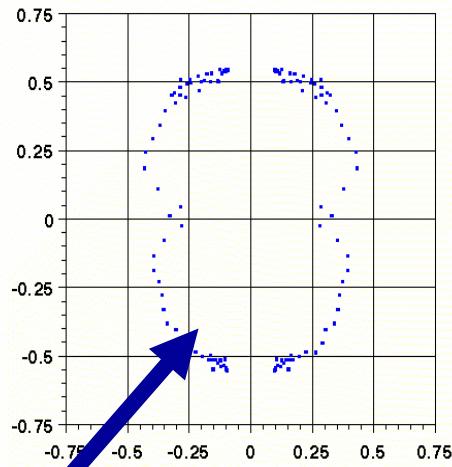


# Cosmic ray latitudinal gradient Ulysses data and model

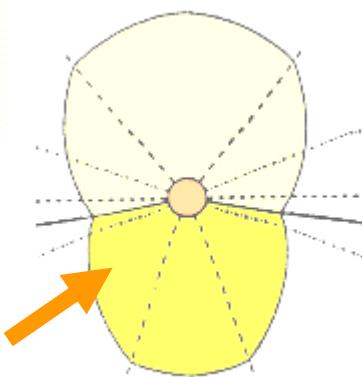


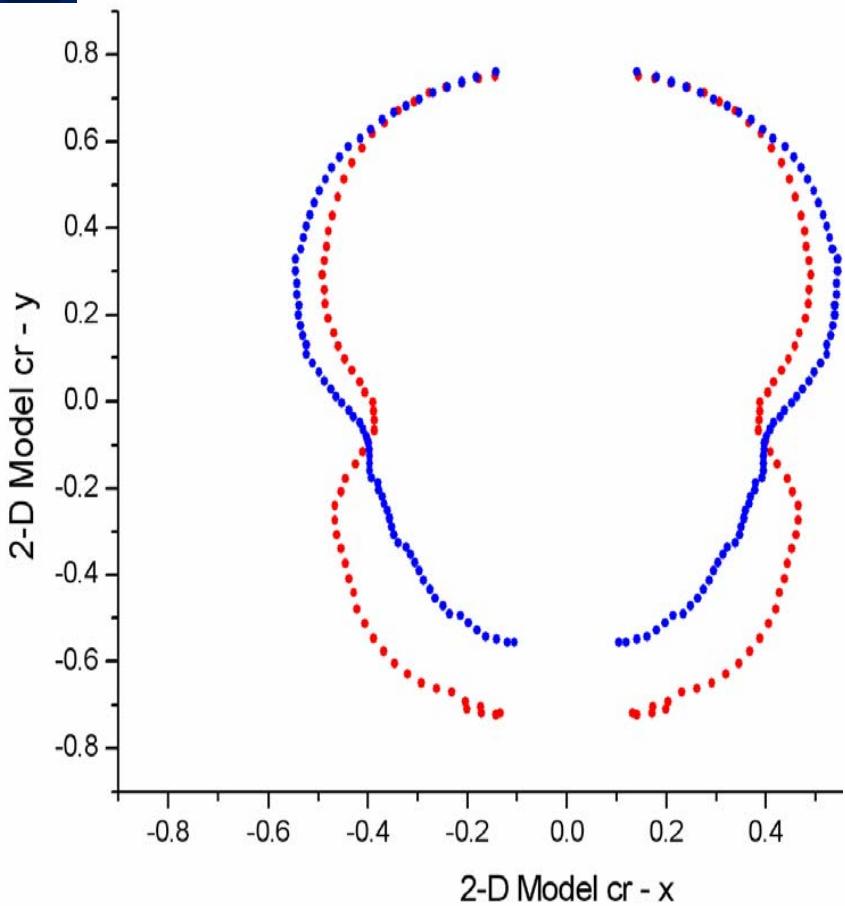
CR model polar diagram

LATITUDINAL COSMIC-RAY INTENSITY PROFILE  
SHELL- MODEL RESULTS

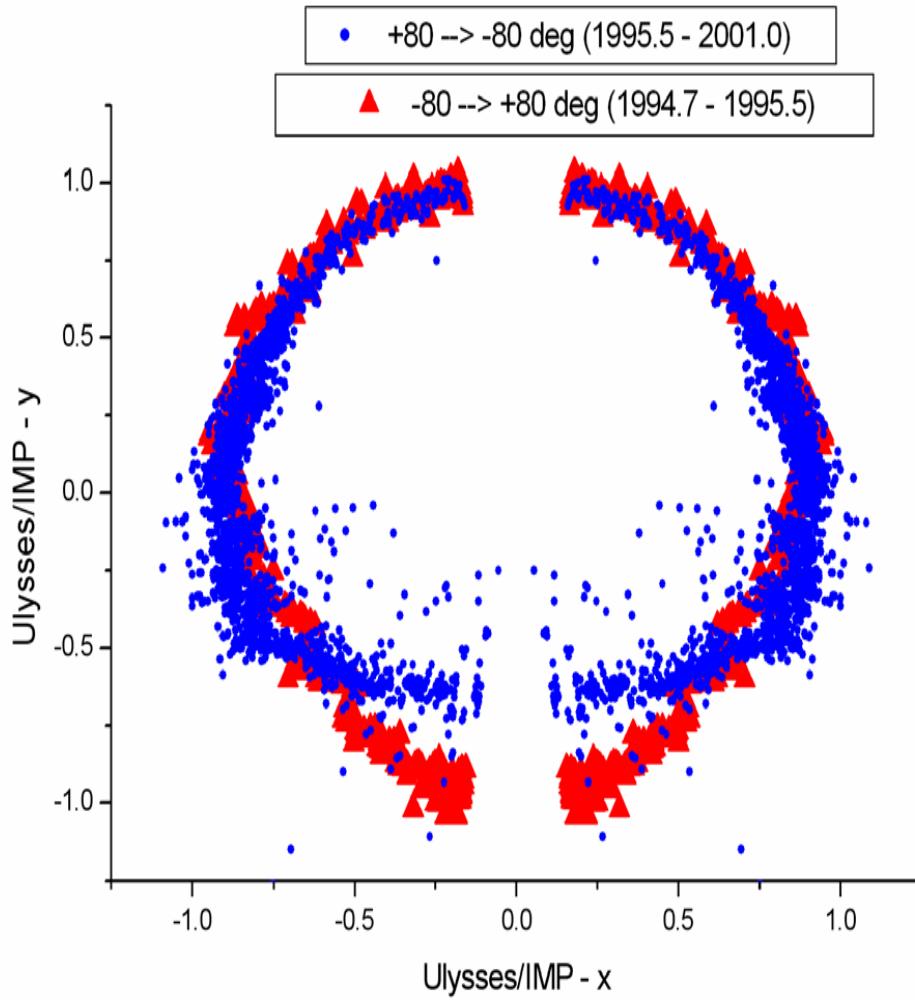


Ulysses cosmic ray measurements  
(McKibben et al 1996)  
polar diagram

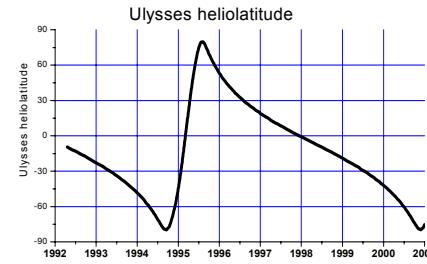
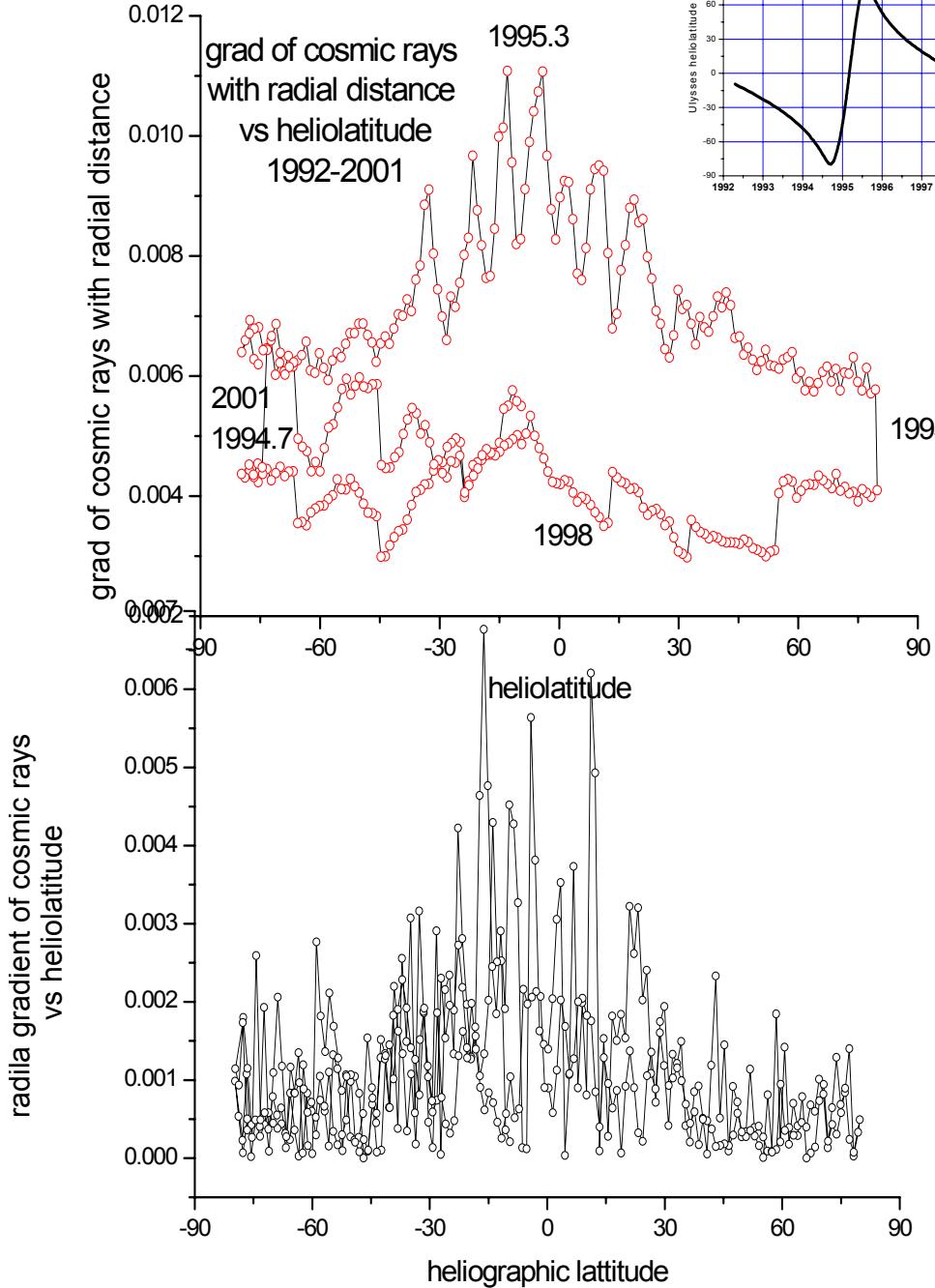




**COSMIC-RAY MODEL  
MEASUREMENTS  
POLAR DIAGRAM**



**ULYSSES COSMIC-RAY  
(320-2100 MeV ) POLAR DIAGRAM**



heliolatitudinal variation of  
cosmic ray radial gradient

model (top) and  
Ulysses data



cosmic ray intensity

0.25

0.20

0.15

0.10

0.05

1980

1985

1990

1995

2000

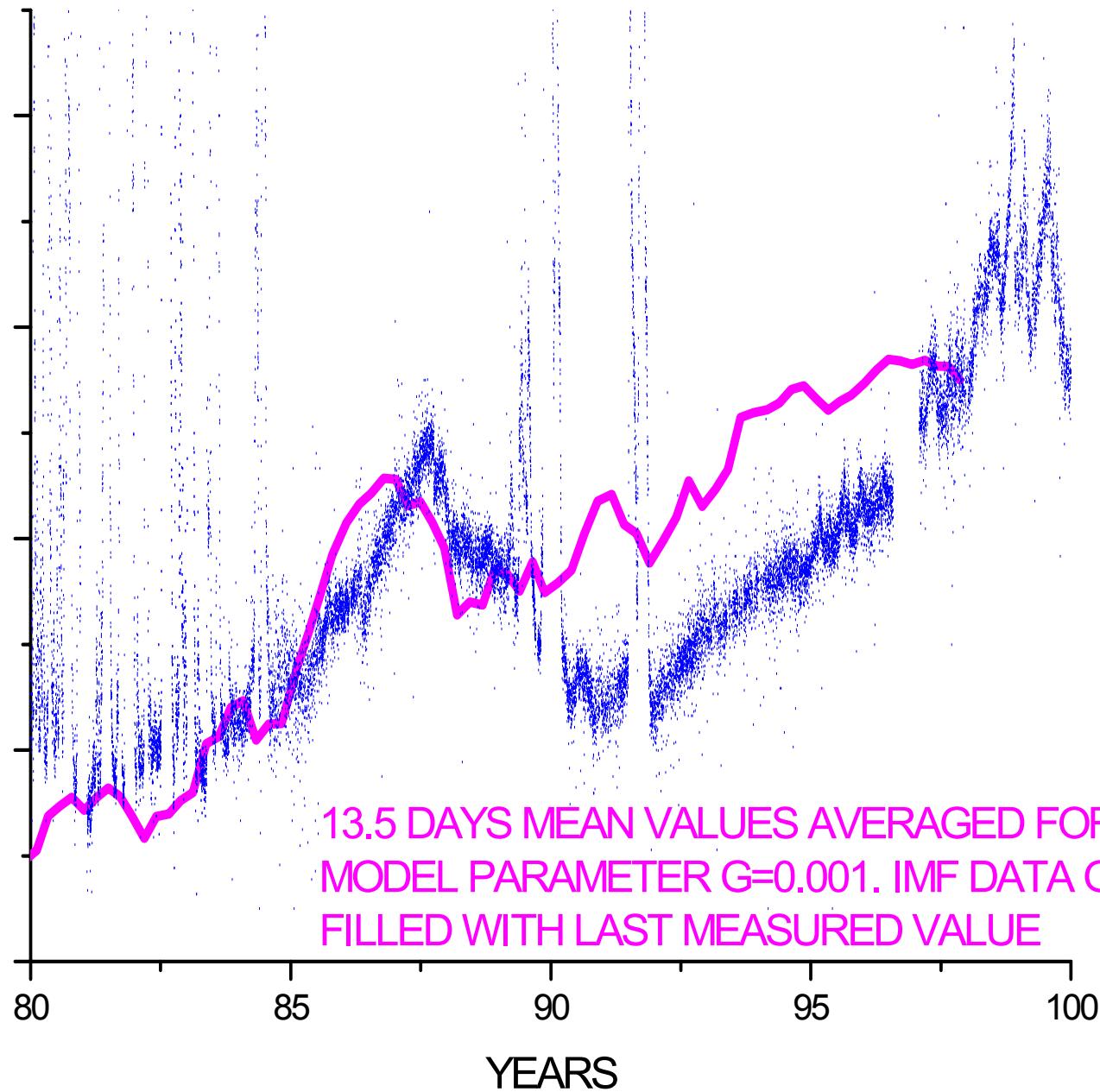
## Voyager 2 data

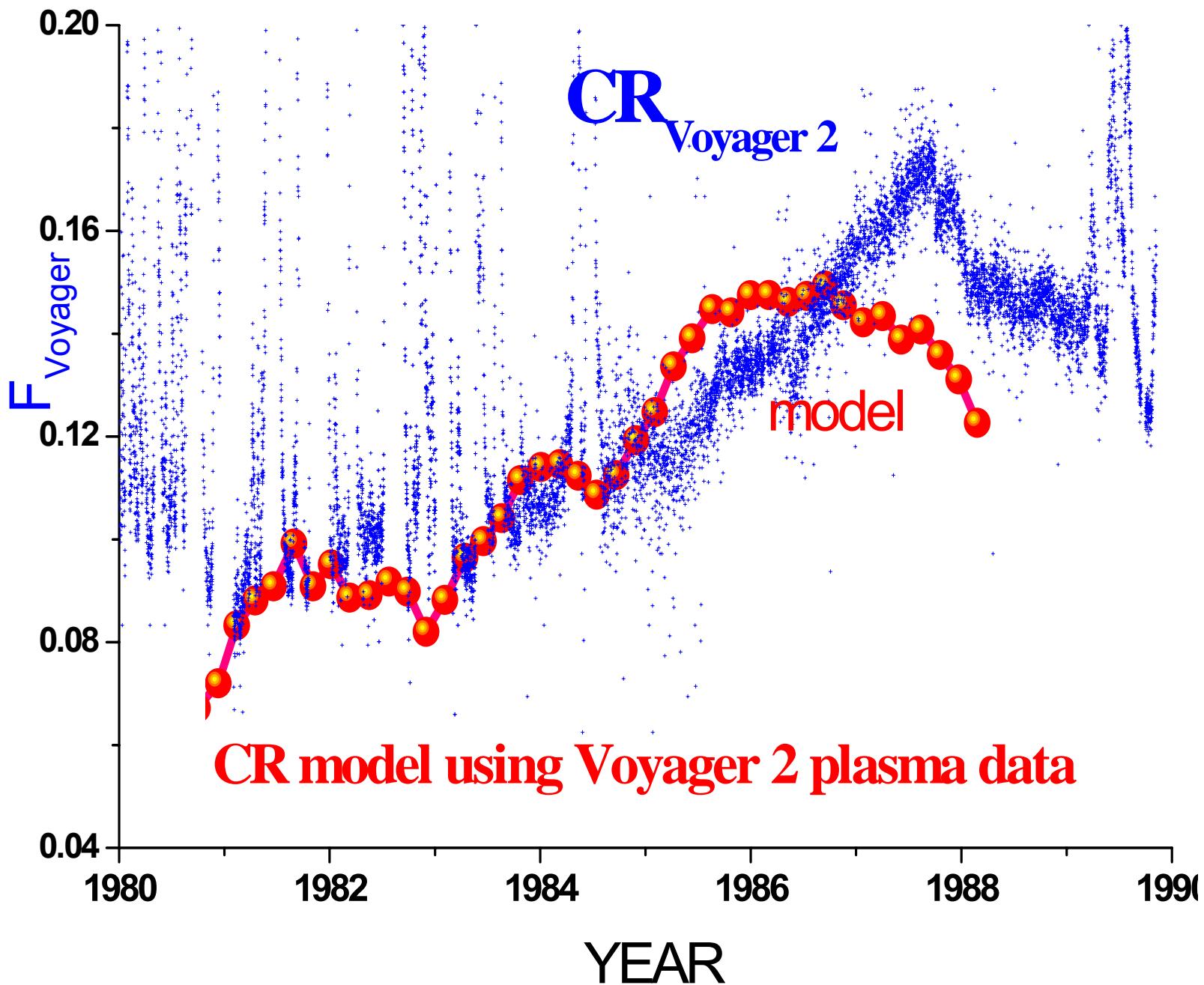
model: 27 day means, averaged over 81 days,  
 $G=0.0003$ , IMF gaps filled,  $R_{TS}$  variable

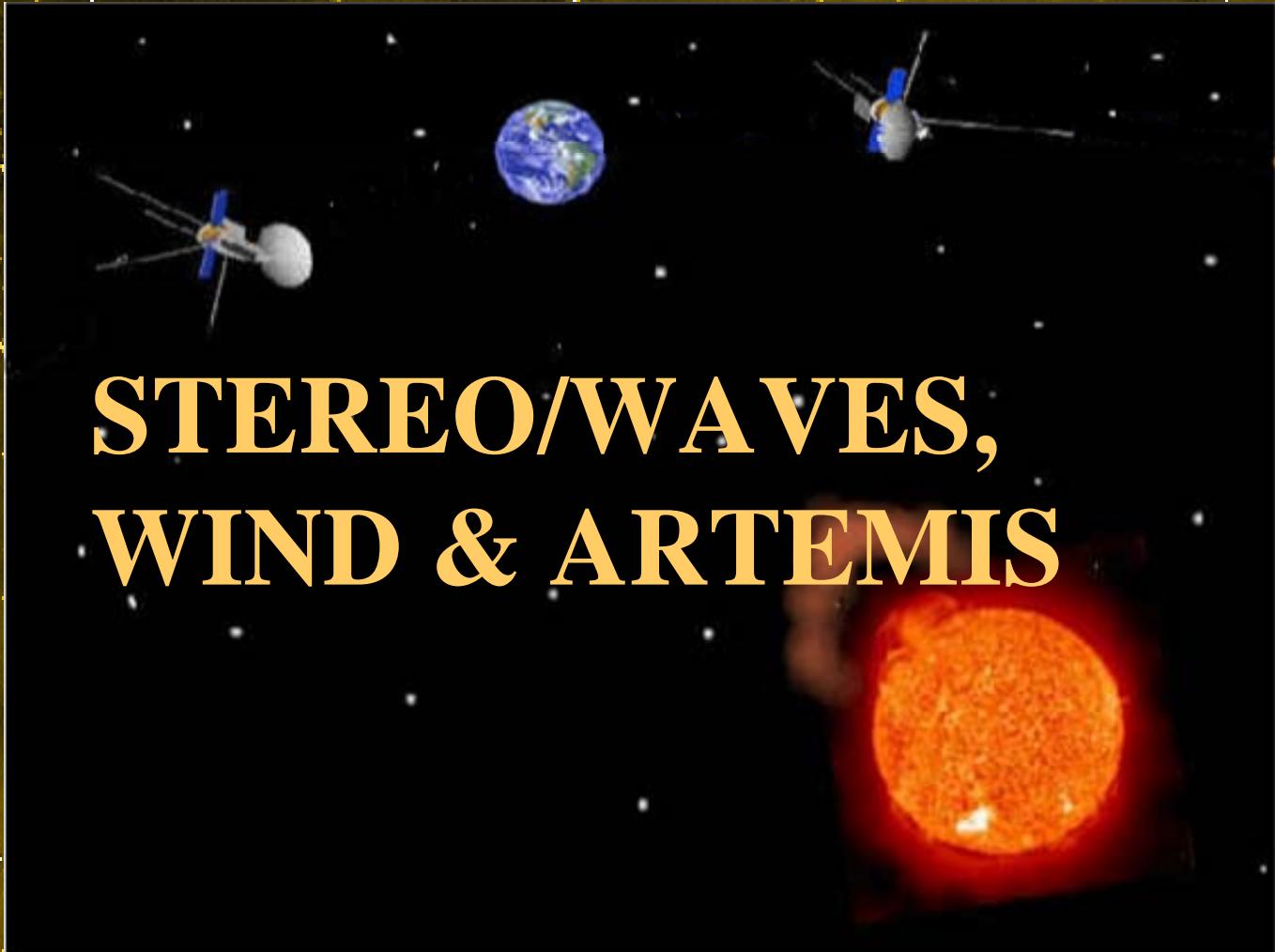


V2\_CR\_RATE

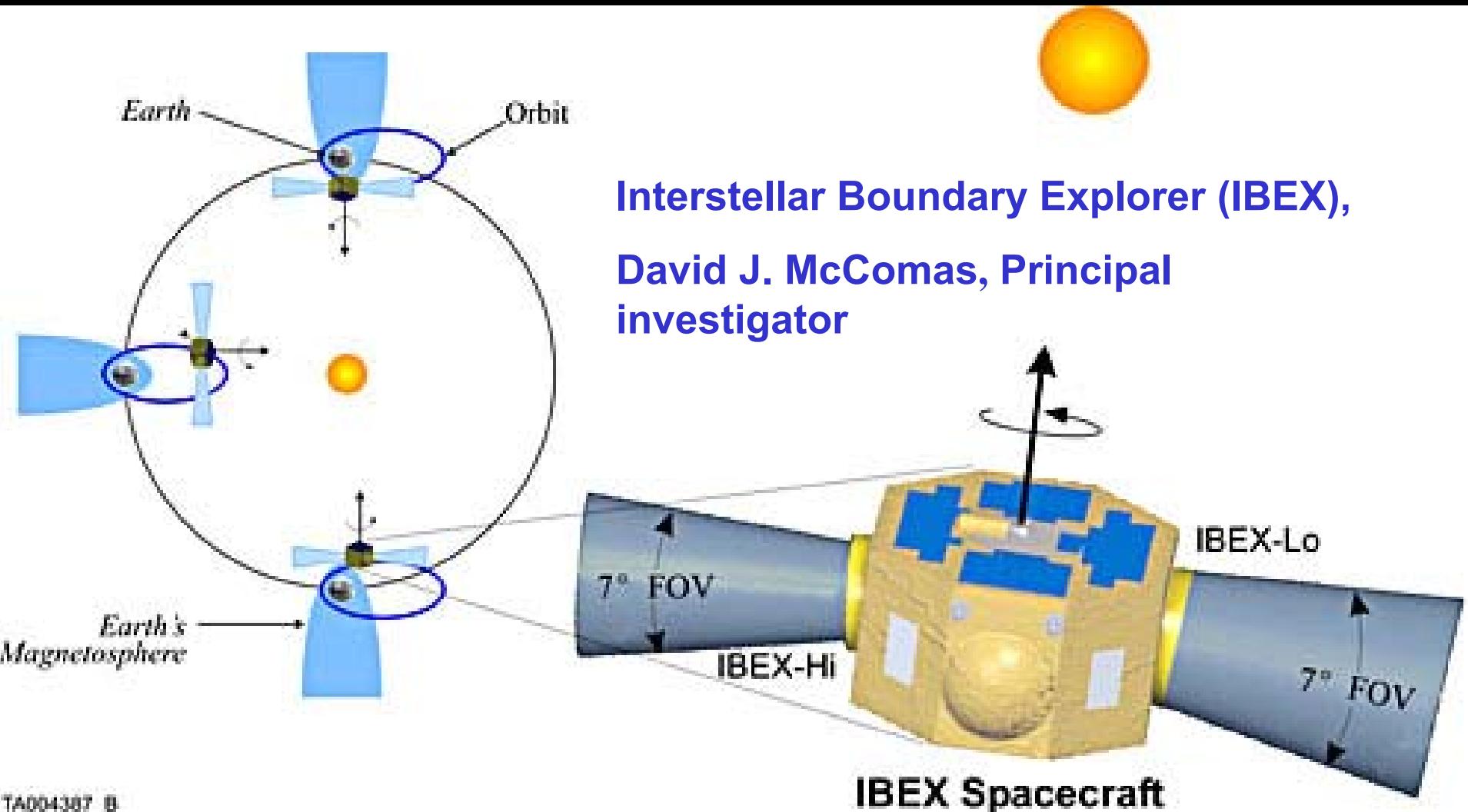
— MODEL\_CR\_RATE







# STEREO/WAVES, WIND & ARTEMIS



Interstellar Boundary Explorer (IBEX),  
David J. McComas, Principal  
investigator

# THE INTERSTELLAR BOUNDARY EXPLORER (IBEX) MISSION

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<sup>(12)</sup>*University of Southern California, Department of Physics and Astronomy*

<sup>(13)</sup>*Moscow State University, Space Research Institute*

<sup>(14)</sup>*University of New Hampshire, Department of Physics*

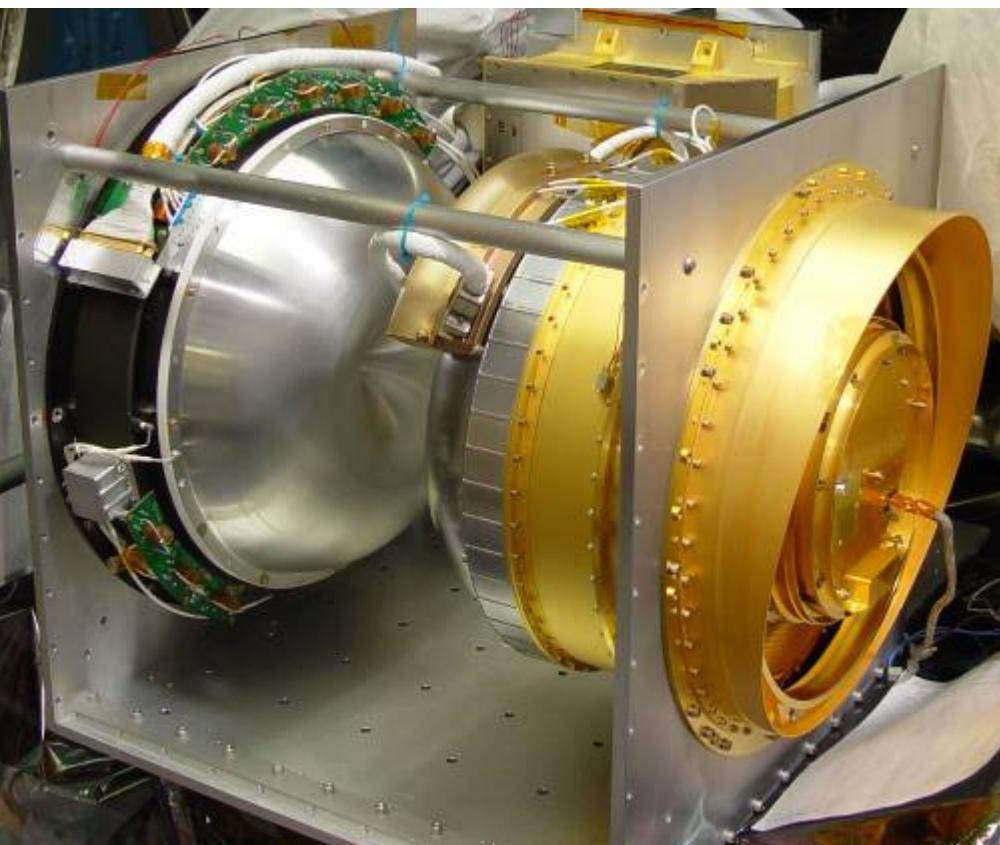
<sup>(15)</sup>*Applied Physics Laboratory, Johns Hopkins University*

<sup>(16)</sup>*University of Montana, Department of Physics*

<sup>(17)</sup>*Orbital Sciences Corporation*

<sup>(18)</sup>*Collaborating Science Institutions*

<sup>(19)</sup>*University of California Riverside*



## ABSTRACT

The Interstellar Boundary Explorer (IBEX) is scheduled to launch in June 2008 to make the first global observations of the heliosphere's interaction with the interstellar medium. IBEX achieves these breakthrough observations by traveling outside of the Earth's

[www.ibex.swri.edu](http://www.ibex.swri.edu).

## 1. IBEX SCIENCE

The sole focused science objective of IBEX is to discover the global interaction between the solar wind

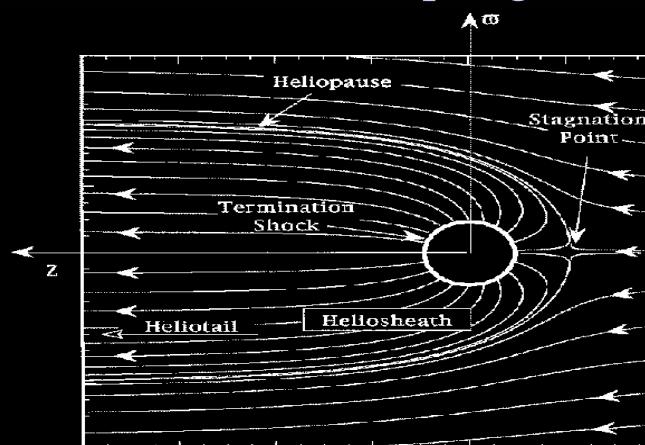


National and Kapodistrian  
University of Athens  
Space Physics course since  
1972  
~20 PhD  
50 MSc theses  
300 PSc theses  
during the last 30 years  
Space Physics group

# Bibliography

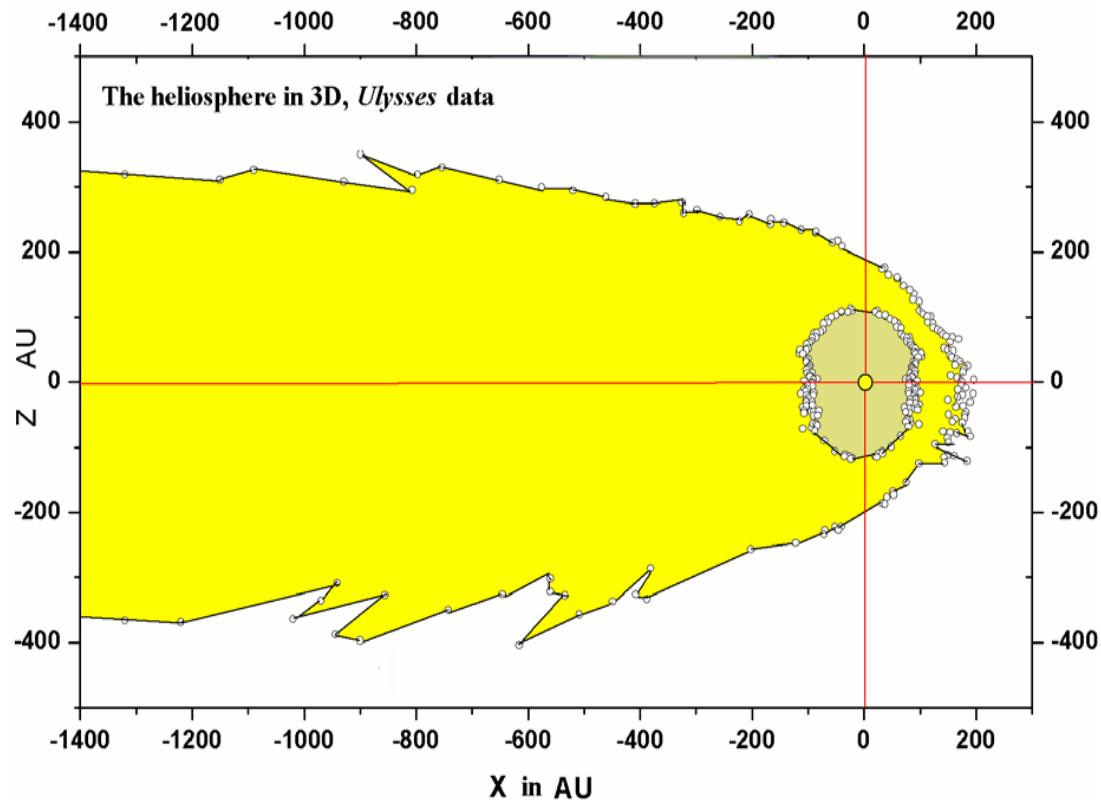
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- Thomas H. Zurbuchen, A New View of the Coupling of the Sun and the Heliosphere, Annual Review of Astronom

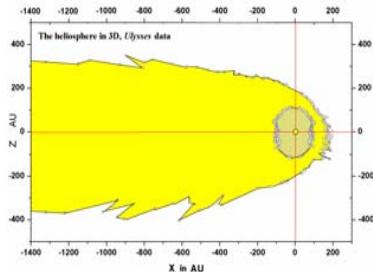
3, 2007





# appendix





# THE LOCATION OF THE HELIOSPHERIC TERMINATION SHOCK

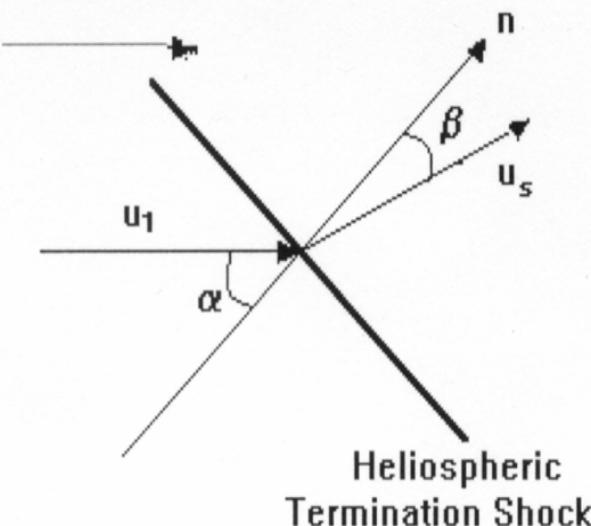


## 2.1. Analysis

From Rankine-Hugoniot shock jump conditions for a strong oblique termination shock, we get (Barnes 1998)

$$u_s \sin \beta = u_1 \sin \alpha \quad (1)$$

solar wind flow



$$u_s \cos \beta = \left( \frac{\gamma - 1}{\gamma + 1} \right) u_1 \cos \alpha \quad (2)$$

$$\rho_s = \rho_1 \left( \frac{\gamma + 1}{\gamma - 1} \right) \quad (3)$$

$$p_s = \rho_1 u_1^2 \left( \frac{2}{\gamma + 1} \right) \cos^2 \alpha , \quad (4)$$

FIG. 1.—Solar wind passing through an oblique termination shock



# solar wind flow

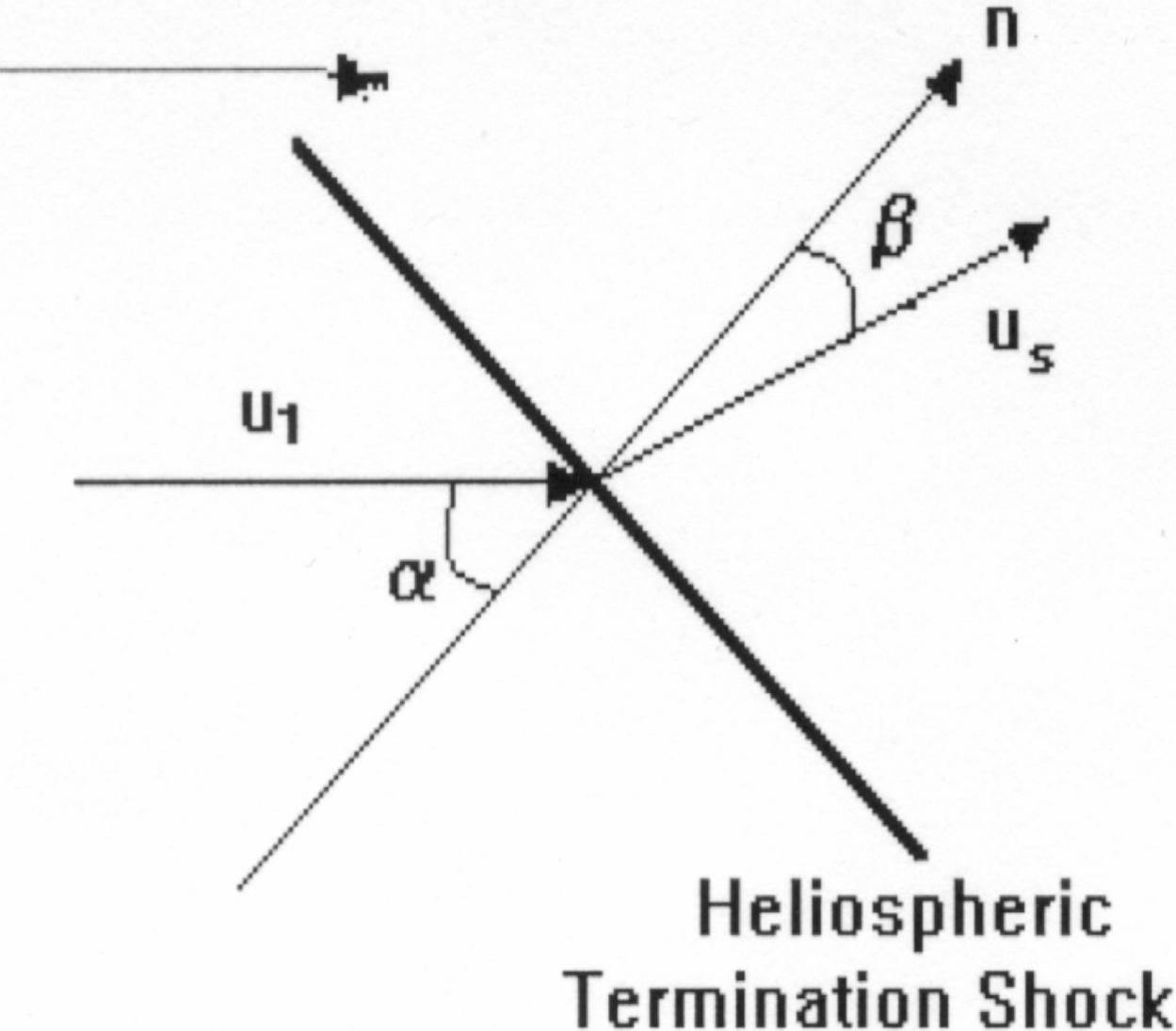


FIG. 1.—Solar wind passing through an oblique termination shock



Then equation (4), with the help of equations (2) and (5), becomes

$$p_s = \rho_1 u_1^2 \frac{2(\gamma + 1)}{(\gamma - 1)^2} \frac{\cos^2 \beta}{[4\gamma/(\gamma - 1)^2] \cos^2 \beta + 1}. \quad (6)$$

The pressure distribution  $p_s$  on the termination shock is obtained applying the Bernoulli equation for the flow between the termination shock and the heliopause, assuming that the flow is incompressible (see § 1):

$$\frac{1}{2}\rho_s u_s^2 + p_s = \frac{1}{2}\rho_\infty u_\infty^2 + p_\infty. \quad (7)$$

Substituting  $\rho_s$  from equation (3) and  $u_s$  from equation (5) and then solving for  $p_s$ , we take

$$p_s = p_\infty + \frac{1}{2} \rho_\infty u_\infty^2 - \frac{1}{2} \rho_1 \left( \frac{\gamma + 1}{\gamma - 1} \right) \times \frac{u_1^2}{[4\gamma/(\gamma - 1)^2] \cos^2 \beta + 1}. \quad (8)$$



The solar wind density  $\rho_1$  upstream of the termination shock varies with radial distance  $r$  like

$$\rho_1 = \rho_o \left( \frac{r_o}{r_s} \right)^2, \quad (9)$$

$$\left( \frac{r_s}{r_o} \right)^2 = \frac{\rho_o (\gamma + 1) \{ u_1^2 + [u_s^2 / (\gamma - 1)] \}}{2\gamma(p_\infty + \frac{1}{2}\rho_\infty u_\infty^2)}.$$



We express the **velocity potential** of the flow after the termination shock in the form (**Fahr et al. 1993; Nerney & Suess 1995**)

where P are the associated Legendre polynomials

$$\Phi = \sum_{lm} (A_{lm} r^l + B_{lm} r^{-(l+1)}) \cos m\phi P_l^m(\cos \theta)$$

$$\Phi = A_o + \frac{B_o}{r} + r(A \cos \phi \sin \theta + B \cos \theta) + \frac{1}{r^2} (\Gamma \cos \phi \sin \theta + \Delta \cos \theta)$$

$$u_r = -\frac{\partial \Phi}{\partial r} = \frac{B_o}{r^2} - (A \cos \theta \sin \theta + B \cos \theta) + \frac{2}{r^3} (\Gamma \cos \phi \sin \theta + \Delta \cos \theta)$$

$$u_\theta = -\frac{1}{r} \frac{\partial \Phi}{\partial \theta} = -A \cos \phi \cos \theta + B \sin \theta - \frac{1}{r^3} (\Gamma \cos \phi \cos \theta - \Delta \sin \theta)$$

$$u_\phi = -\frac{1}{r \sin \theta} \frac{\partial \Phi}{\partial \phi} = A \sin \phi + \frac{\Gamma \sin \phi}{r^3}.$$

The boundary conditions that we use are the following:

1.  $u(r \rightarrow \infty) = -u_\infty \hat{z};$
2.  $r_s(\theta = \pi/2, \phi = 0) = r_s(\theta = \pi/2, \phi = \pi);$
3.  $u(r = r_{hp}, \theta = 0) = 0;$
4.  $u[r = r_s(\theta = 0)] = (\gamma - 1)/(\gamma + 1)u_1.$

From condition 2 we find that  $A = 0$  and  $\Gamma = 0$ .

From condition 1

$$B = u_\infty .$$

From condition 3 we have  $B_o = \left[ B - \frac{2\Delta}{r_h^3(\theta = 0)} \right] r_h^2(\theta = 0)$

$$\Delta = \frac{\{[(\gamma - 1)/(\gamma + 1)]u_1 + u_\infty\}r_s^2(\theta = 0) - u_\infty^2 r_h^2(\theta = 0)}{2\{[1/r_s(\theta = 0)] - [1/r_h(\theta = 0)]\}}.$$

the only unknown parameters are  
the termination shock radius  
and the heliopause radius  $r_s$   $r_h$

$r_s(0)$  can be determined from:

$$\left(\frac{r_s}{r_o}\right)^2 = \frac{\rho_o(\gamma + 1)\{u_1^2 + [u_s^2/(\gamma - 1)]\}}{2\gamma(p_\infty + \frac{1}{2}\rho_\infty u_\infty^2)}.$$

$r_h(0)$  can be determined from the one-dimensional model by  
Khabibrakhmanov et al. 1996)

$r_h(0)$ -  $r_s(0)$ =37.6 AU .

# CR modulation

$$J = J_o \exp(-\gamma u_{sw} B^\alpha)$$

$$\begin{aligned} J(i, j) = & \left( J(i - 1, j) \exp(-\gamma_1 u_{sw} B_{(i-1,j)}^\alpha) \right. \\ & + J(i - 1, j - 1) \exp(\gamma_2 u_{sw} B_{(i-1,j-1)}^\alpha) \\ & \left. + J(i - 1, j + 1) \exp(-\gamma_3 u_{sw} B_{(i-1,j+1)}^\alpha) \right) / 3.0, \end{aligned}$$